



**Porous silicon and Si nanoparticles:
new photonic and electronic materials
*Technologies and physics properties***

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OUTLINE

1

Quantum confined effect

2

Technology of nano- and Porous Si

3

Optical properties

Surface

Luminescence

Electrical properties

4 **Applications**

Wave-guides,
optical fibers,
filters,
mirrors

Chemical &
bio-sensors

Photonic
crystals

Microelectronics:
SOI, Si epitaxy

Solar
Cells

Hydrogen
reservoirs

Explosive
materials

LED,

Bioreactors,
synthesis

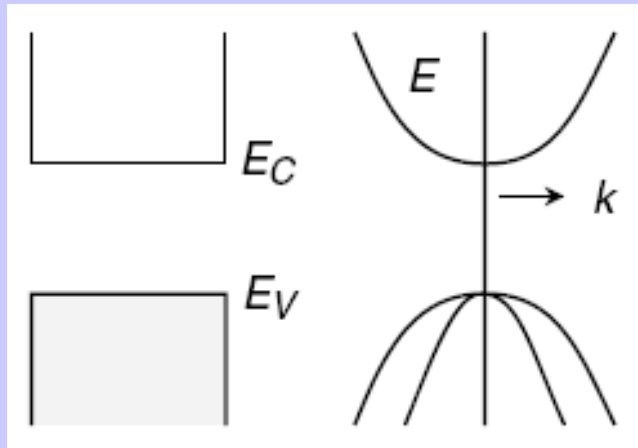
Medicine:
Implants,
Diagnostics
electrophoresis,
drug deliver

Evolution of modern semiconductor physics: *from bulk to nano*

- Band theory + doping
- Effective mass theory

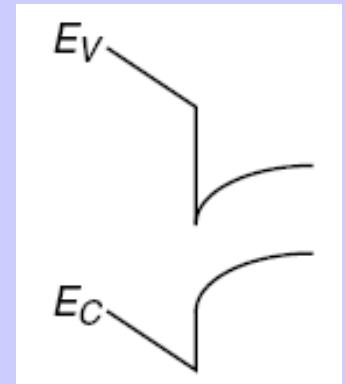
$$\mathbf{p} = \hbar \mathbf{k}$$

$$E = \frac{\hbar^2 k^2}{2m_0}$$

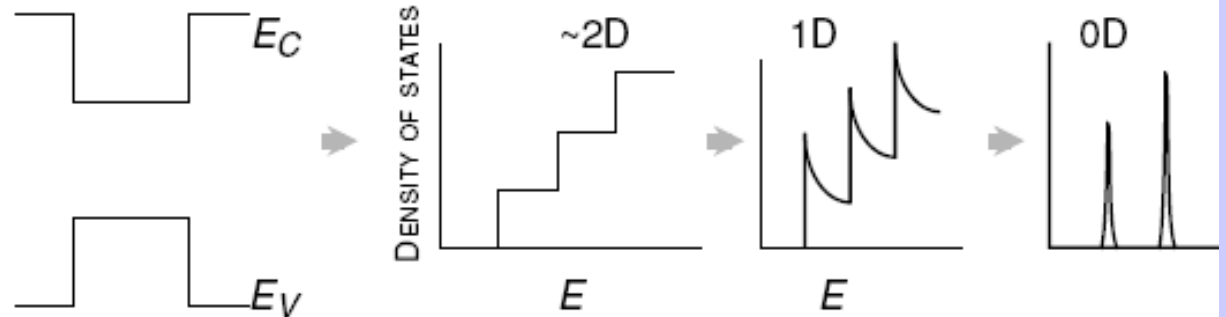


Semiconductor transistor

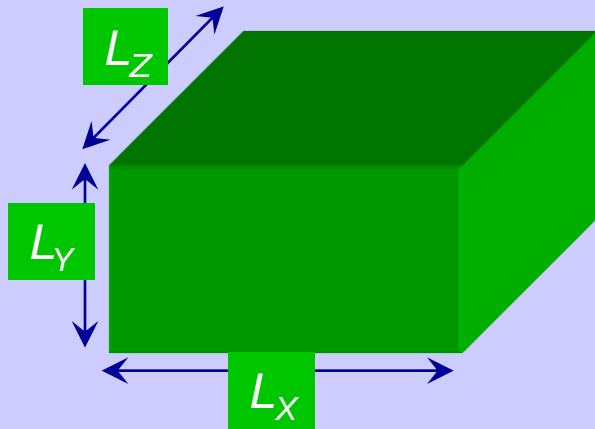
Semiconductor laser



HETEROSTRUCTURES
Heteroepitaxy, strained epitaxy, self-assembly
➔ carrier confinement
➔ low-dimensional systems



Why nano ?



Move of electron in periodic field of lattice
Schrodinger equation

$$\left[\frac{-\hbar^2}{2m_0} \nabla^2 + U(\mathbf{r}) \right] \psi(\mathbf{r}) = E \psi(\mathbf{r})$$

$$\psi(\mathbf{r}) = u(\mathbf{r}) e^{i\mathbf{k} \cdot \mathbf{r}}$$

**Quantum effects
for electron in Si:
 $\lambda \sim 3 \text{ nm}$**

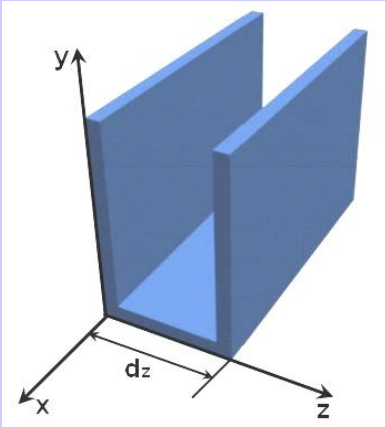
**Geizenberg
equation**

de Broglie wavelength (λ) – quantum phenomena

$$\lambda \approx L_i$$

$$\lambda = \frac{h}{p} = \frac{h}{m_e^* v} \quad m_e^* \sim 0.2m_0$$

Quantum confined effect



$$V(z) = \begin{cases} 0, & 0 \leq z \leq d_z \\ \infty, & \text{autrement} \end{cases}$$

Quantum well

Quantum wire

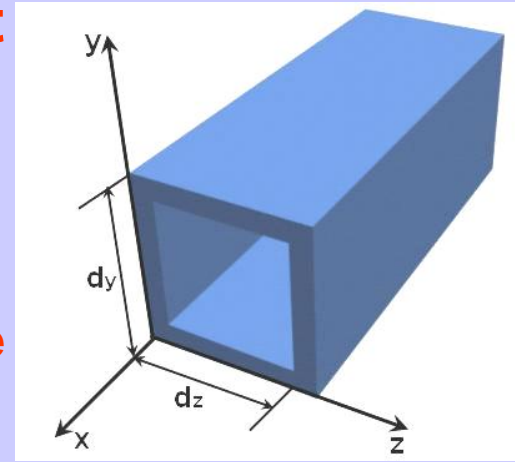


Figure 1. 1 Modèle d'un puits quantique infini : l'électron est confiné dans la direction z , sur une épaisseur de largeur d_z .

Figure 1. 1 Modèle de fil quantique infini : l'électron est confiné dans les directions z et y .

$$E = E_n^\infty + \frac{\hbar^2}{2m^*} (k_x^2 + k_y^2) \quad E_n^\infty = \frac{\hbar^2}{2m^*} \left(\frac{n\pi}{d_z} \right)^2, \quad n \in N$$

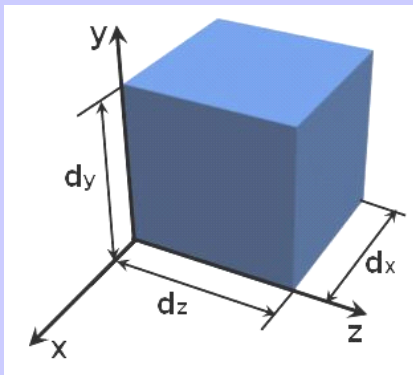


Figure 1. 1 Modèle de boîte rectangulaire : l'électron est confiné dans trois directions.

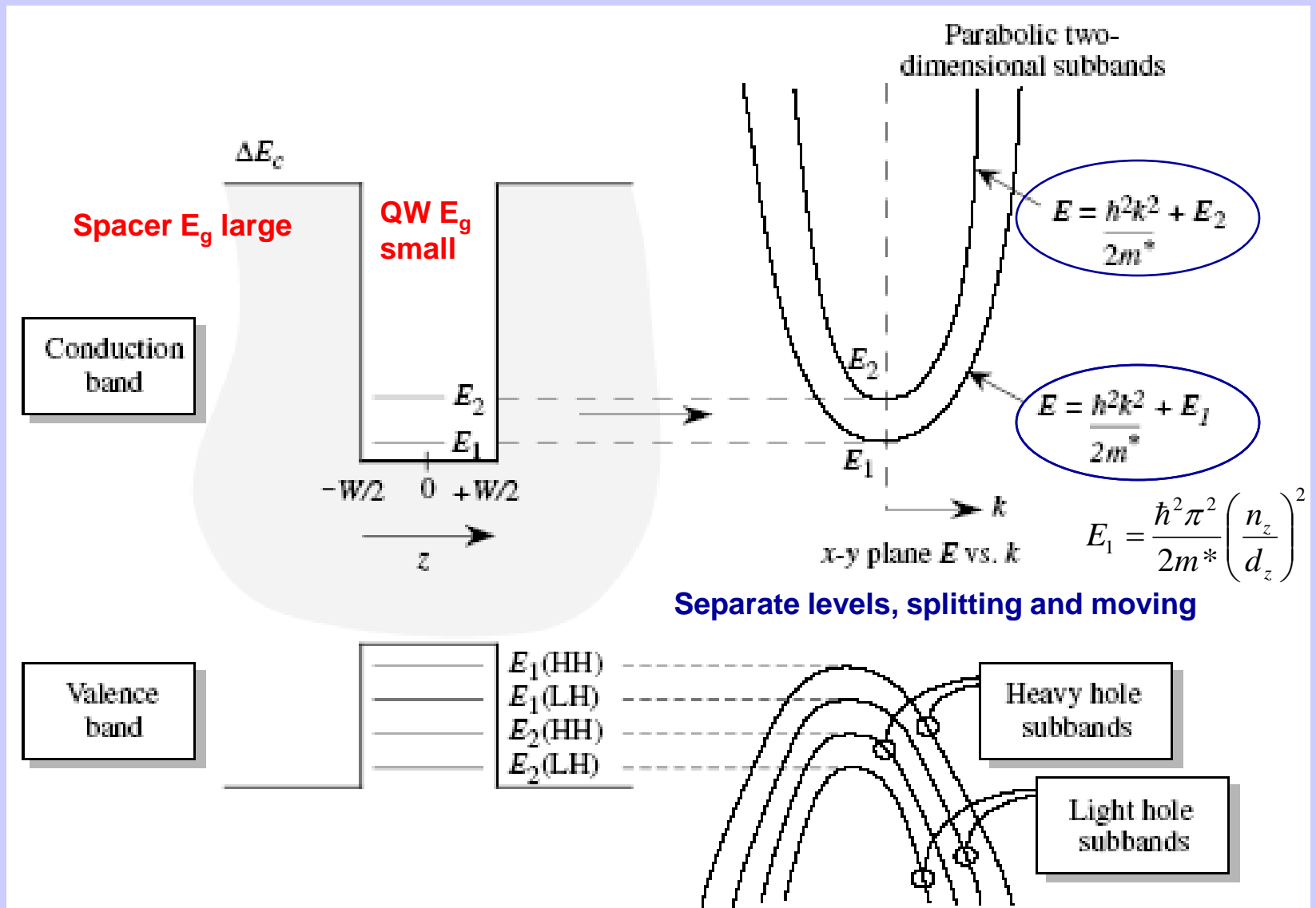
$$E = \frac{\hbar^2 \pi^2}{2m^*} \left[\left(\frac{n_y}{d_y} \right)^2 + \left(\frac{n_z}{d_z} \right)^2 \right] + \frac{\hbar^2 k_x^2}{2m^*}$$

$$E = \frac{\hbar^2 \pi^2}{2m^*} \left[\left(\frac{n_x}{d_x} \right)^2 + \left(\frac{n_y}{d_y} \right)^2 + \left(\frac{n_z}{d_z} \right)^2 \right]$$

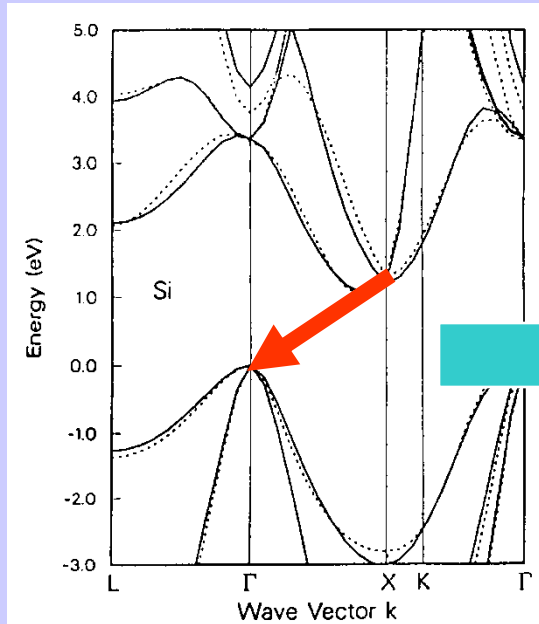
Quantum dot

Electronic spectra – series of levels like in atom !

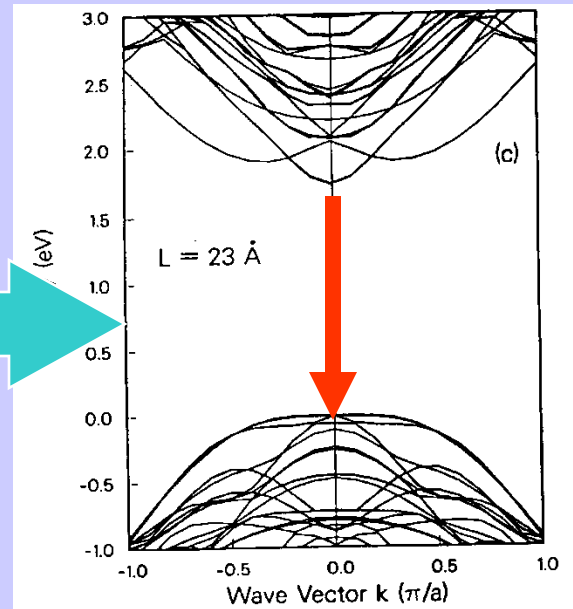
Quantum well



Band structure of nano-Si: two possibilities



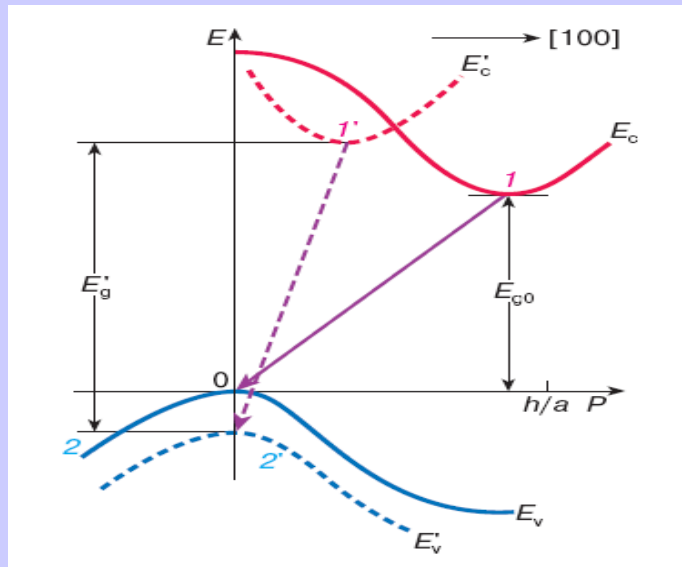
Band structure of bulk Si



Si quantum wires , $L = 2.3 \text{ nm}$

Si Qwires:
Indirect- direct band
gap transformation,
 E_g increases

Si Qdot:
Indirect band gap,
 E_g increases,
Electron-wall collision



$$E_c - E_v = h\nu$$

$$\Delta \hbar k \gg \frac{\hbar \omega}{c}$$

$$\Delta \hbar k = \frac{\hbar \omega}{c} + mv_{\text{collision}}$$

**law of conservation of
energy**

**law of conservation of impulse in
indirect semiconductor
(need phonon mv_{ph})
and QW (collision with well)**

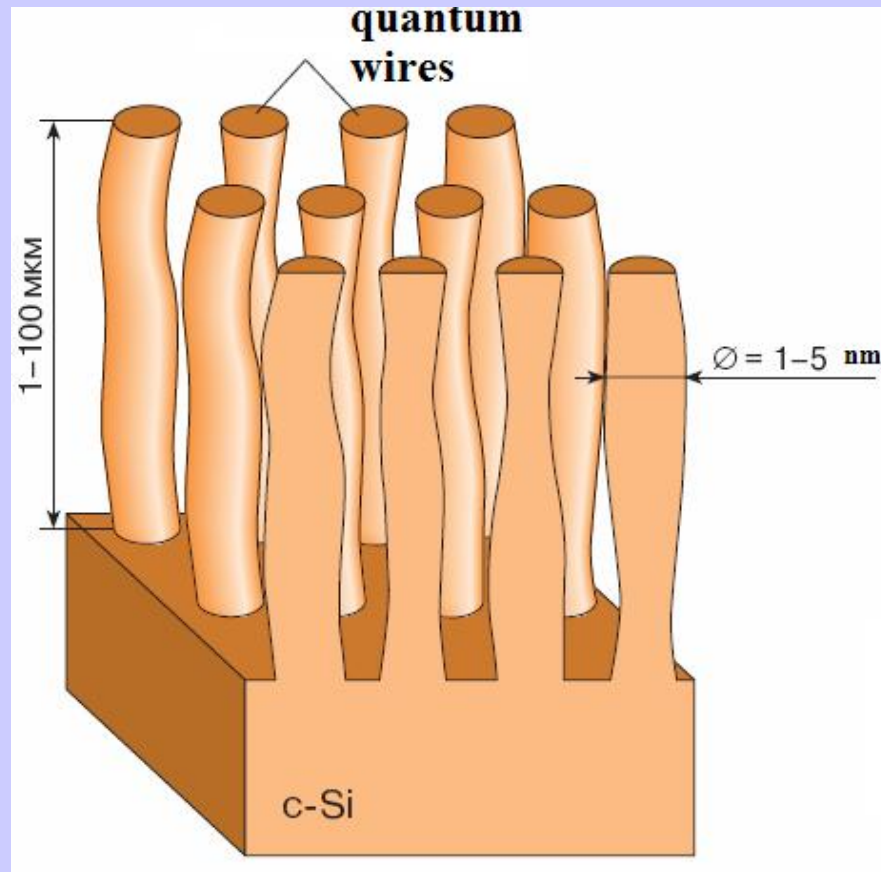
Nomenclature of pores

(International Union of Pure and Applied Chemistry, IUPAC) standard

Micropore, with pore diameters and pore distances ≤ 2 nm.

Mesopores, with geometries in the 2-50 nm region.

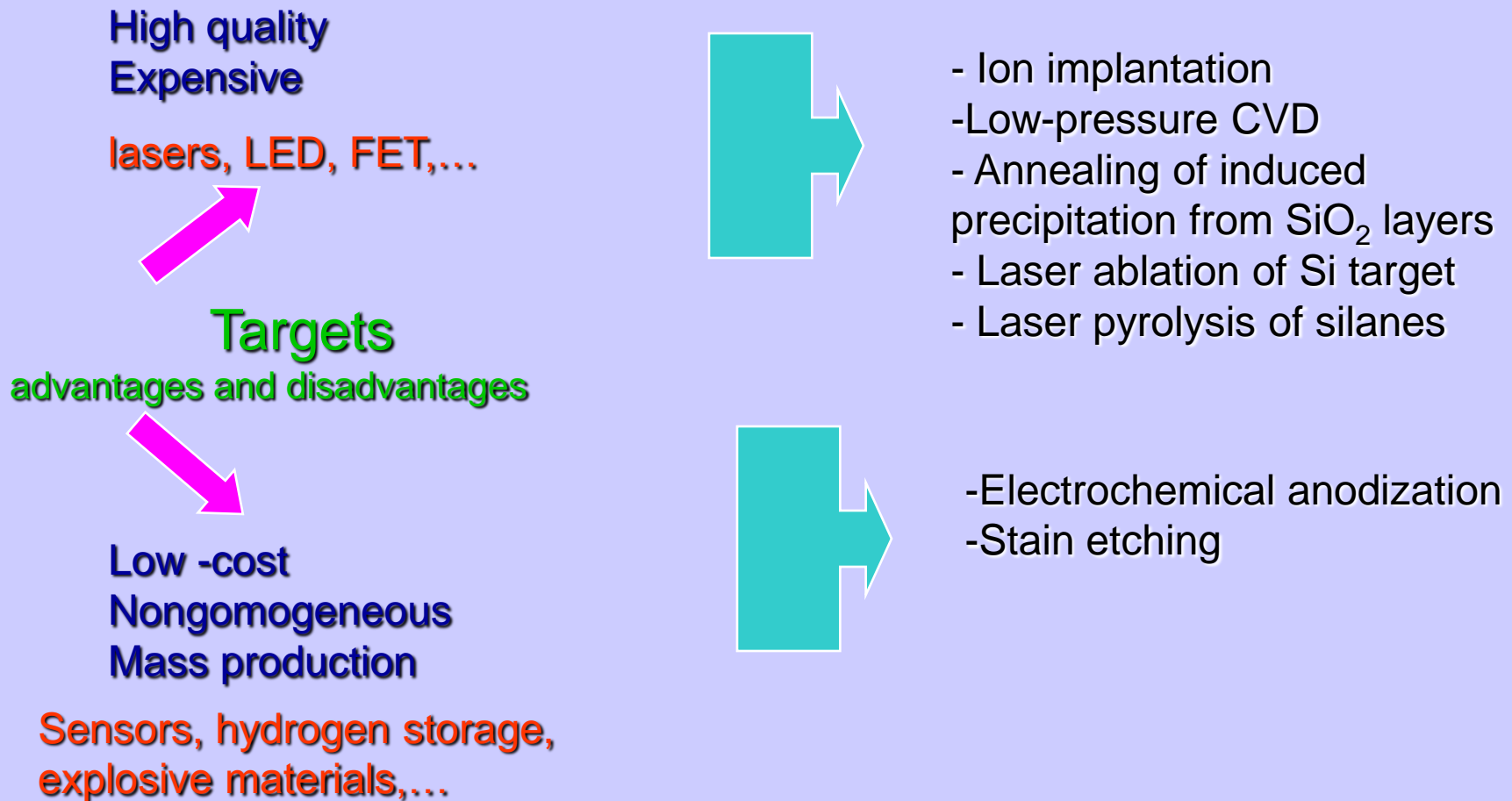
Macropores, with geometries in the >50 nm region.



Technology of nano- and Porous Si

Criteria for choice of pore formation methods

Preparation Methods:



High Si nanotechnologies

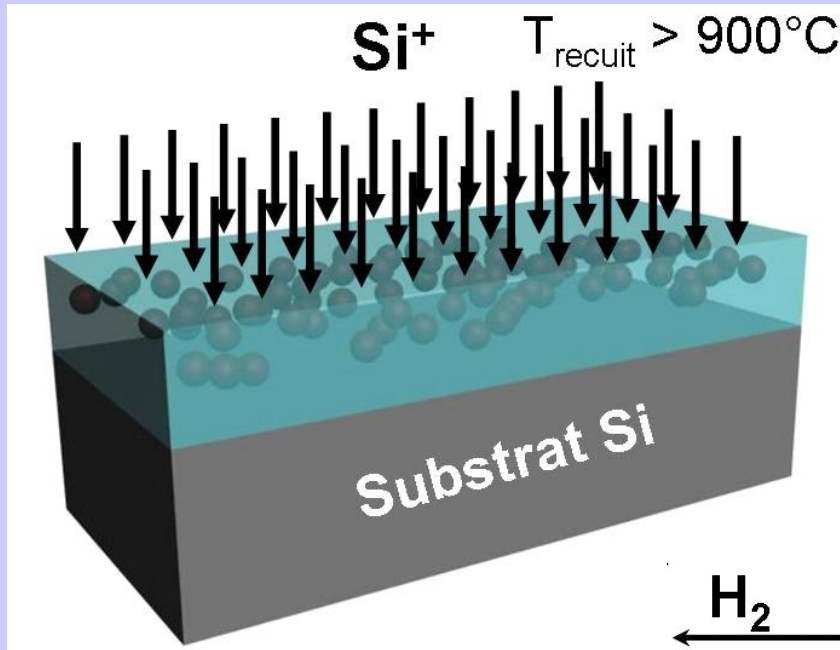


Schéma du processus de fabrication de nanostructures de Si par implantation ionique

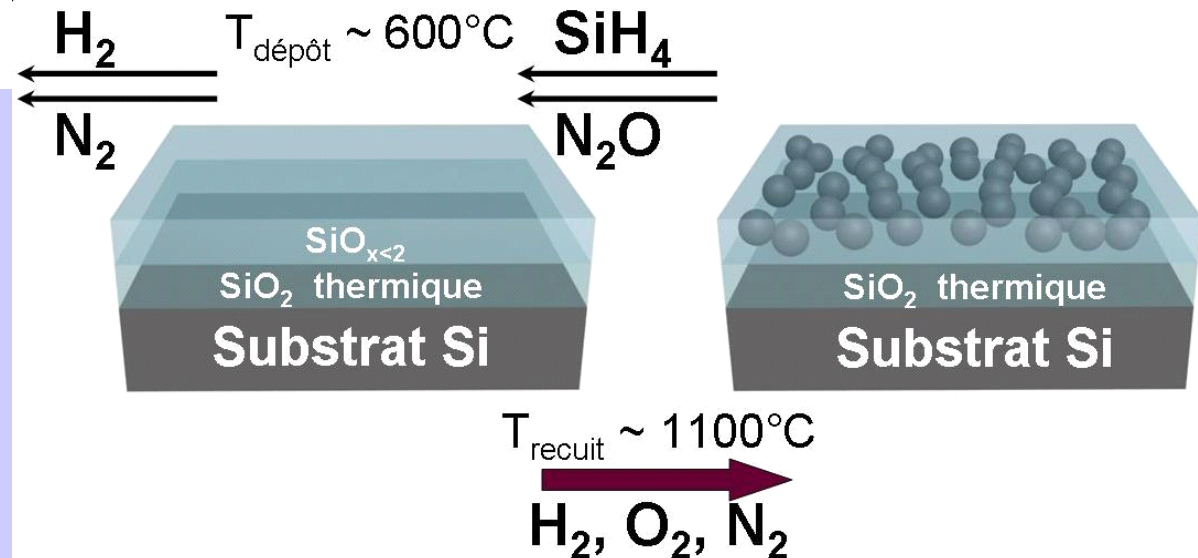
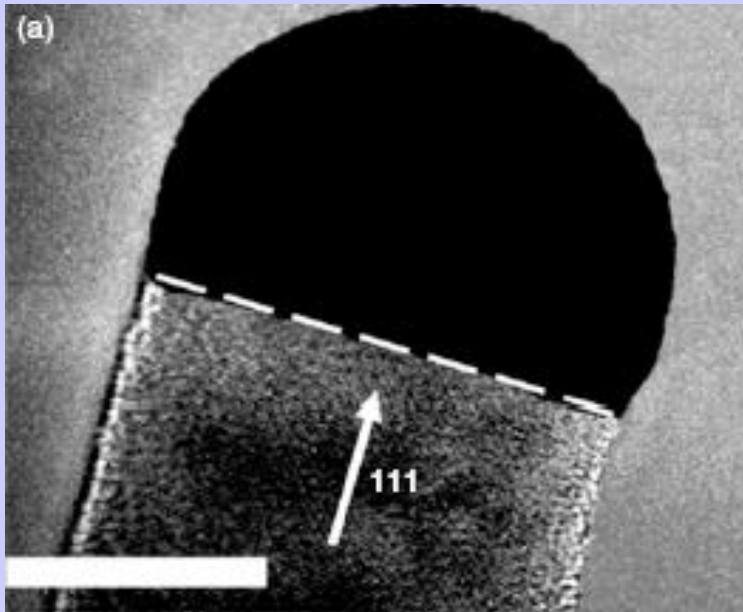
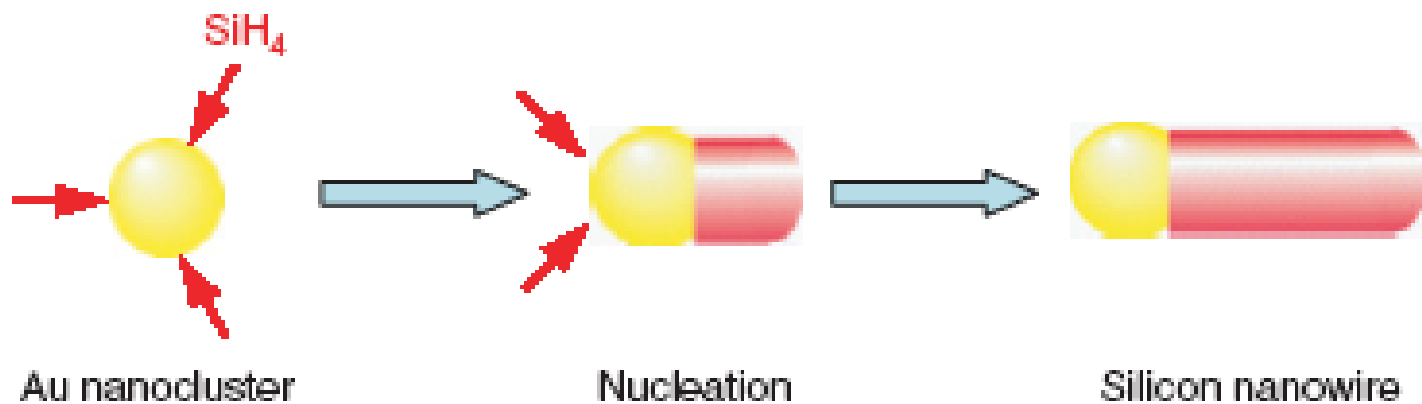


Schéma du processus de fabrication de nanostructures de Si par LPCVD : précipitation dans une couche d'oxyde.

A nanocluster catalysed SiNW growth by CVD



scale bar 20 nm



High nano Si technologies

Schéma de principe de la pulvérisation cathodique.

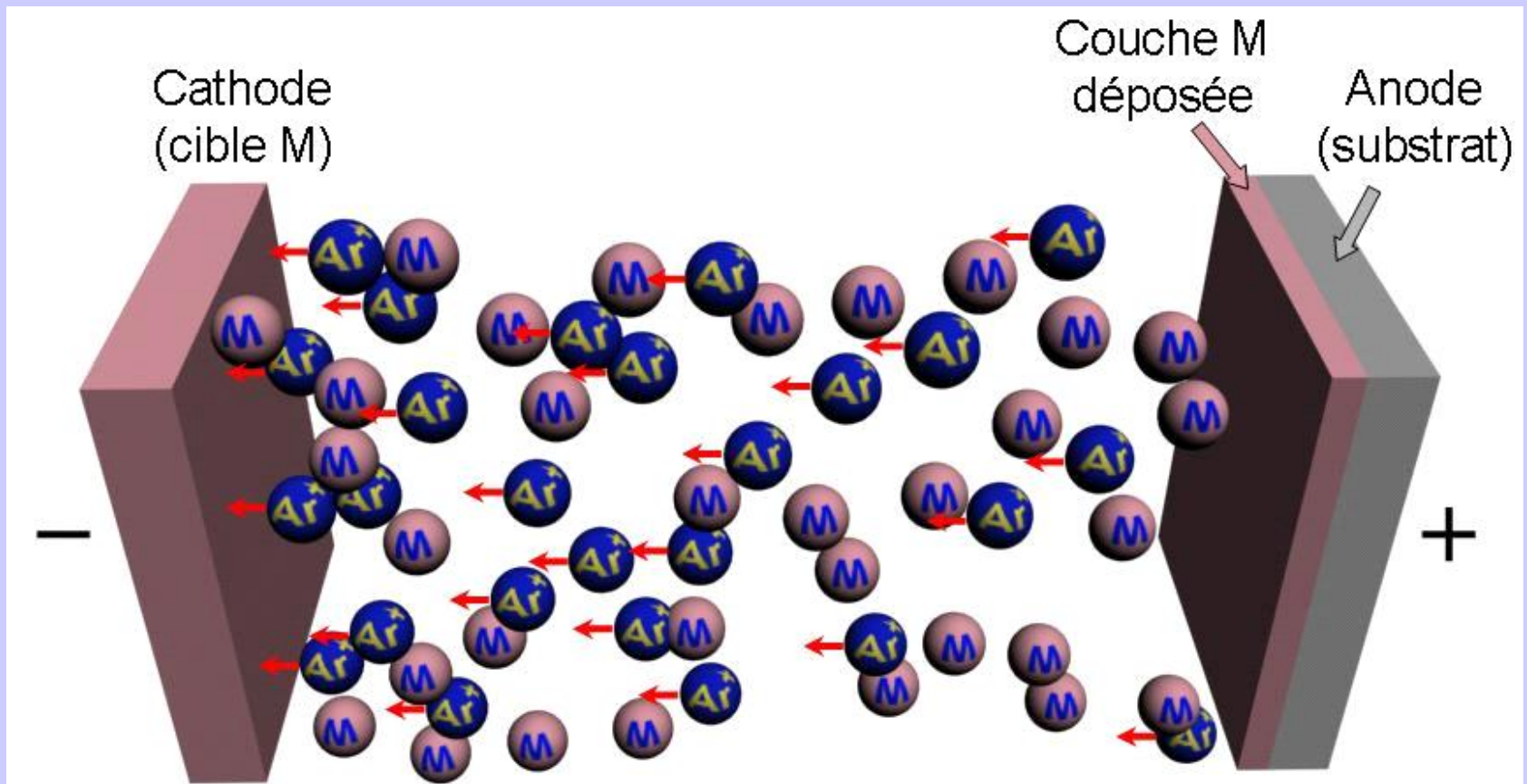


Schéma de principe de l'ablation laser.

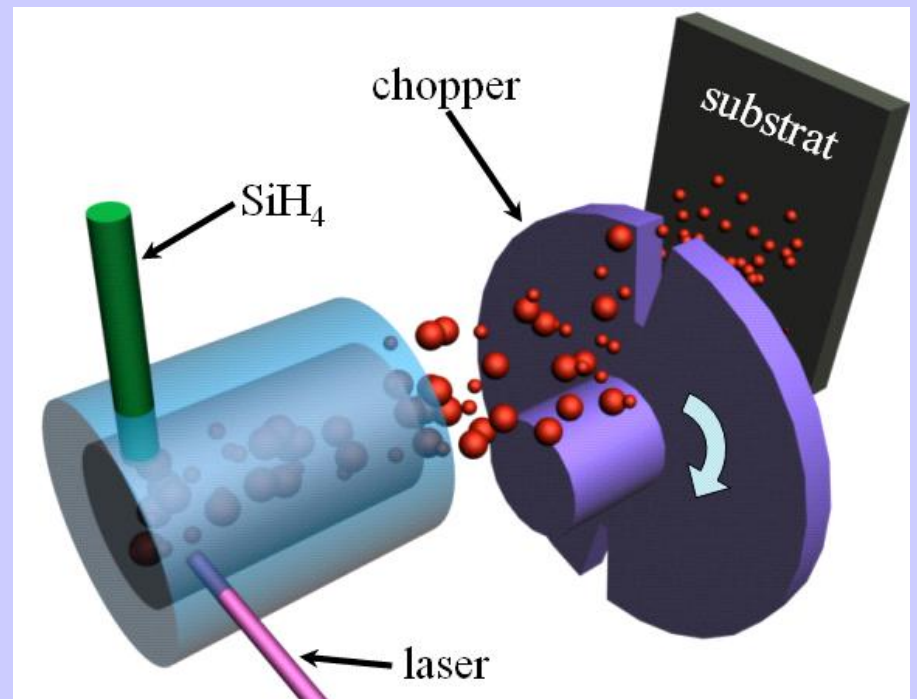
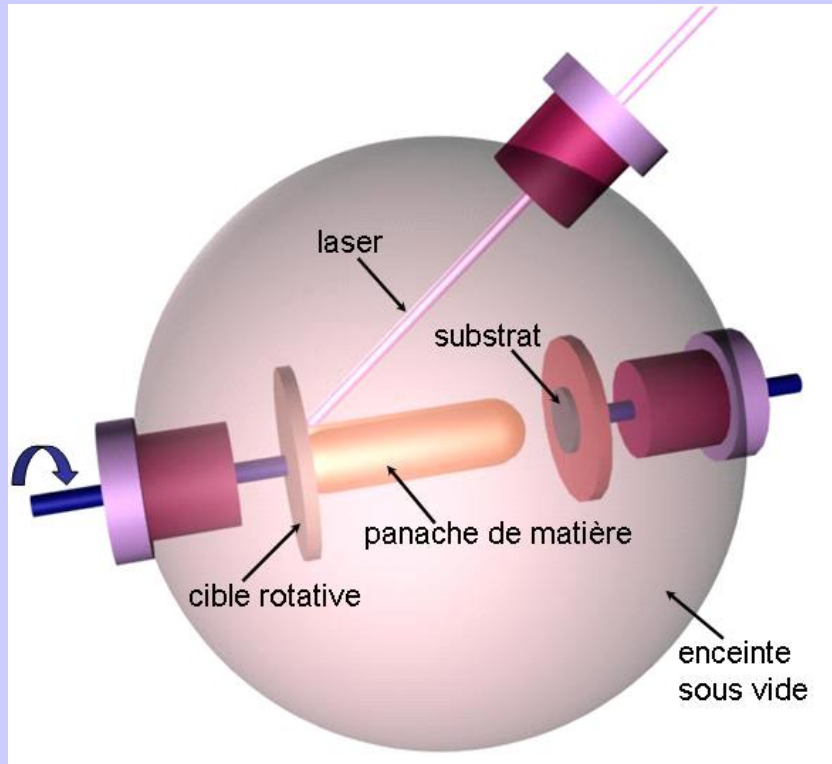


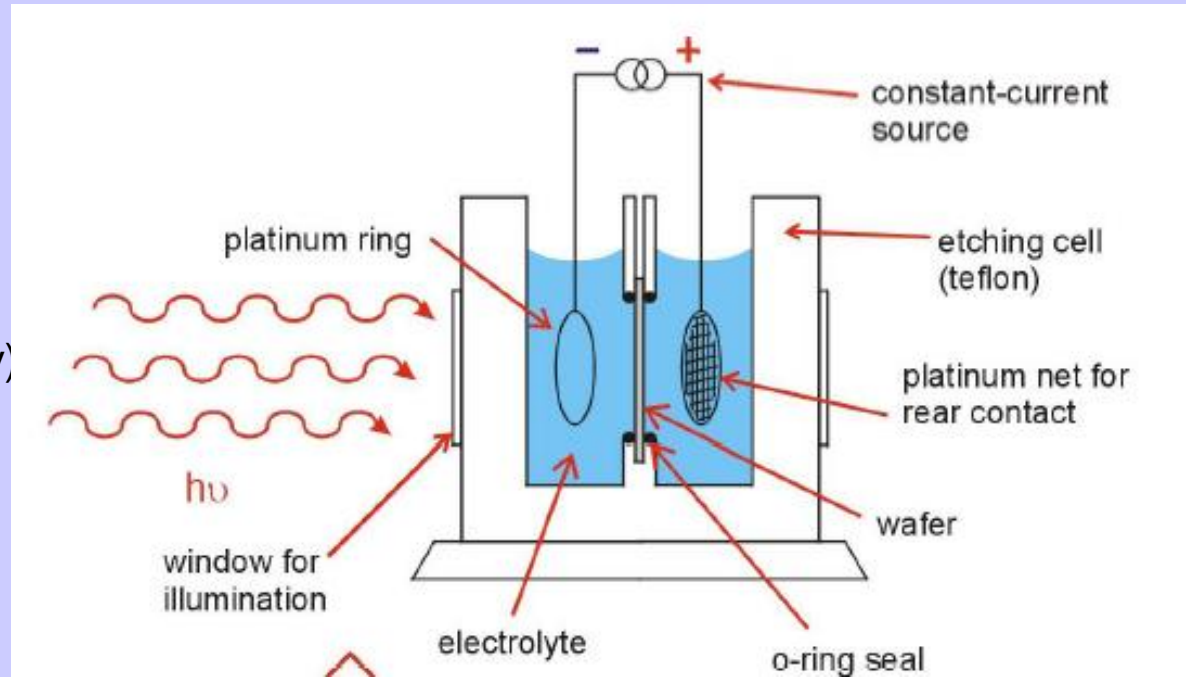
Schéma de principe du pyrolyse laser.

Electrochemical formation

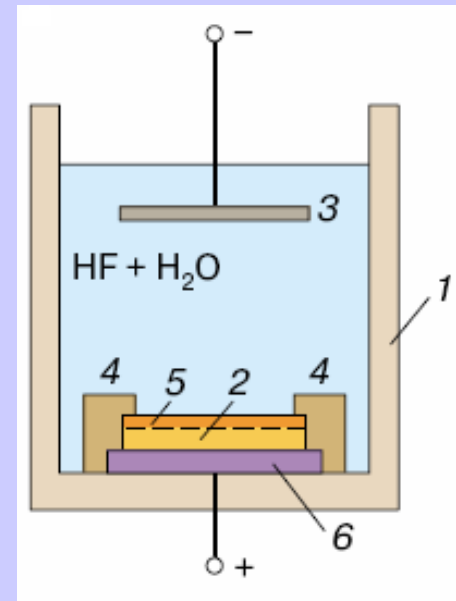
Key parameters:

Si surface- hydrophobic!

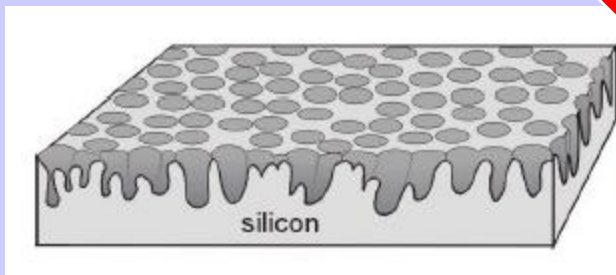
- Electrolyte type ($\text{C}_2\text{H}_5\text{OH}$ for wettability, org. for homogeneity)
- HF concentration (<50%)
- Doping level (n, n+, p, p+)
- Illumination state
- Anodical current (constant I mode=control porosity)
- Cell: H_2 bubble remove!



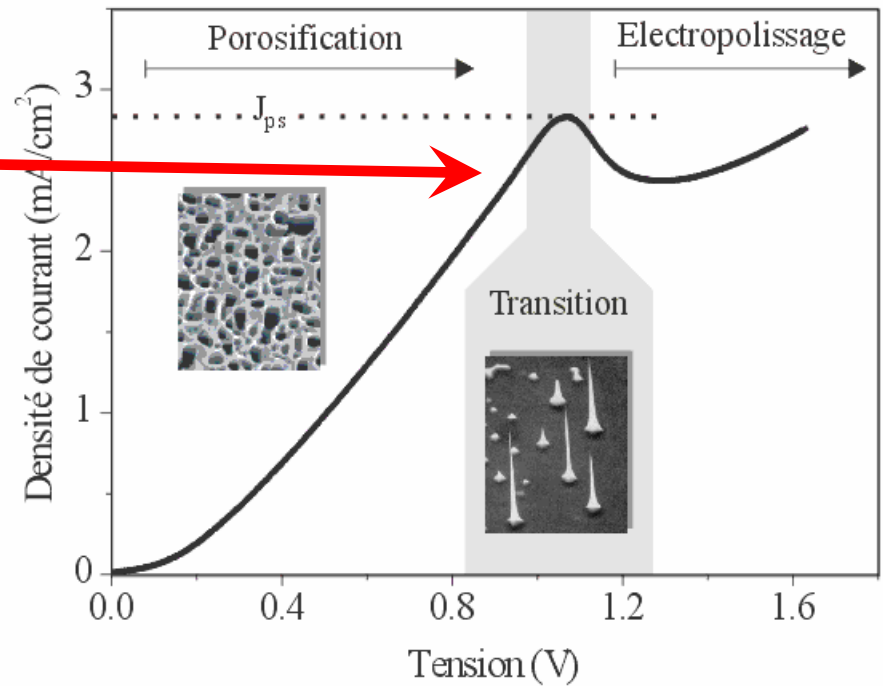
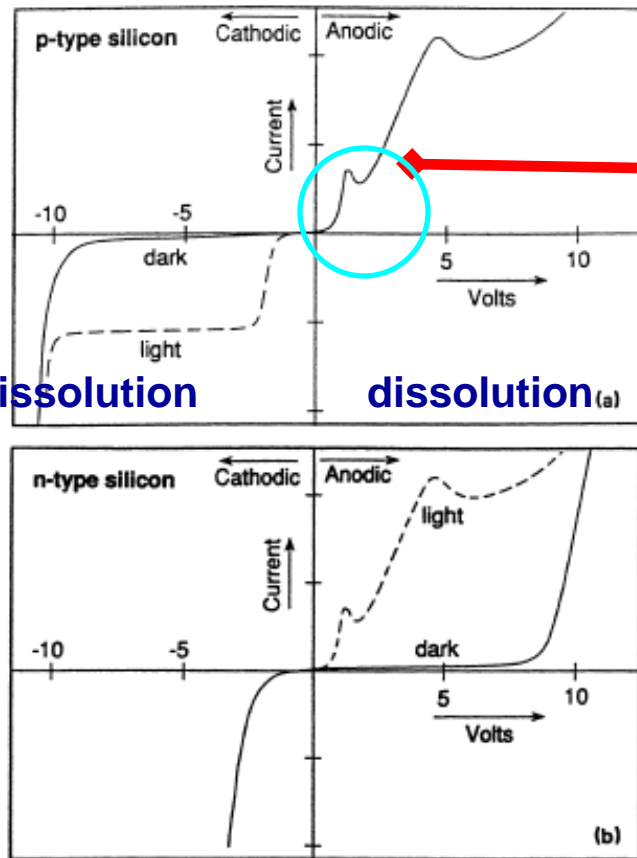
Double tank cell



single tank cells



Electrochemical formation

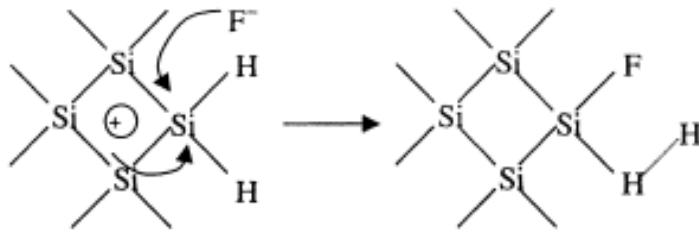


(Schottky diode behavior)
Change from electronic
to ionic current due to
specific redox reaction on Si surface

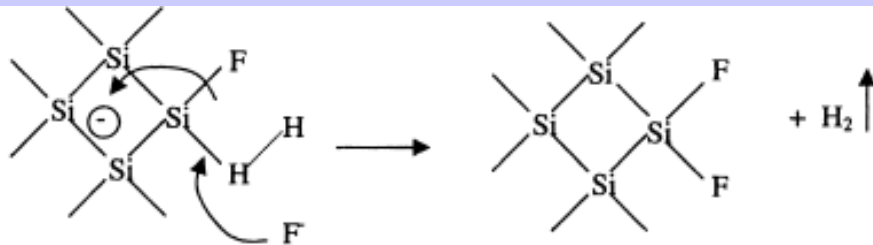
$$J = J_0 \left[e^{\frac{eV}{nkT}} - 1 \right]$$

Dissolution chemistry:

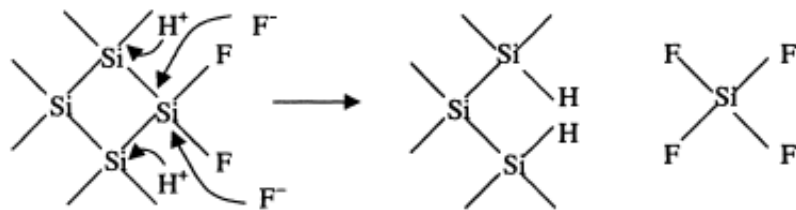




Hole injection and attack on a Si-H bond by a fluoride ion



Second attack by a fluoride ion with hydrogen evolution and electron injection into the substrate



HF attack to the Si-Si backbonds. The remaining Si surface atoms are bonded to the H atoms and a silicon tetrafluoride molecule is produced

Mechanism of Si dissolutions

To dissolve 1 Si atom:
 $2h^+ + H_2O$.

One H_2 molecule forms
 on the surface

Process of replacing:
 $Si-H \rightarrow Si-OH \rightarrow Si-F$ &
 settling-out of SiF_4

**Silicon dissolution scheme, Lehmann
 and Gosele**

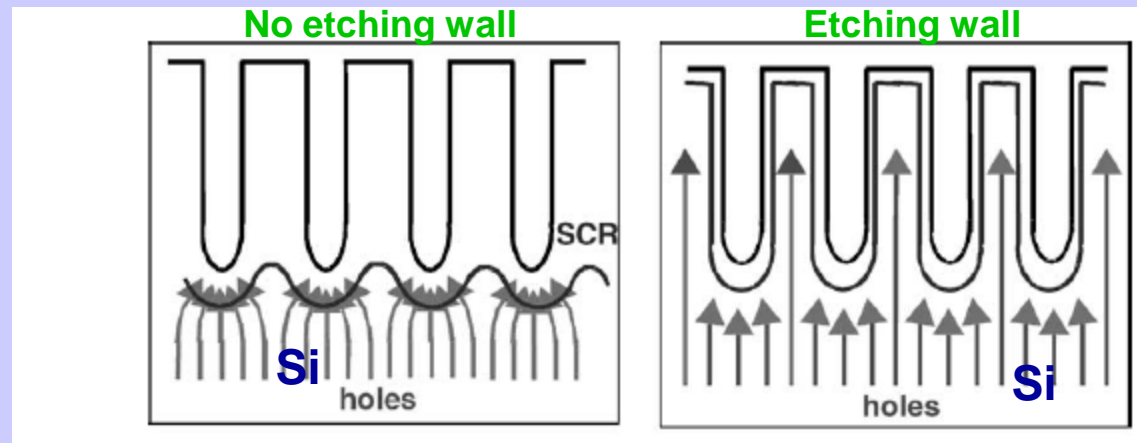
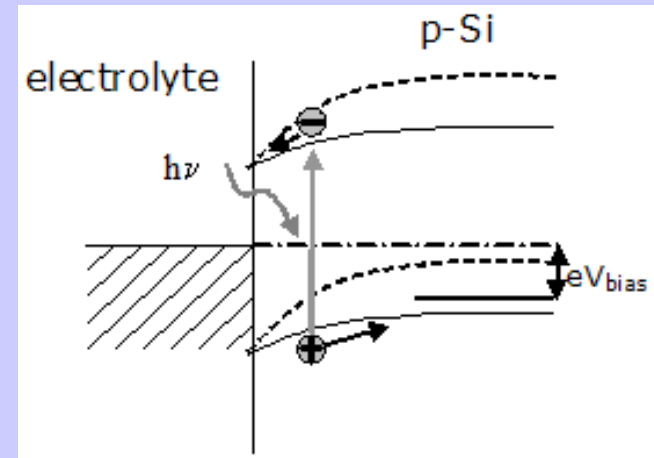


The silicon tetrafluoride reacts with two HF molecules to give H_2SiF_6 and then ionizes.

Why pore formation?

- There are initial roughness or pores
- A surface region depleted in mobile carriers at Si/electrolyte interface (Schottky contact).
- The thickness of depleted region depends on doping level.
- The size of pore is related both to the depletion layer and mechanism of charge transfer (breakdown, tunneling, overcome the barrier PS-Si...)

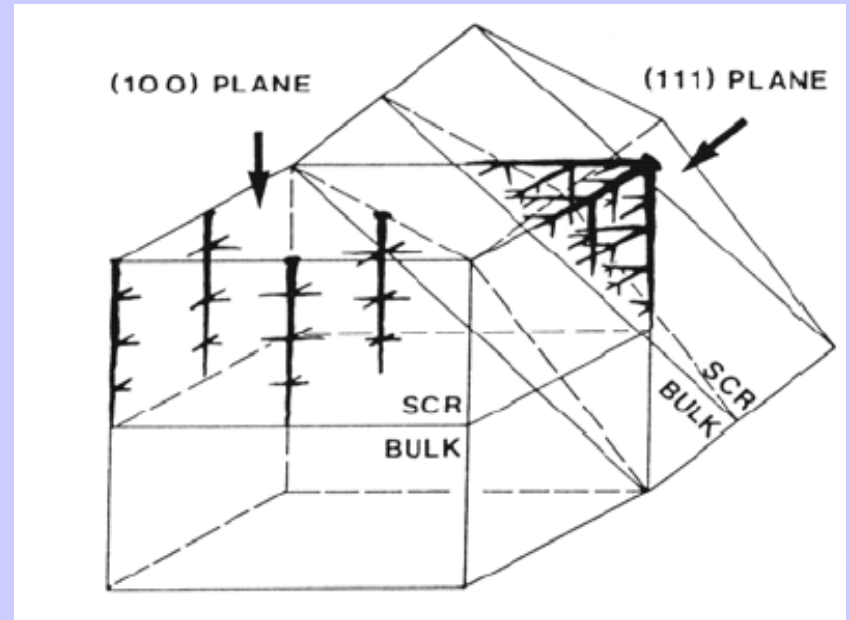
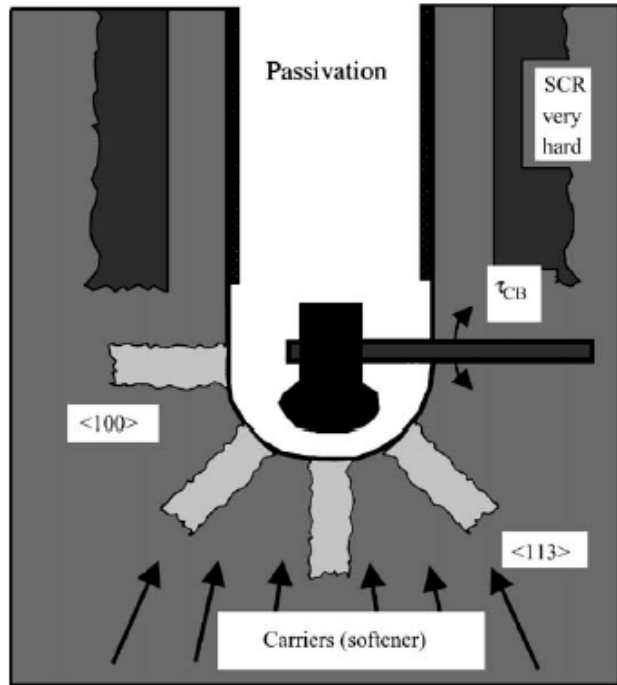
$$x_0 = \sqrt{\frac{2\epsilon\epsilon_0 e \psi_s}{e^2 N_A}}$$



Large SCR and
small SCR

Hammer model of pore formation

Si is always removed in patches corresponding to the domain size of system!

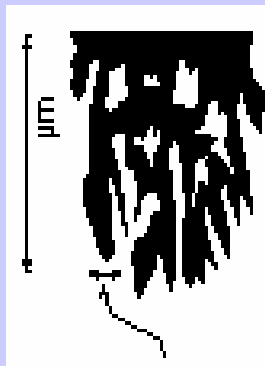


Pore formation region

Nano -porous Si P-type

- « nano -sponge » morphology

- nanocrystallites sizes: **1 - 5 nm**

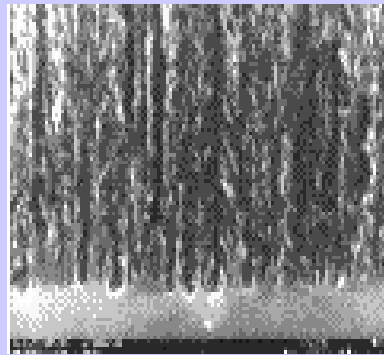


<5 nm

Meso -porous Si P+ -type

- « nano - column » morphology

- column width: **5 - 20 nm**



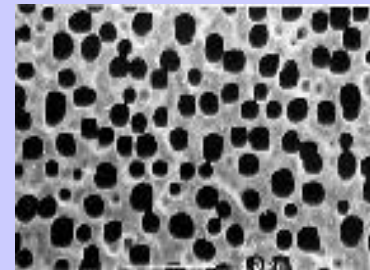
5 nm

Macro -porous Si N-type + light

- « nano -wells » morphology

- inter -well space: **0.1 - 1 μm**

Top view

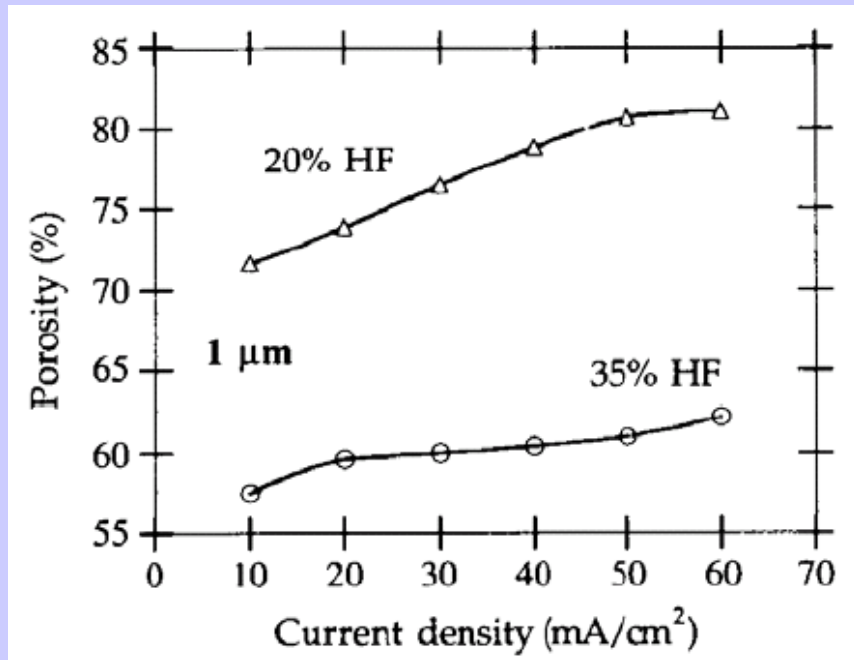


Cross -section

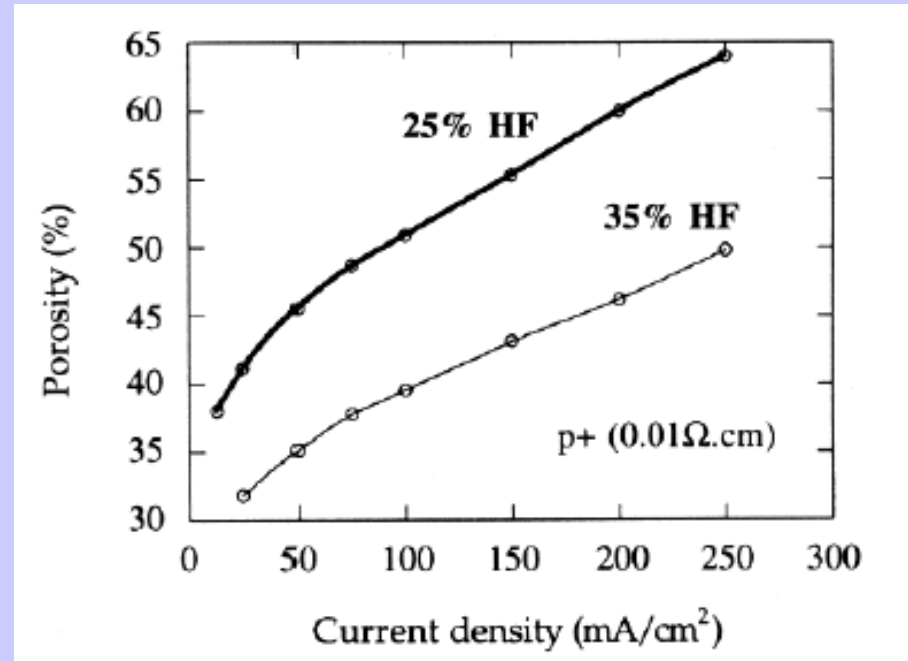


Porosity

Nano-porous Si P-type



Meso-porous Si P+-type

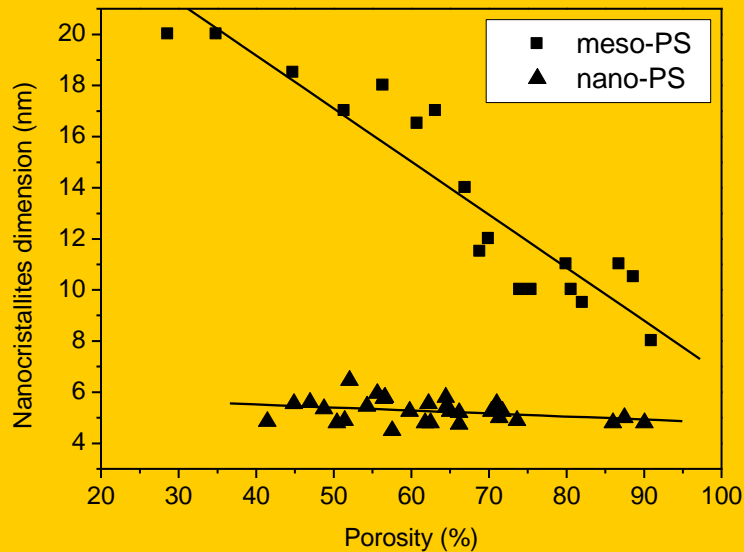


Porosity

$$P = \frac{V_{pore}}{V_{pore} + V_{Si}} = \frac{m_1 - m_2}{m_1 - m_3}$$

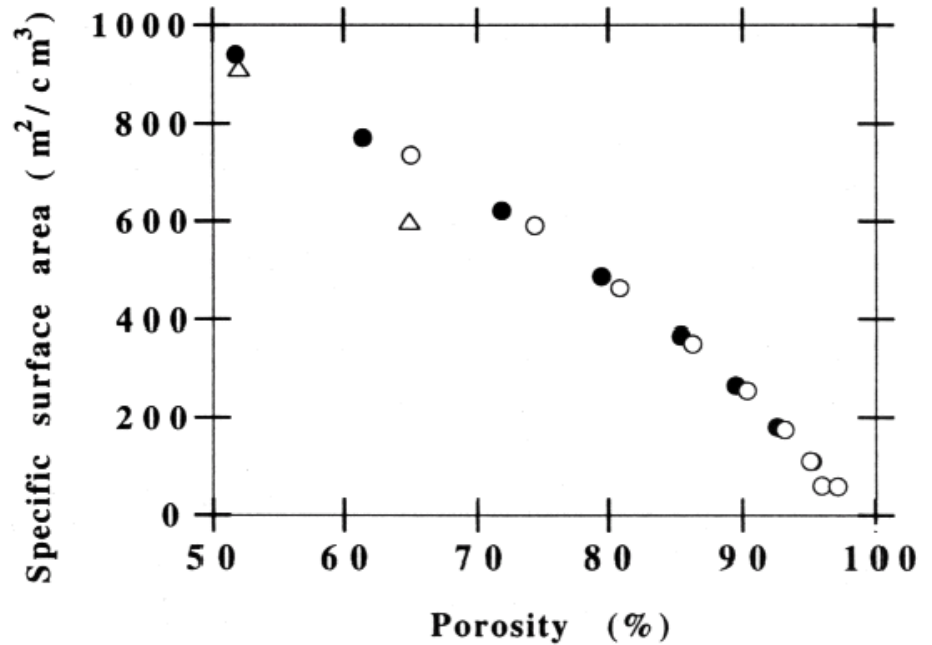
m_1 - weight before anodization, m_2 - after, m_3 - after rapid dissolution of PS in KOH

Porosity, particles dimension, specific surface



Particle dimension vs Porosity

Nano-PS (sponge type)
meso-PS (column type)



Specific surface

Macropores

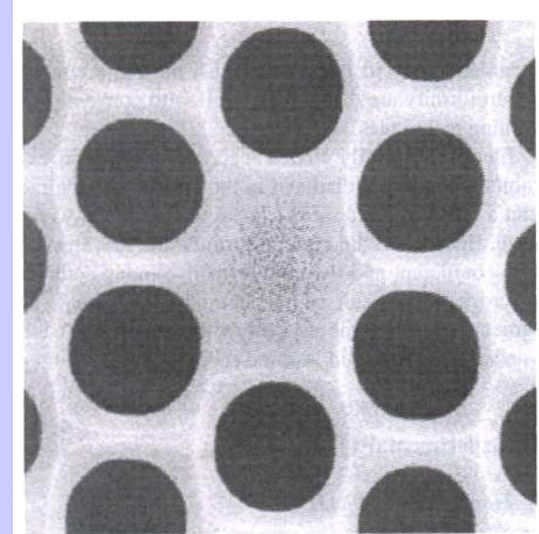
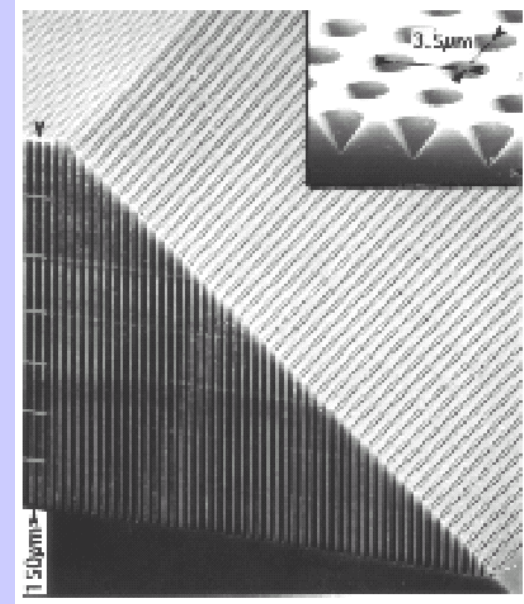
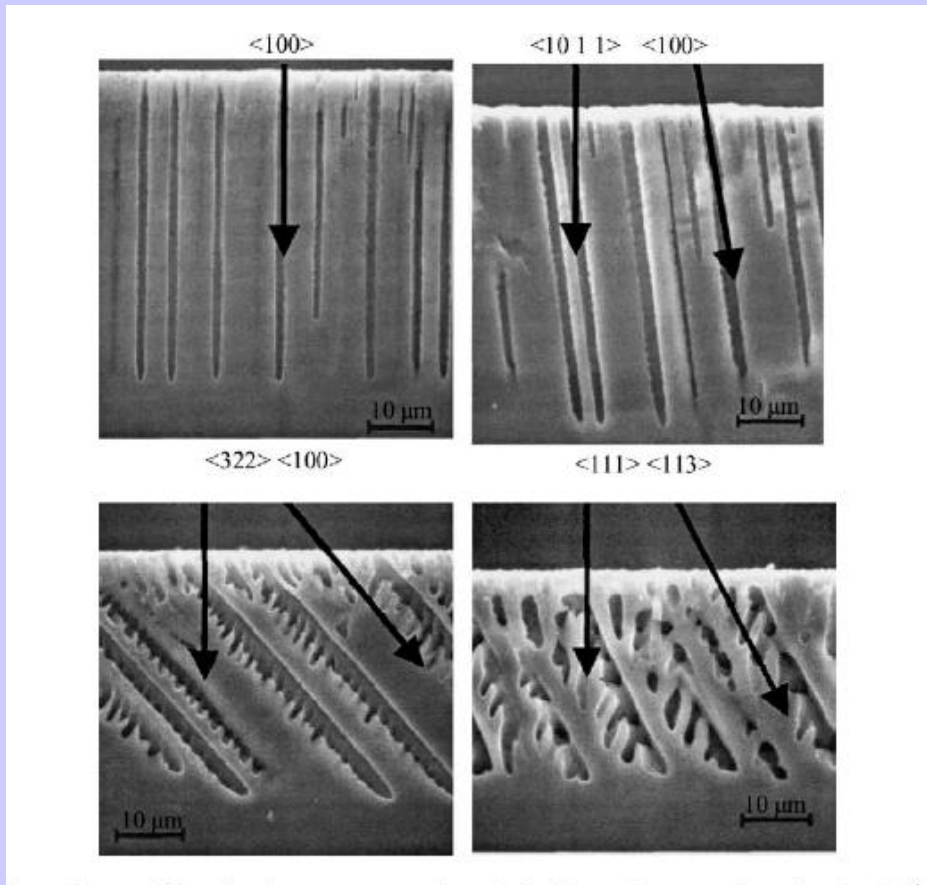
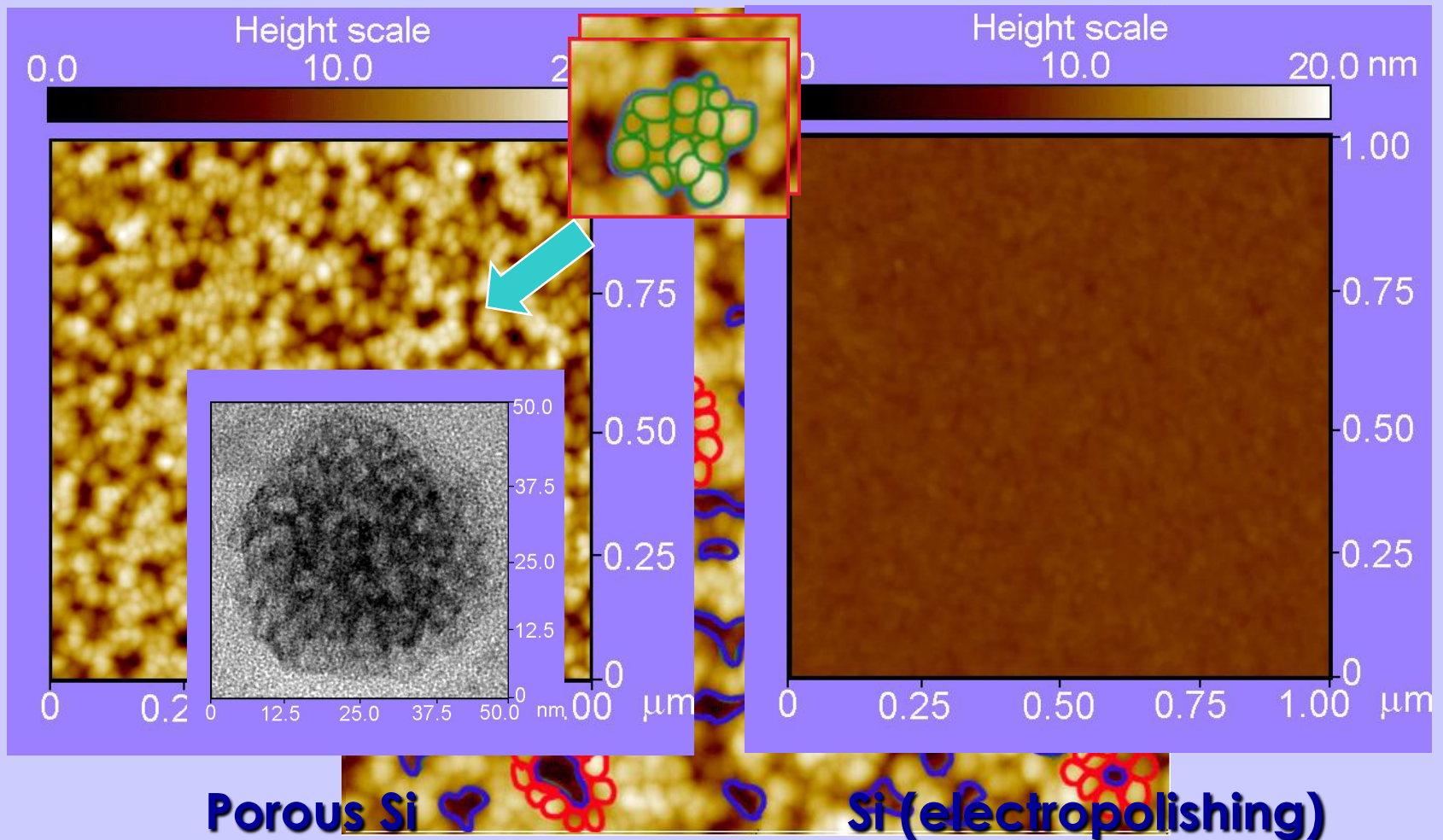
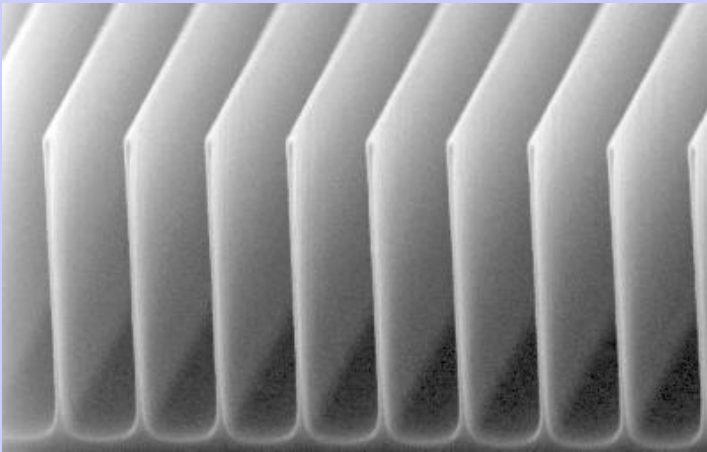


Figure 1. SEM image of the region around a missing etch pit after electrochemical pore growth and subsequent pore widening by oxidation/etching steps. The distance between the pores is $1.5 \mu\text{m}$, pore diameters are $1.15 \mu\text{m}$.

Nano-porous nanostructures

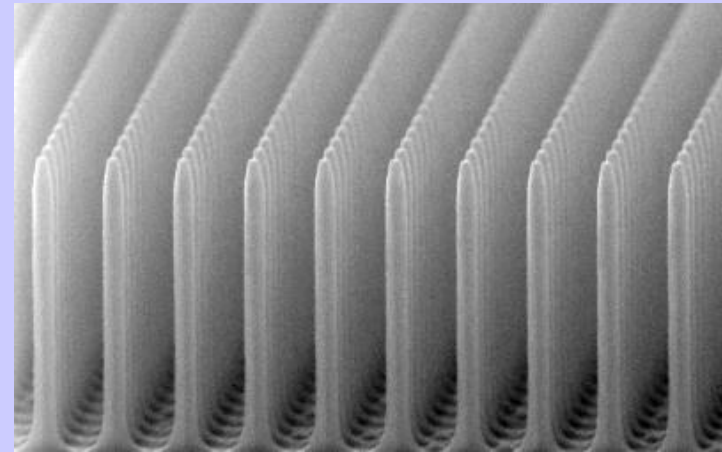


Transient anodization regime



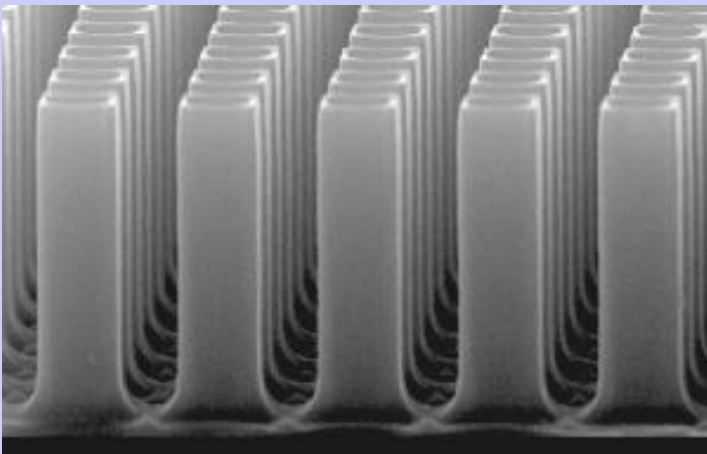
Réseau de Murs

Période 1.6 μm ; Largeur 110 nm ; hauteur 7 μm



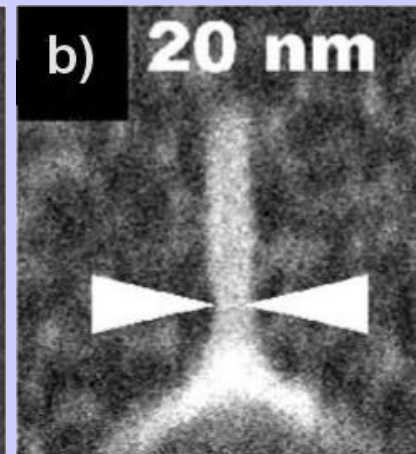
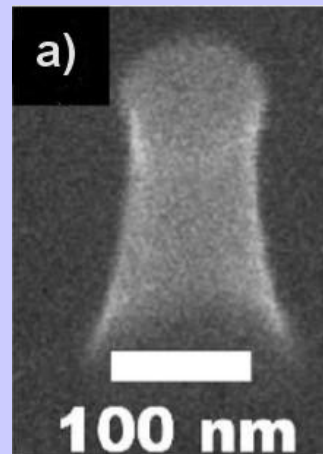
Réseau de Piliers

Période 1.6 μm ; Largeur 450 nm ; hauteur 7 μm



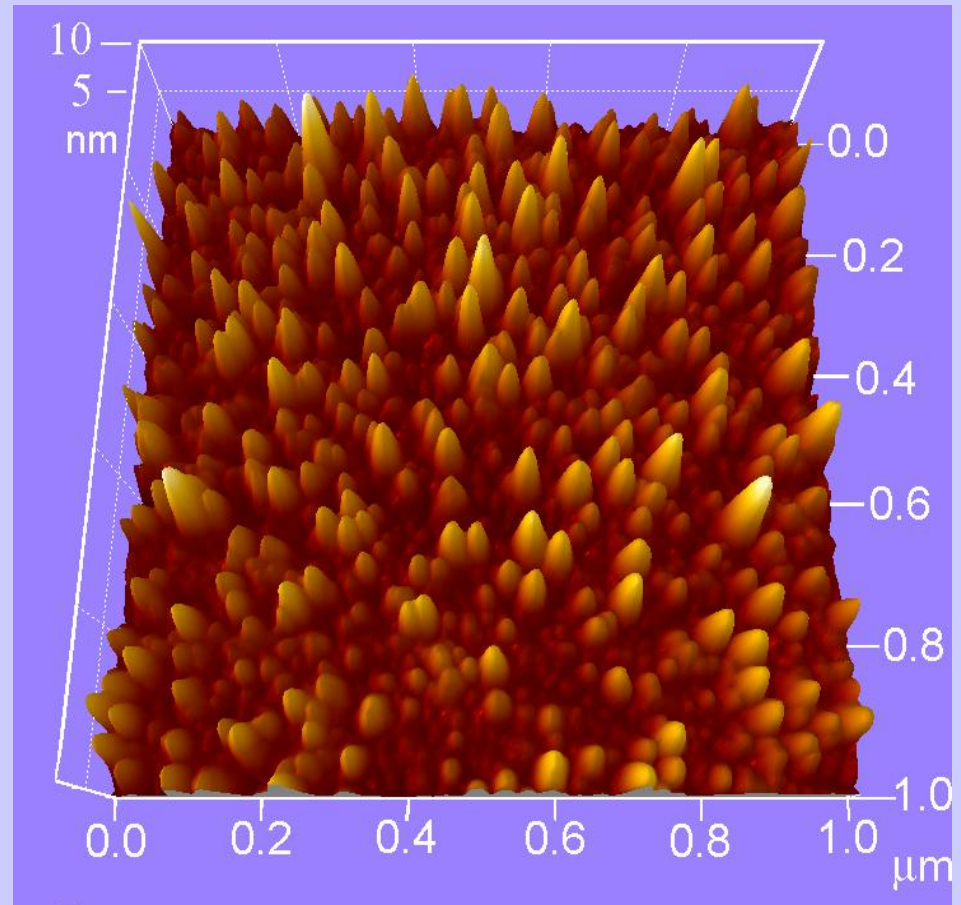
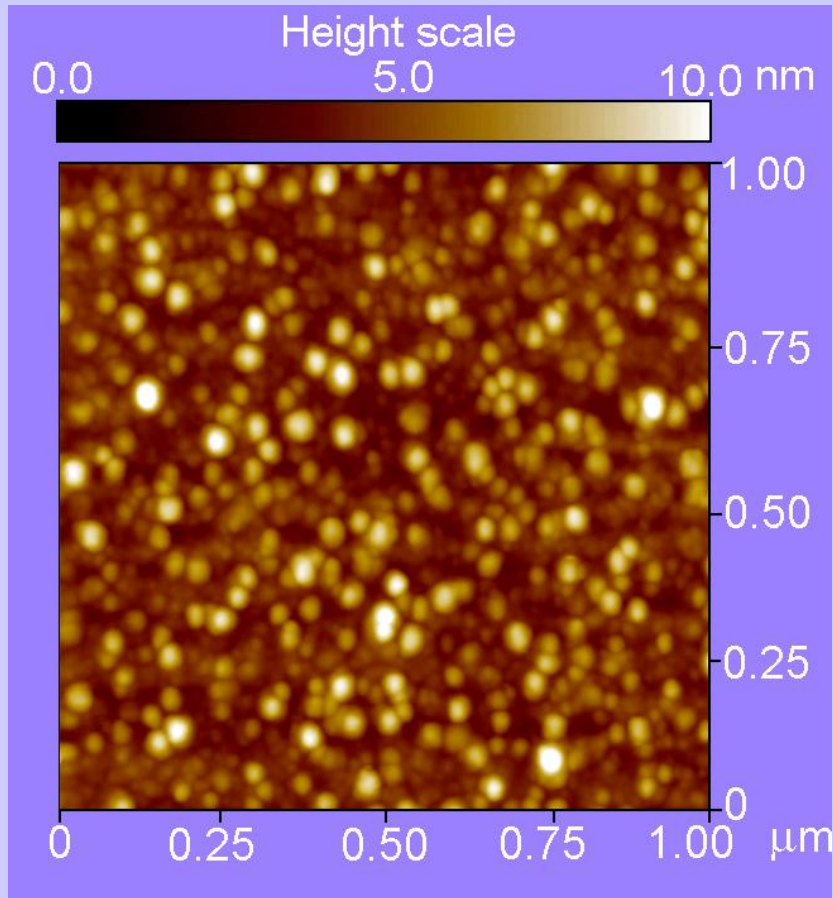
Réseau de Tubes

Période 3.2 μm ; Murs 220 nm ; hauteur 7 μm

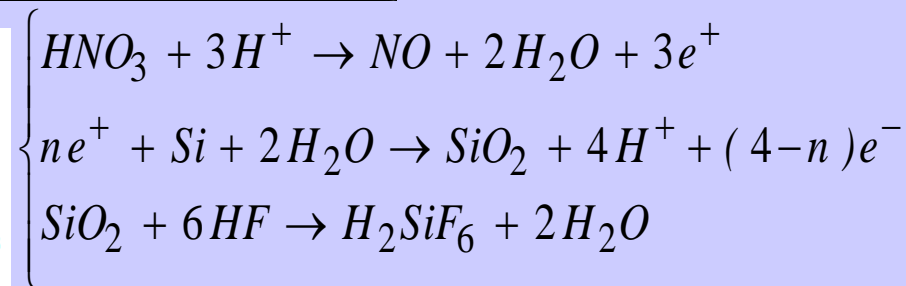
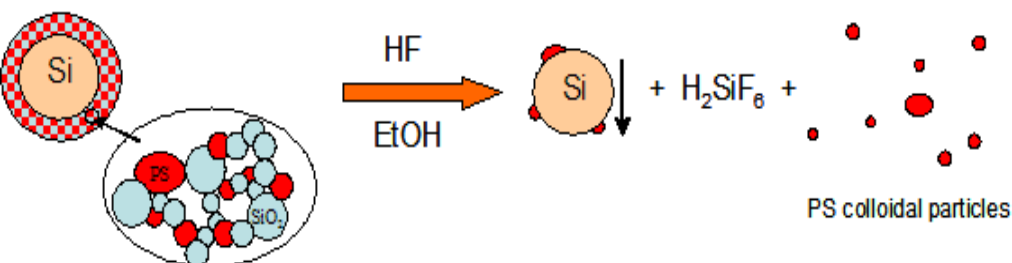
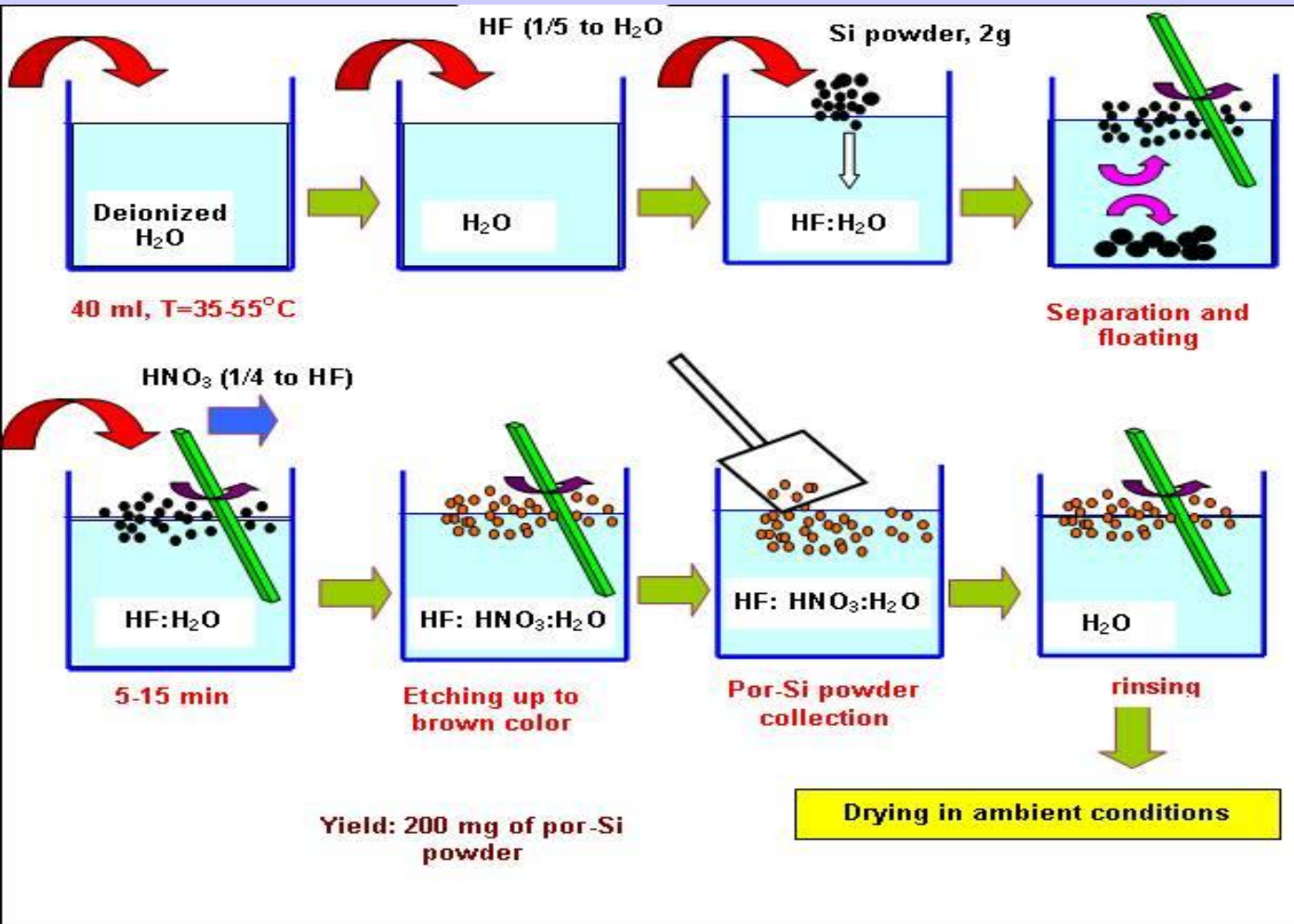


a) Pilier obtenu par gravure plasma puis b) aminci par gravure électrochimique

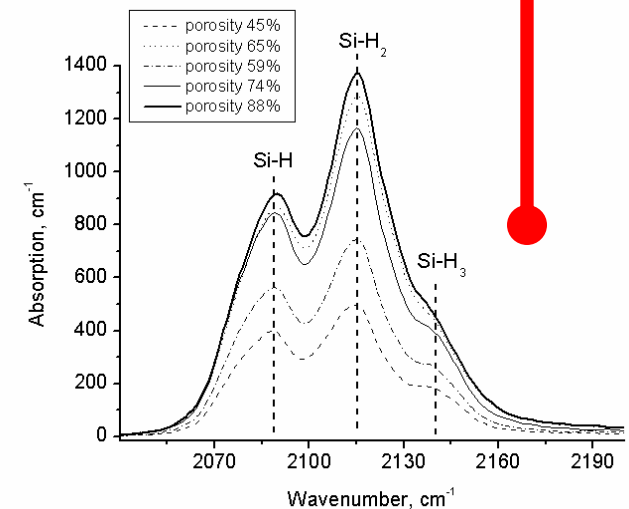
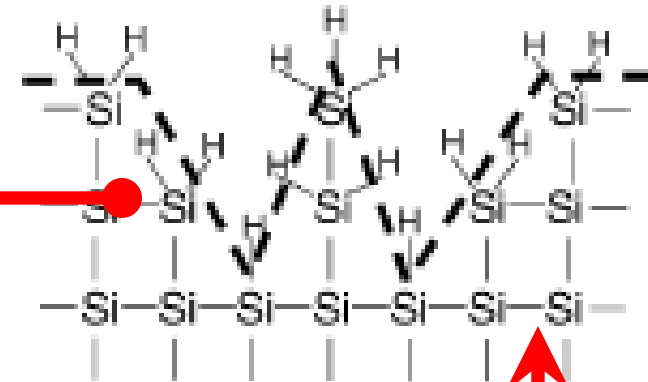
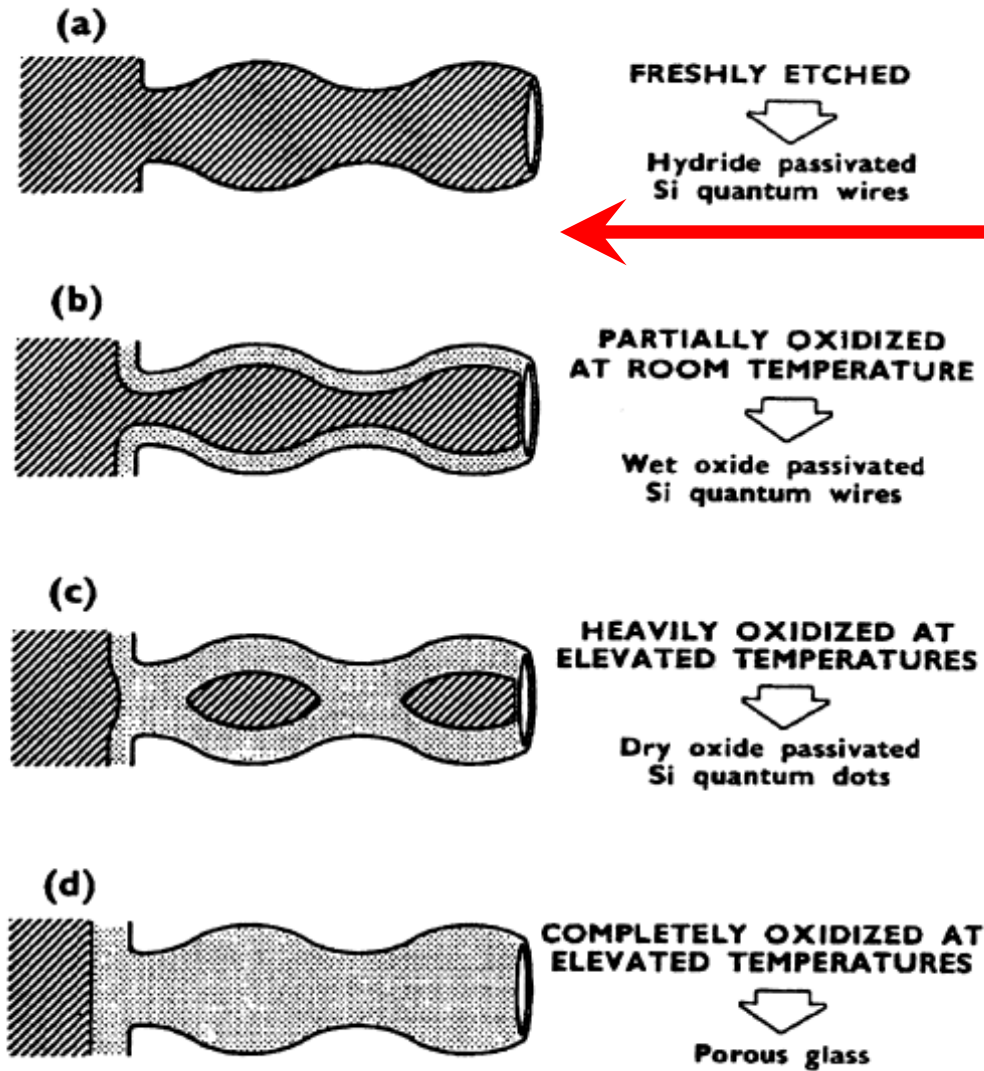
Time-resolved transient anodization regime: nanoparticle formation



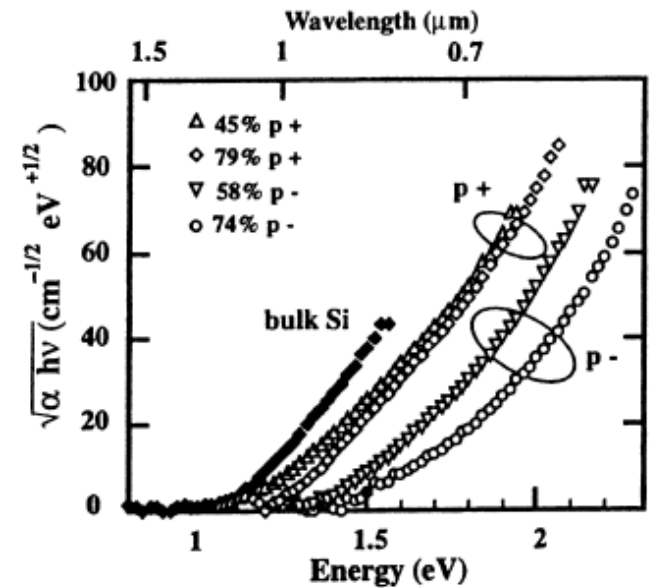
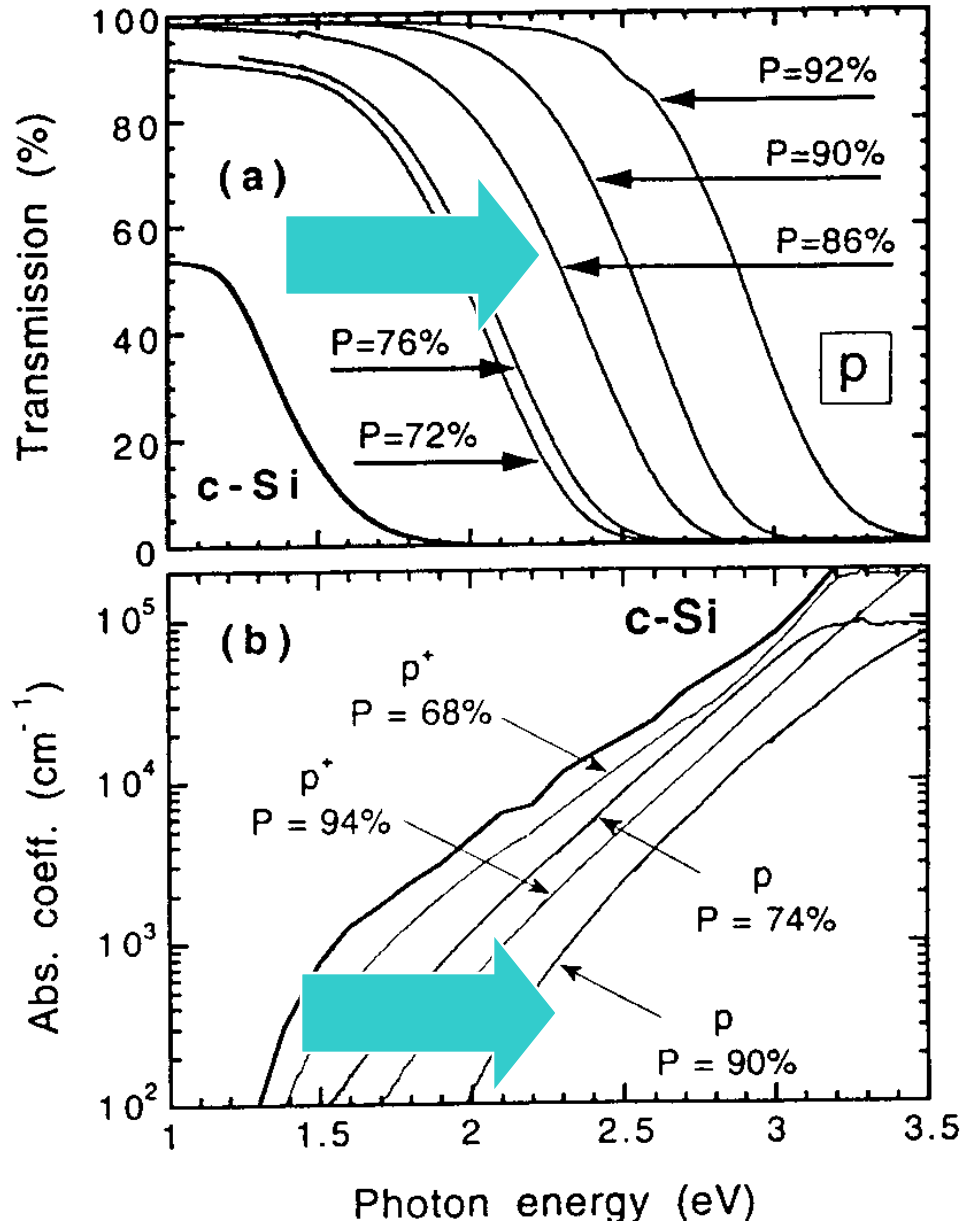
Stain etching of Si powder: method



Idealized schematic steps in the oxidation process of highly PS



Optical properties of nano-porous Si

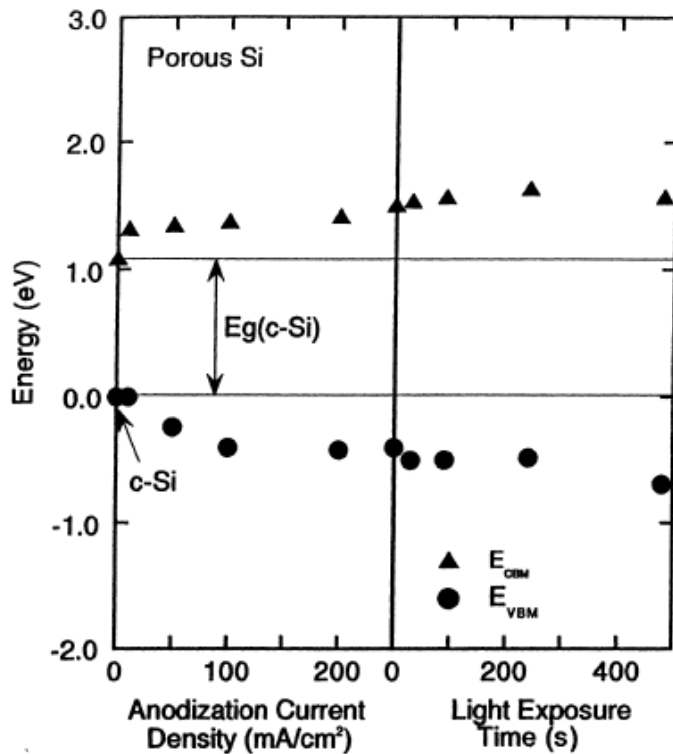


Square root of the absorption coefficient times photon energy vs photon energy

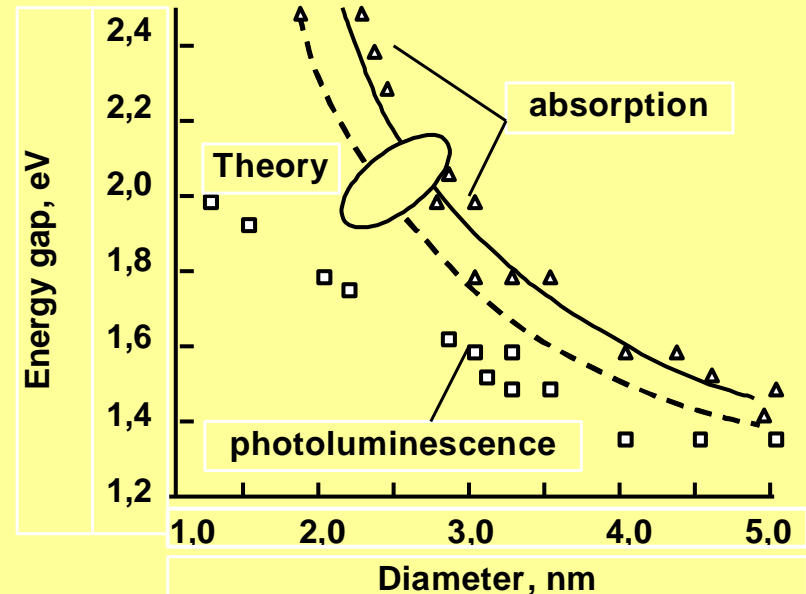
$$\alpha = \left(h\nu - E_g \pm E_{ph} \right)^2$$

/P.M.Fauchet, In: "Properties of porous silicon",
ed.L.Canham, Emis, N18, 1997

Energy band of nano-porous Si

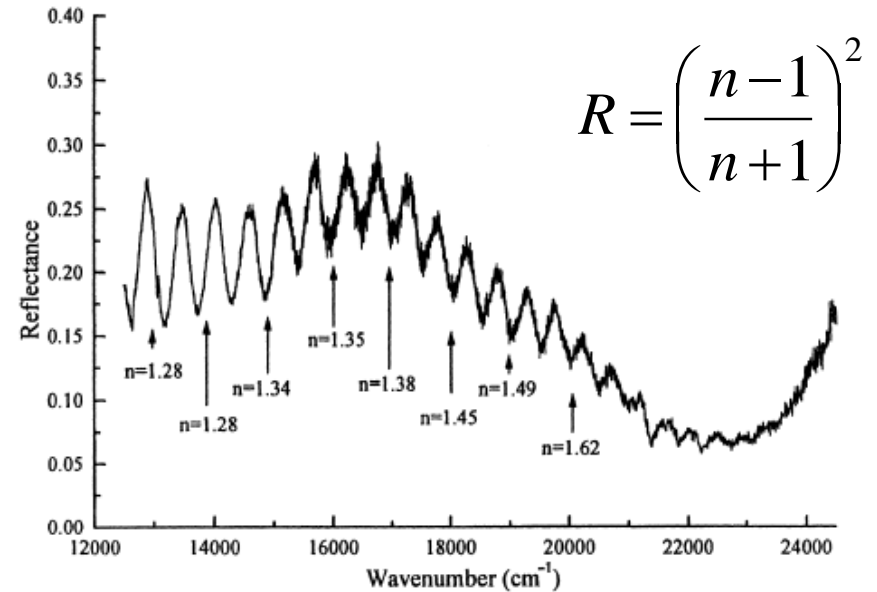
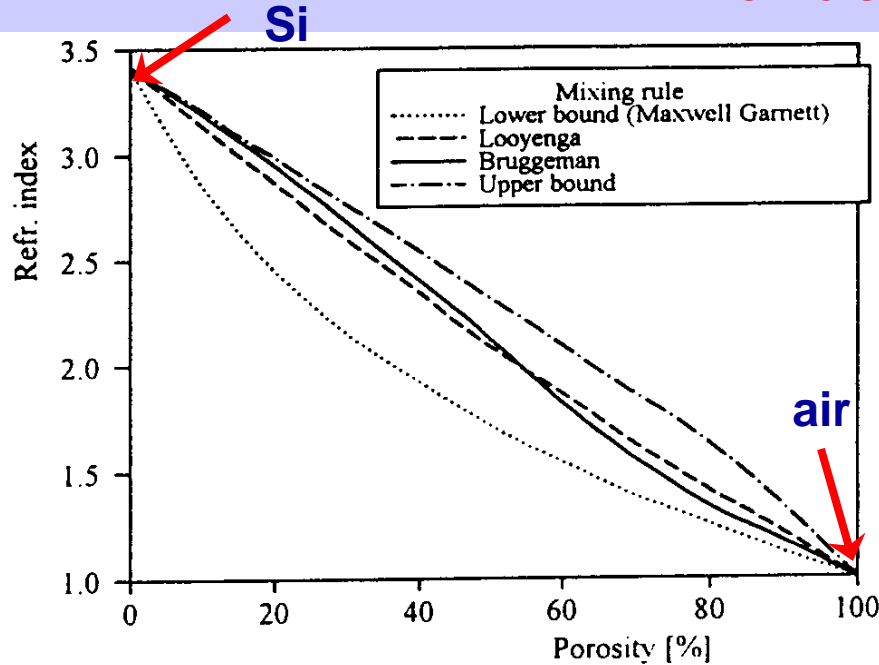


Energy position of c-band minimum and v-band maximum vs anodization current



Energy band gap vs diameters of Si particles

Refractive index



Bruggeman effective medium approximation

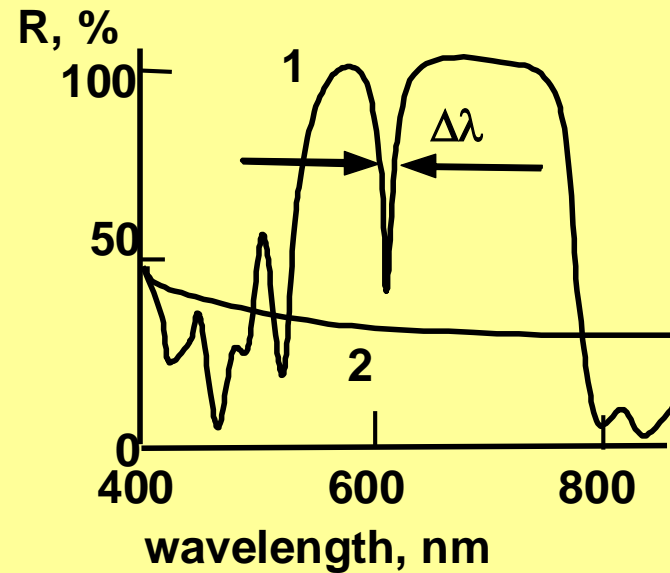
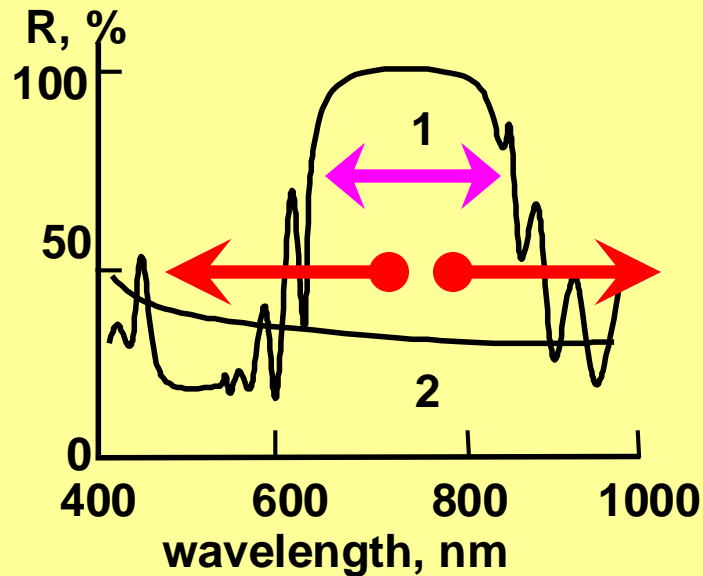
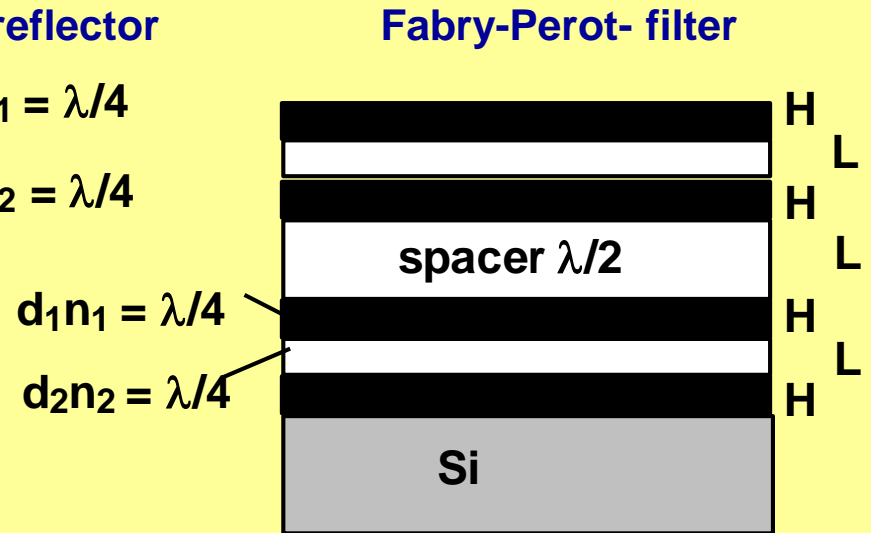
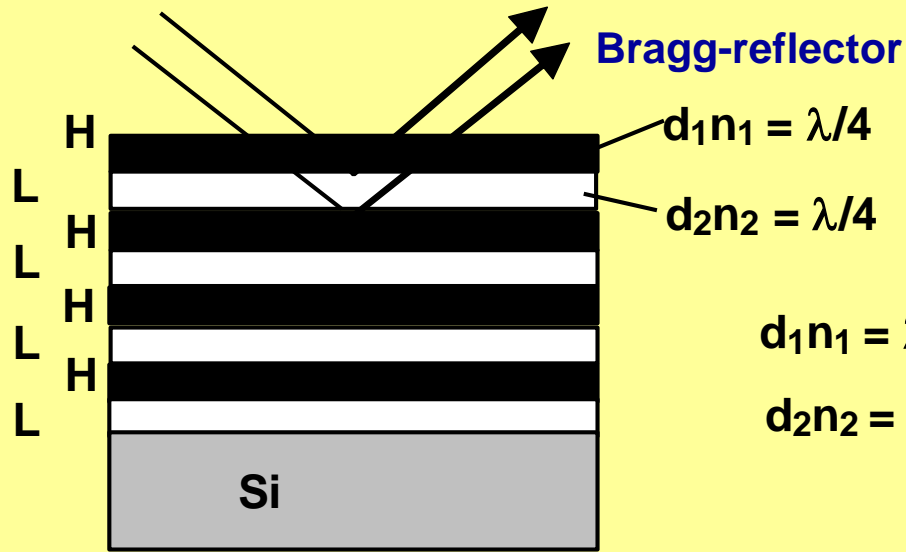
$$P \left(\frac{1 - \hat{\epsilon}}{1 + 2\hat{\epsilon}} \right) + (1 - P) \left(\frac{\hat{\epsilon}_{Si} - \hat{\epsilon}}{\hat{\epsilon}_{Si} + 2\hat{\epsilon}} \right) = 0$$

$$\hat{n} = \sqrt{\hat{\epsilon}} \quad \hat{\epsilon} = \epsilon_1 + i\epsilon_2 \quad P = \frac{V_{pore}}{V_{pore} + V_{Si}}$$

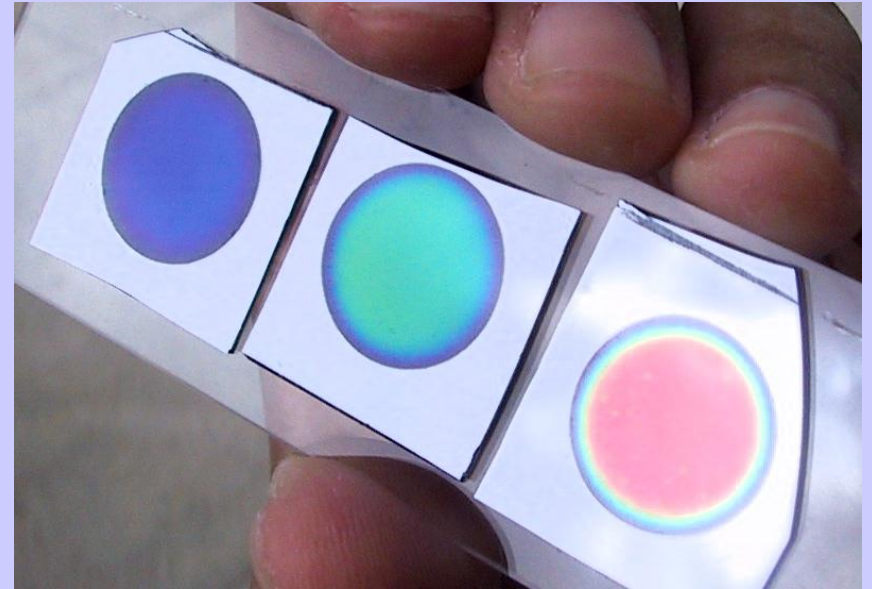
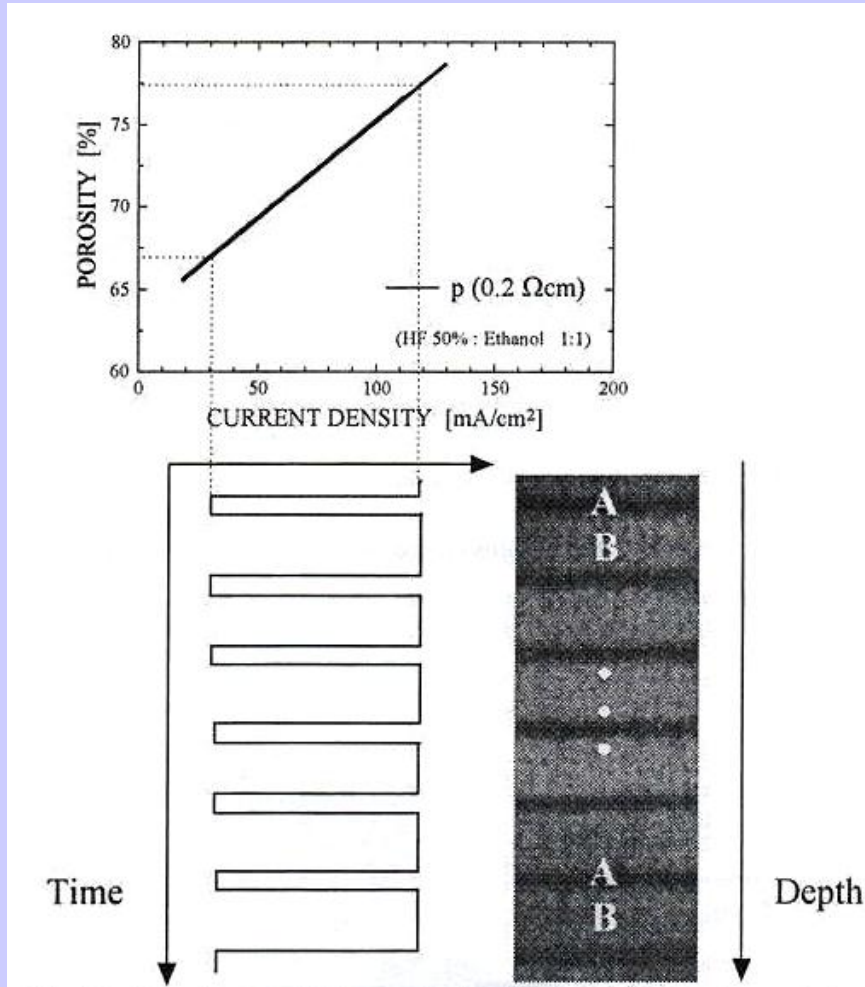
$$\epsilon = (1-P)\epsilon_{Si} + P\epsilon_{air}$$

$$n = \frac{1}{2d} \left(\frac{1}{\lambda_k} - \frac{1}{\lambda_{k+1}} \right)^{-1}$$

Optical multi-structures



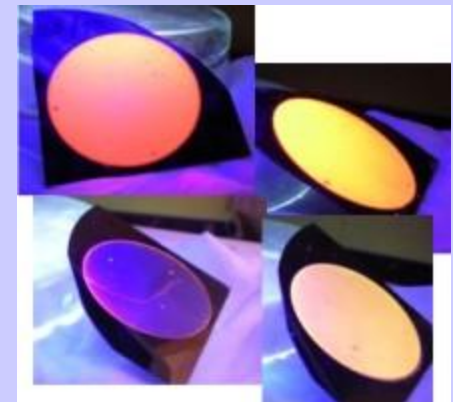
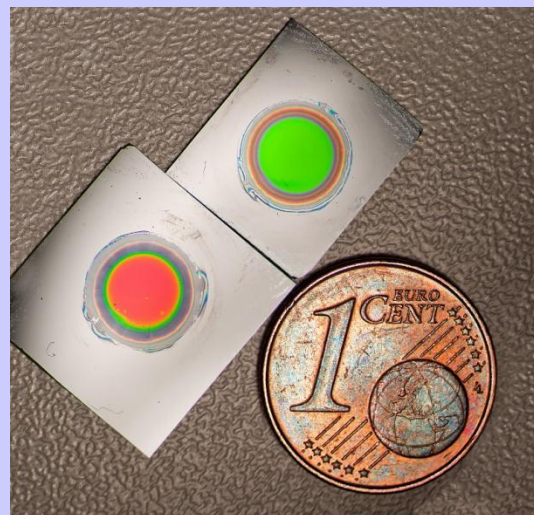
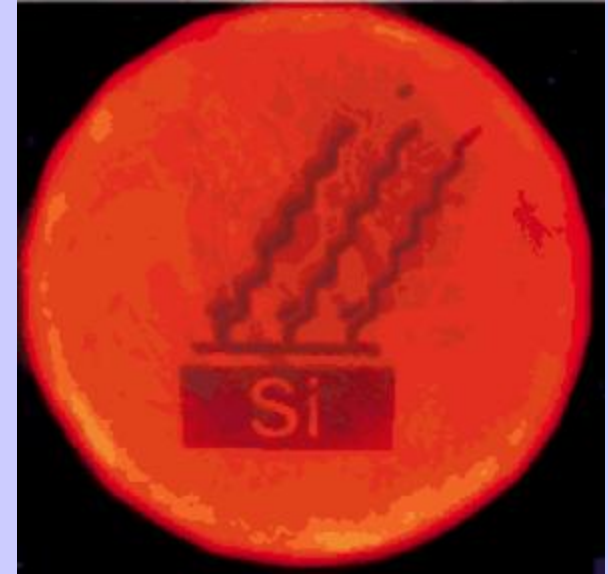
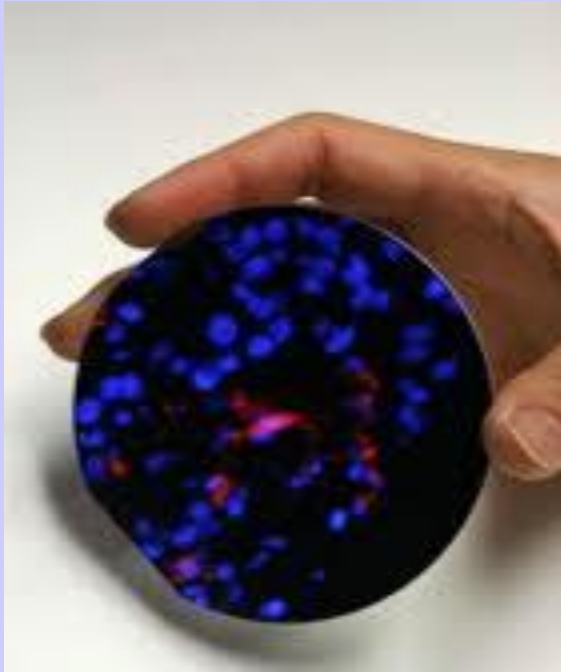
Bragg's reflectors



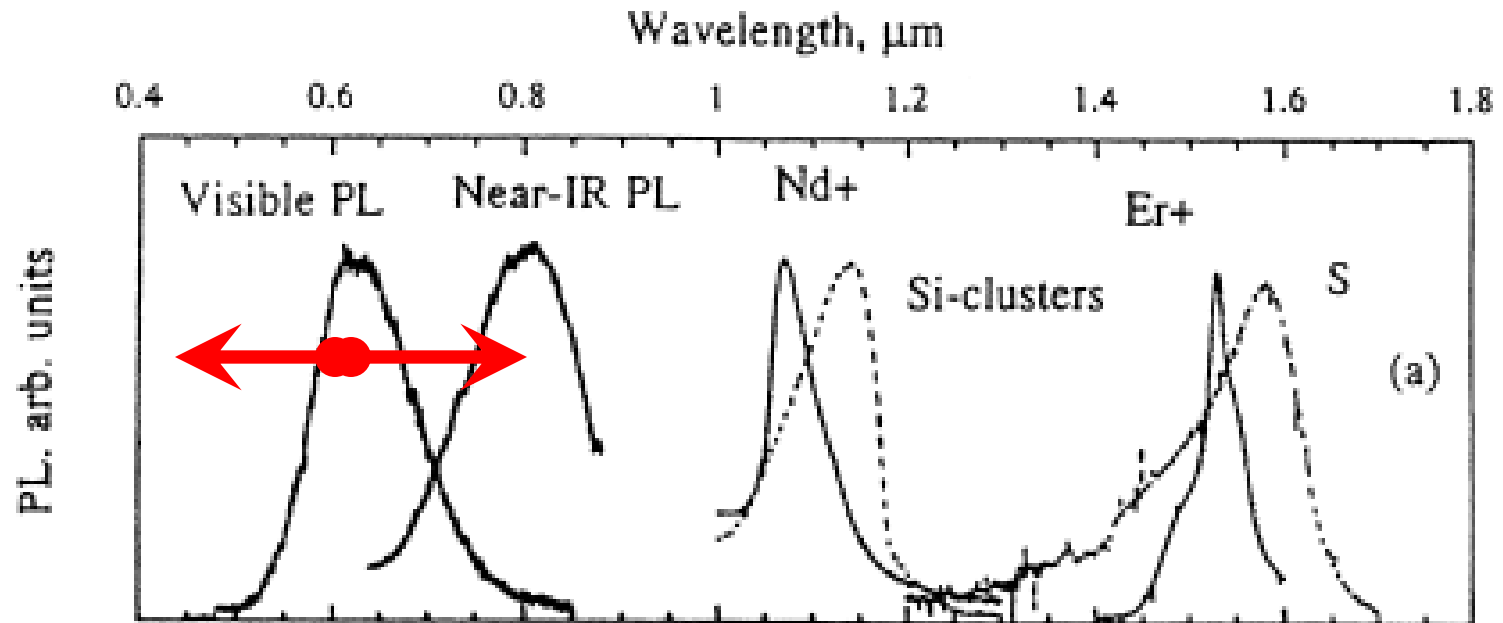
$$m\lambda_{Bragg} = 2(d_1n_1 + d_2n_2)$$

$$\lambda_{Bragg} \uparrow \Rightarrow d_{12} \uparrow n_{12} \uparrow$$

Photoluminescence of nano- porous Silicon at UV illumination at T_{room}



Photoluminescence of nano-porous Silicon at UV illumination at T_{room}

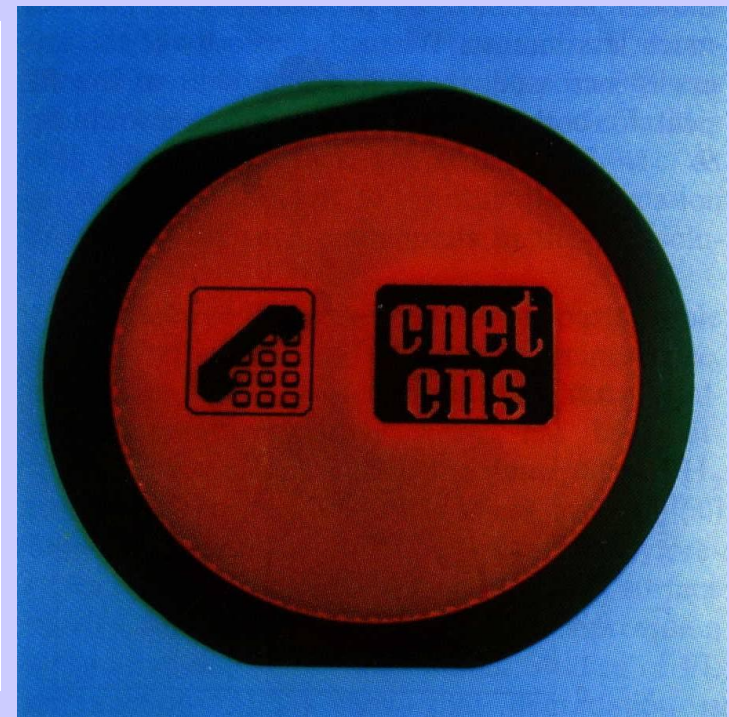
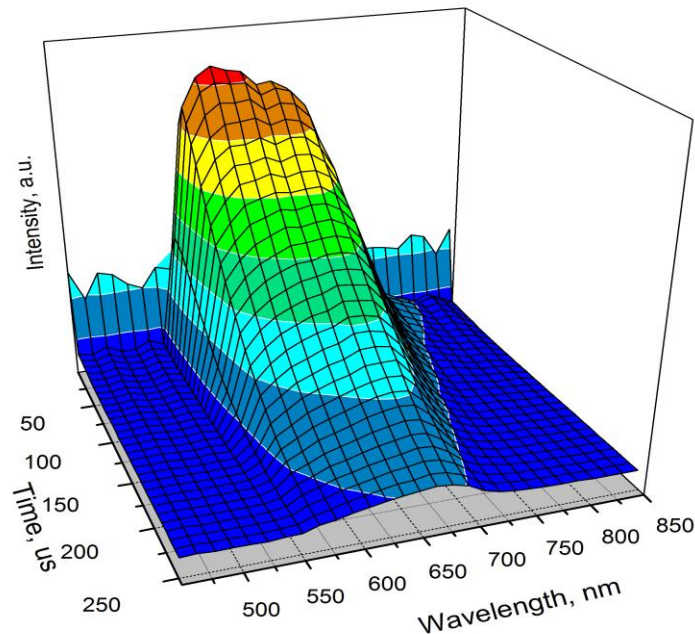


Spectral range	Peak wavelength	Label
UV	~ 350 nm	UV band
Blue-green	~ 470 nm	F band
Blue-red	400–800 nm	S band
Near IR	1100–1500 nm	IR band

Photoluminescence of nano- porous Silicon

Some spectral characteristics of the S-band (adapted from Ref. [459])

Property	Typical values	Comments
Peak wavelength	1100–400 nm	At 300 K
PL efficiency	$\geq 5\%$	At 300 K and for external quantum efficiency
FWHM	0.3 eV	At 300 K (8 meV in porous silicon microcavities)
PL decay times	$\simeq 10 \mu\text{s}$	Strongly dependent on wavelengths, temperature and aging condition
Polarizability ratio	$P \leq 0.2$	
Fine structure under resonant excitation	Phonon replica at 56 and 19 meV	Heavily aged PS, energies typical of Si phonons



Si QDs preparation in colloidal solution

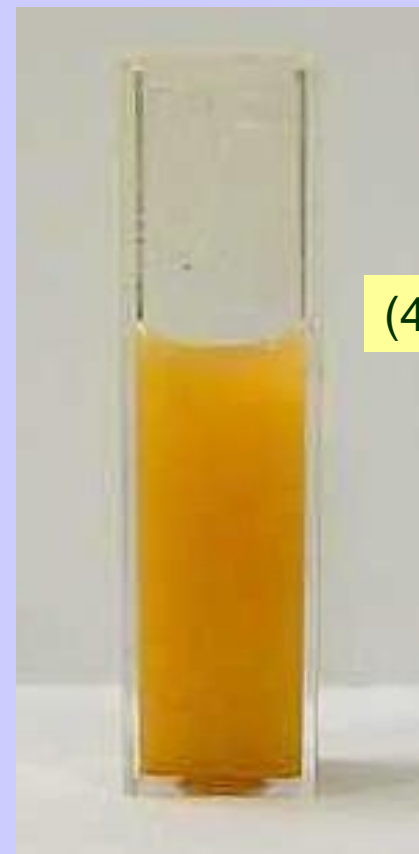
- 2) Grinding of layer
- 3) Few times washing in pure ethanol, drying and formation of homogeneous micro powder
- 4) Dissolution in pure ethanol **2-5 mg/mL**



(2)



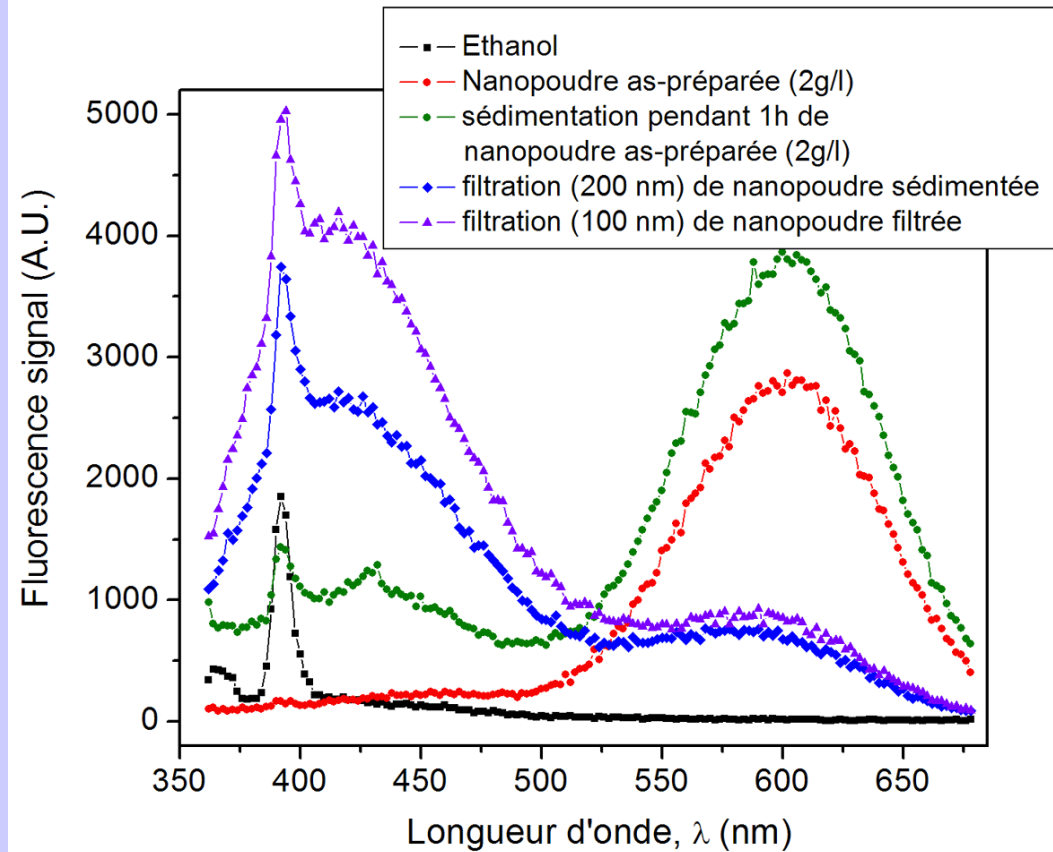
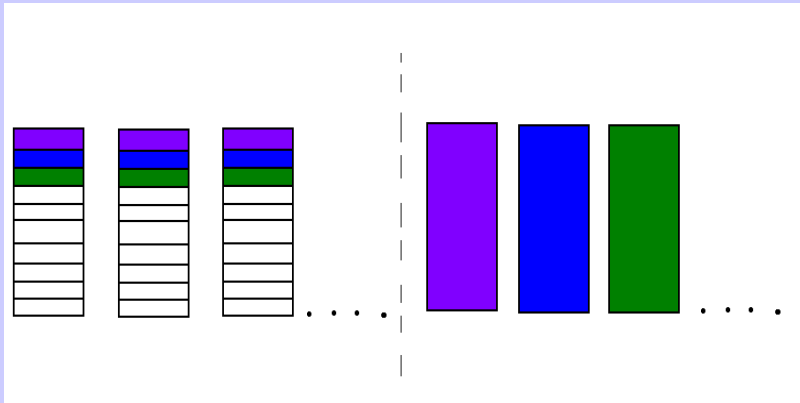
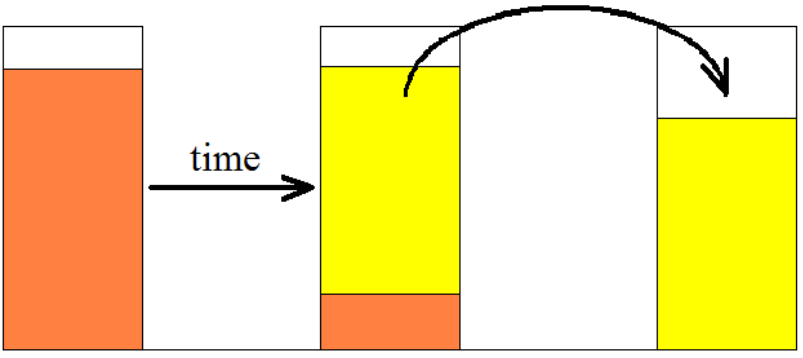
(3)



(4)

Sedimentation+ filtration

(5)

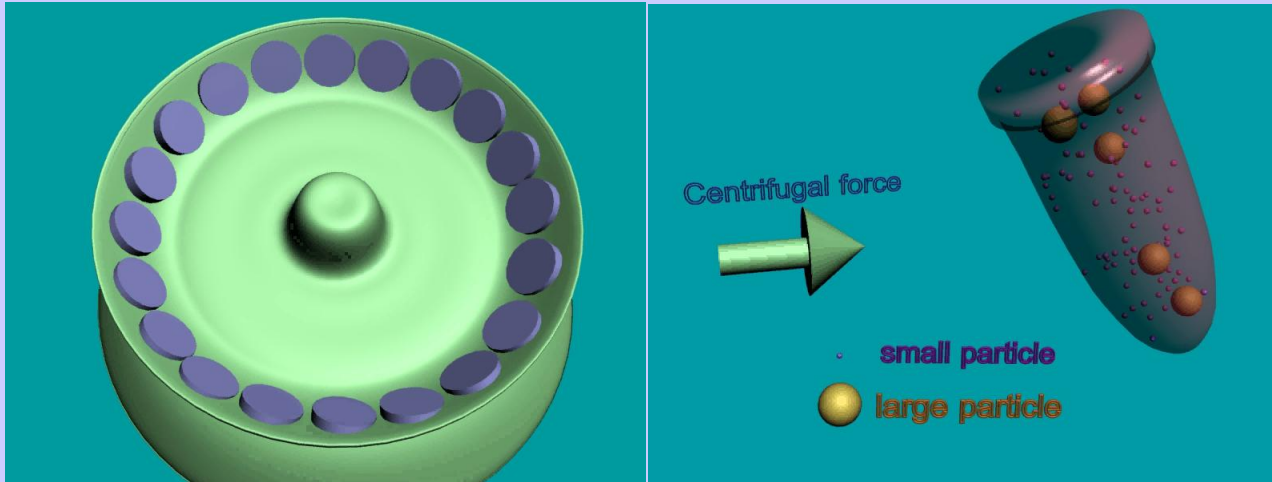


PhL of different sedimented layers

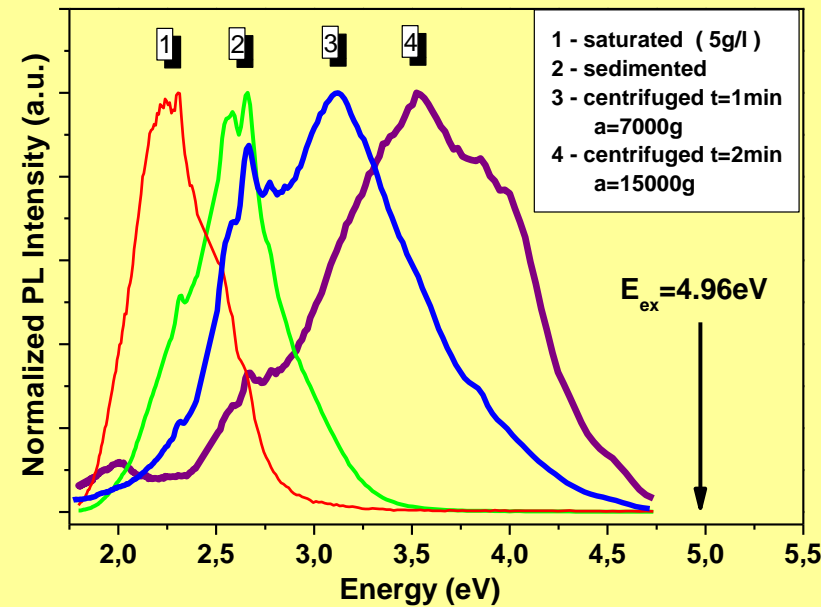
V.Lysenko, V.Onyskevych, O.Marty, V.Skryshevsky, Y.Chevolot, C.Bru-Chevalier, Appl.Phys.Lett, 92(2008) 251910

Centrifugation

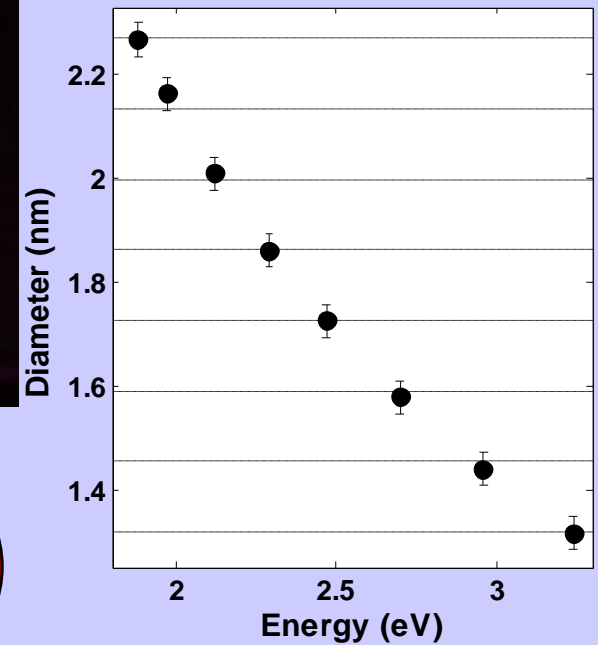
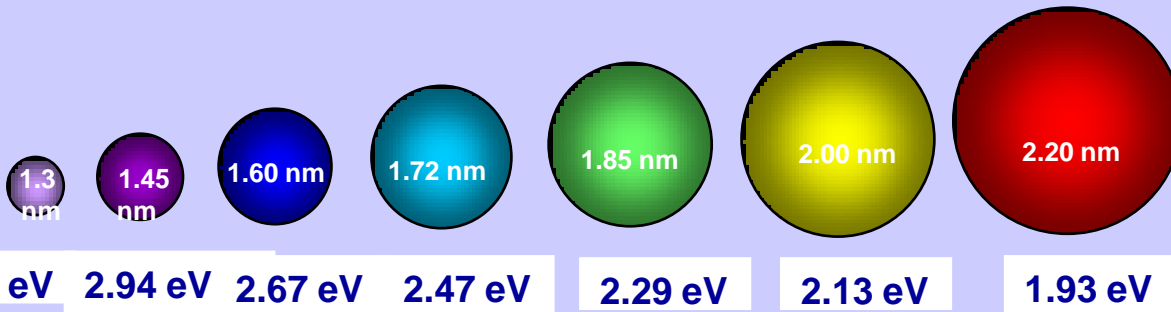
(6)



PL spectrum of the initial PS nanopowder in ethanol solution and its evolution upon sedimentation and moderate centrifugation

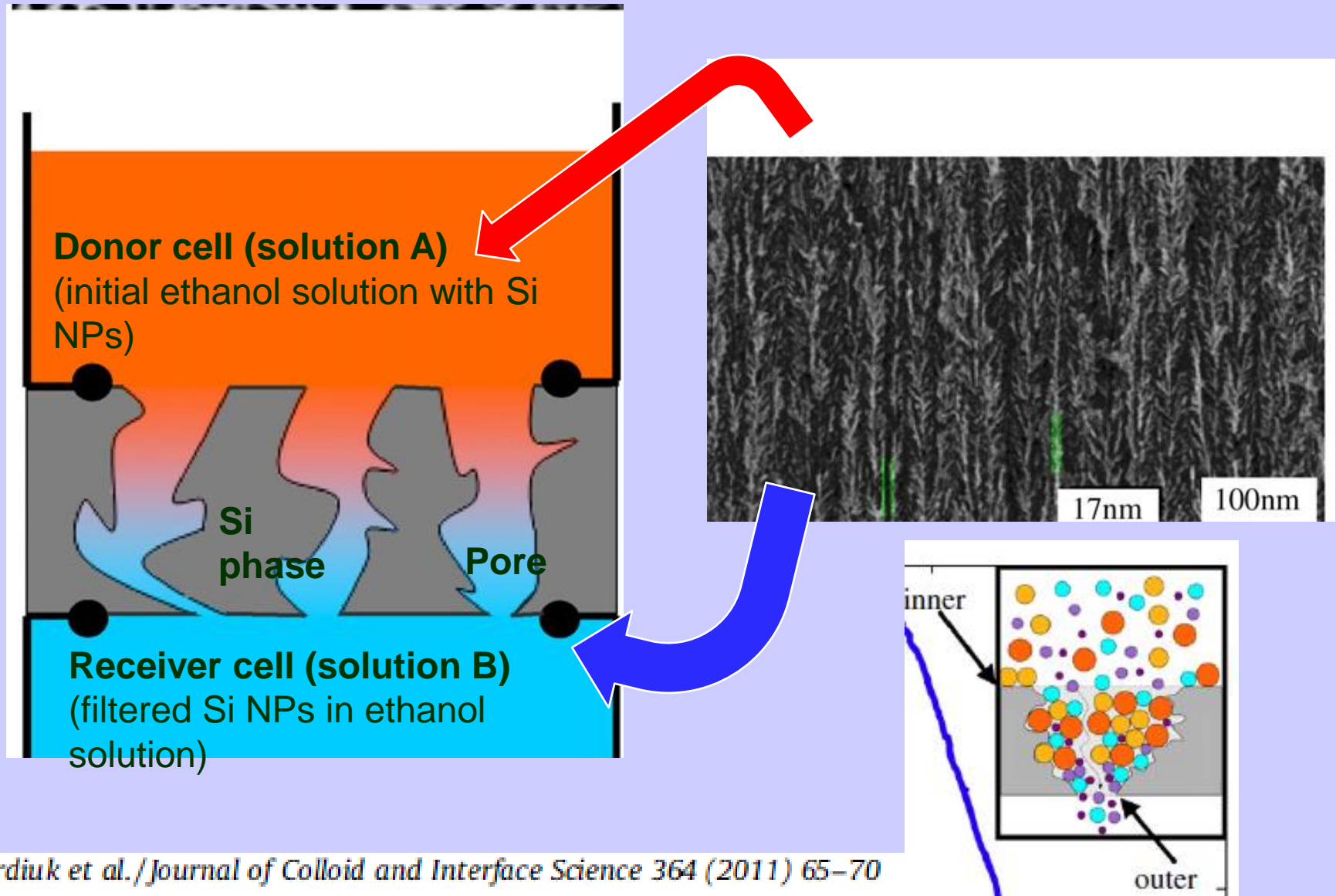


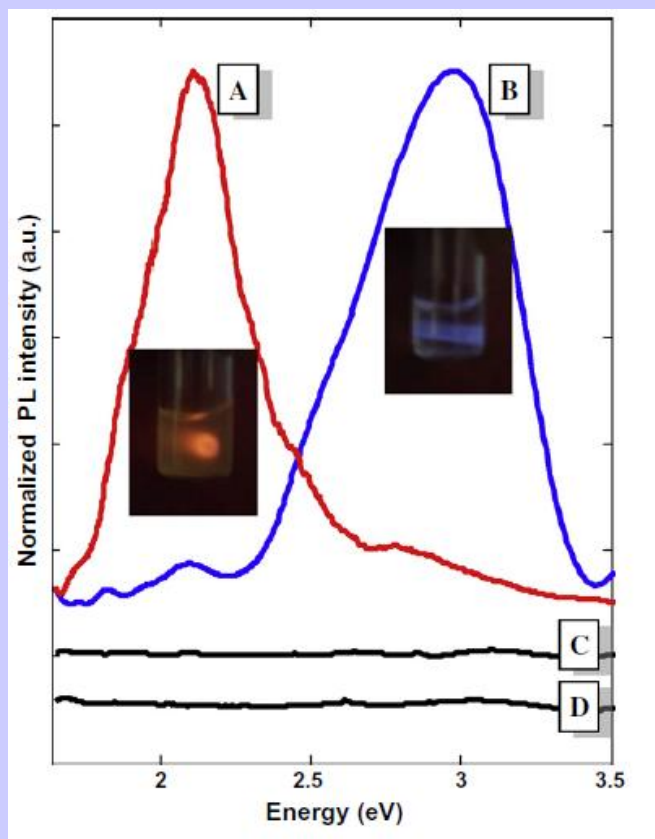
Semiconductor nanoparticles



J.K. Jaiswal, S. M. Simon, *Trends in cell biology*, vol 14, 497-504 (2004)

Autofiltration of nano-Si particles





PL spectra with corresponding photos of initial (curve A) and filtered (curve B) ethanol solutions with dispersed Si NPs.

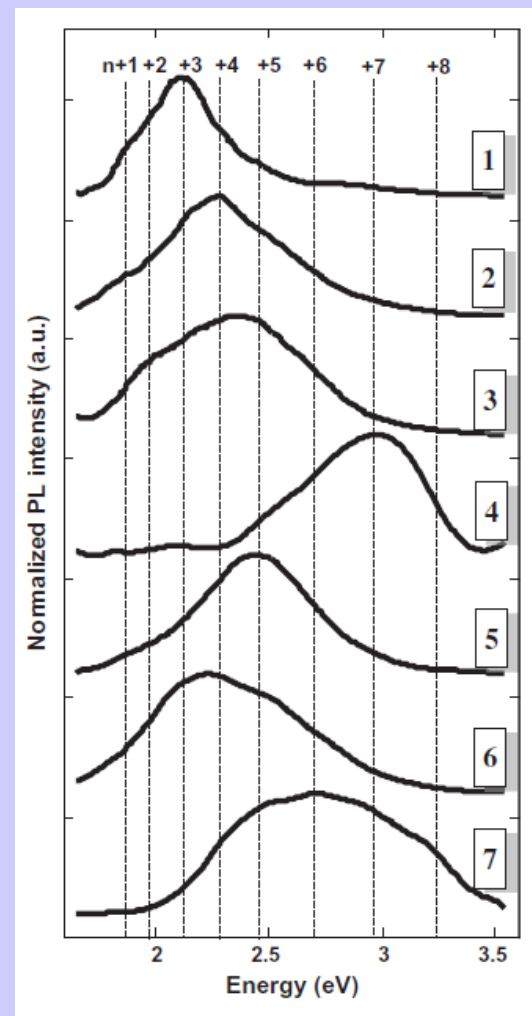
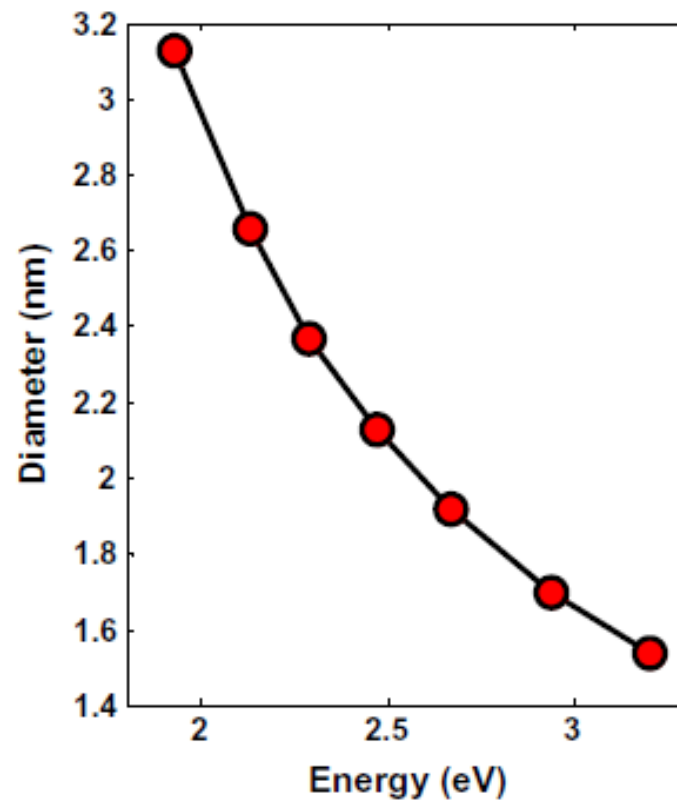
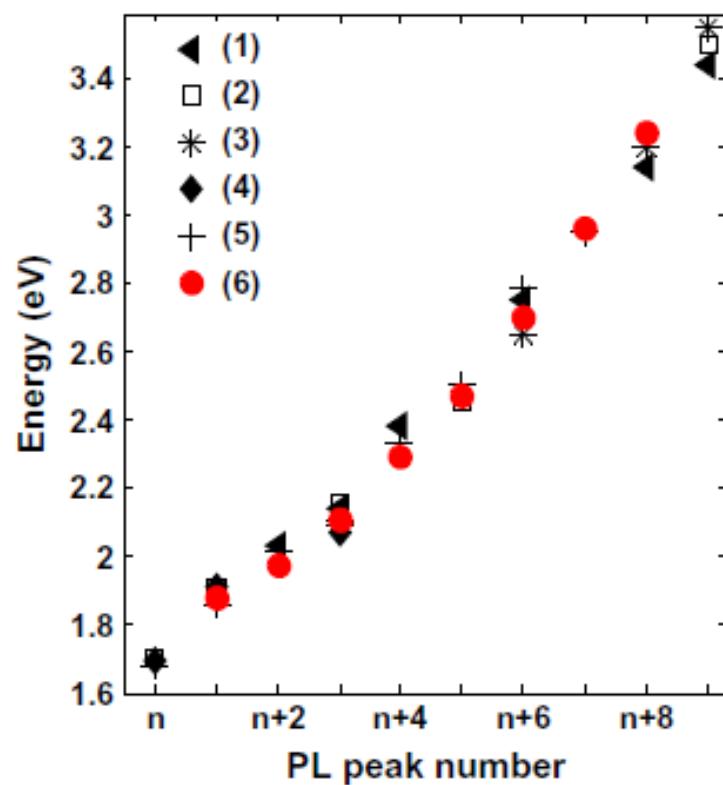


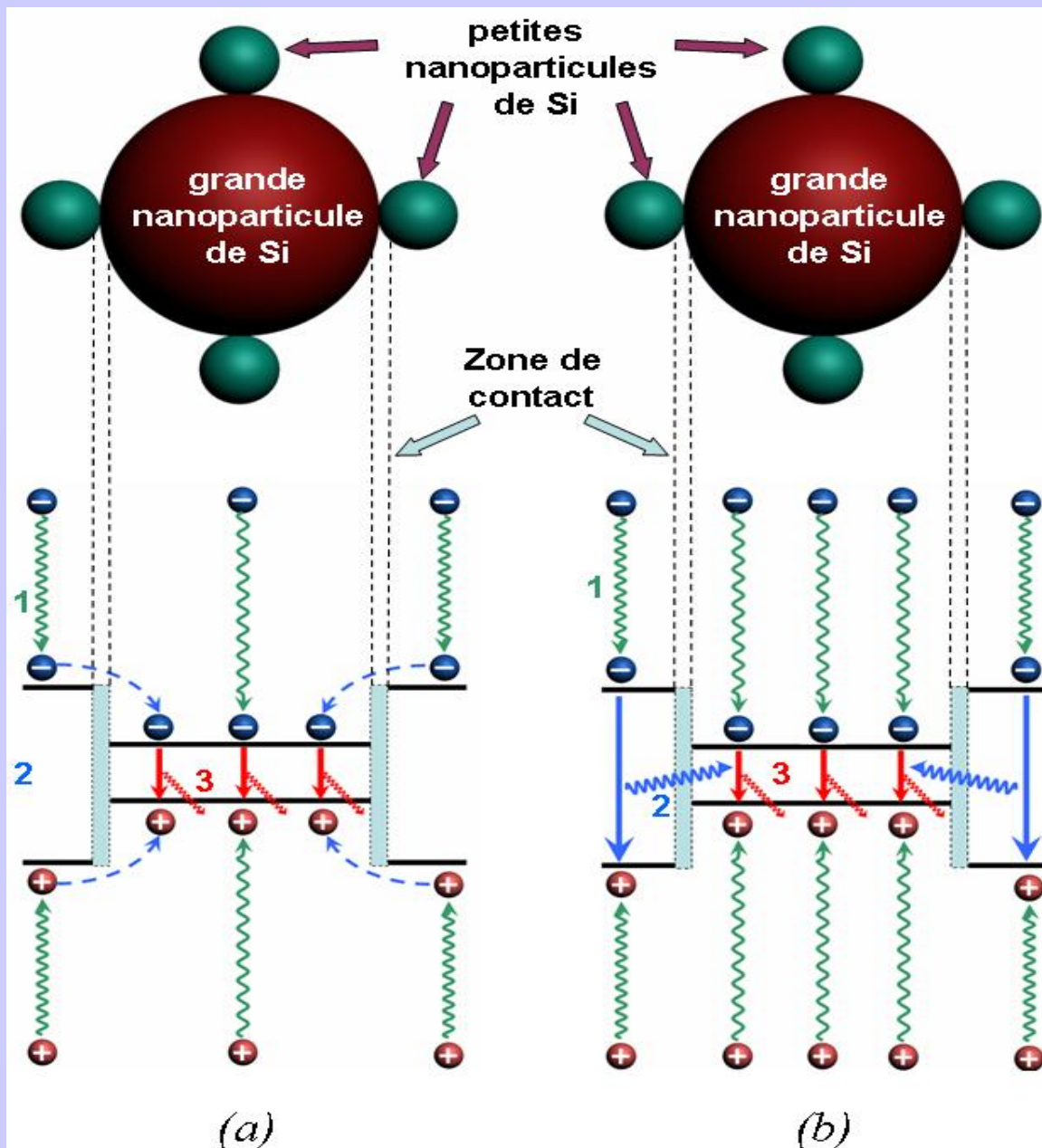
Fig. 6. PL spectra of Si NPs dispersed in initial (curve 1) ethanol solutions, filtered with the use of 23- μm thick free-standing meso-PS membrane (curve 2), filtered with the use of 37- μm thick free-standing meso-PS membrane before (curve 3) and after (curve 4) oxidation in 1:1 volume mixture of deionized water and ethanol at about 320 K during 15 min, filtered with the use of 246- μm thick free-standing meso-PS membrane before (curve 5) and after (curve 6) etching in 1:10 volume mixture of HF and deionized water at room temperature during 10 min, filtered with the use of 350- μm thick free-standing meso-PS membrane (curve 7).



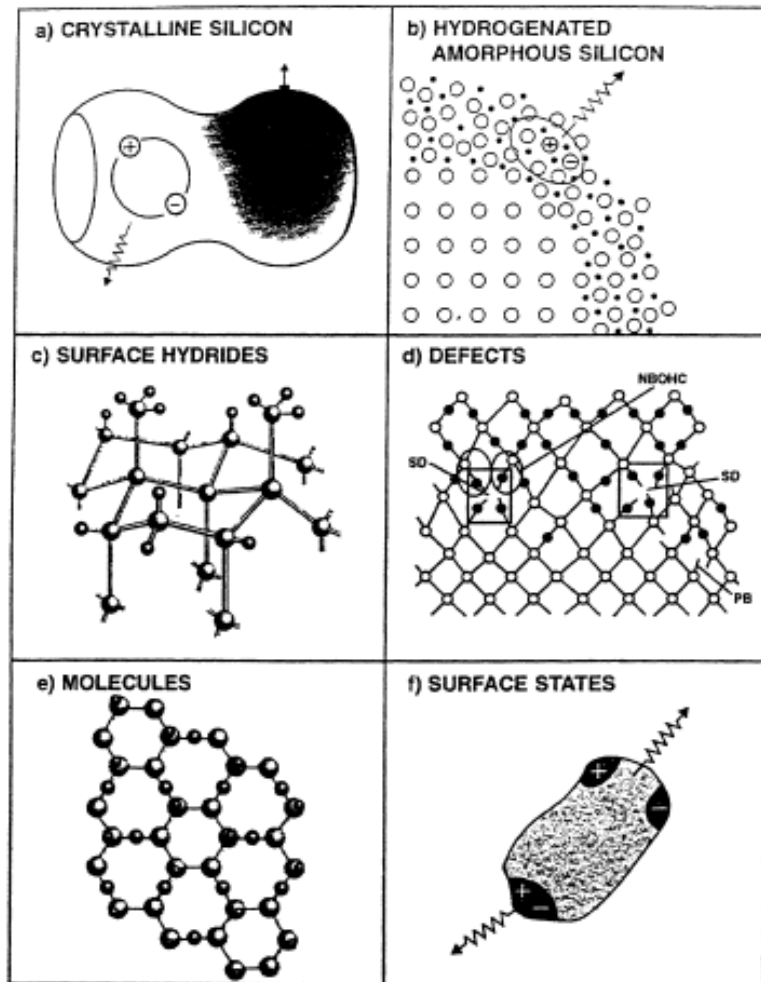
Dependence of Si NPs size calculated according to the model described in [24] on the PL peak energies reported in this work

$$E_g(d) = 1.167 + 3.73 * d^{-1.39}$$

Why UV Photoluminescence is not observed in solid PS?

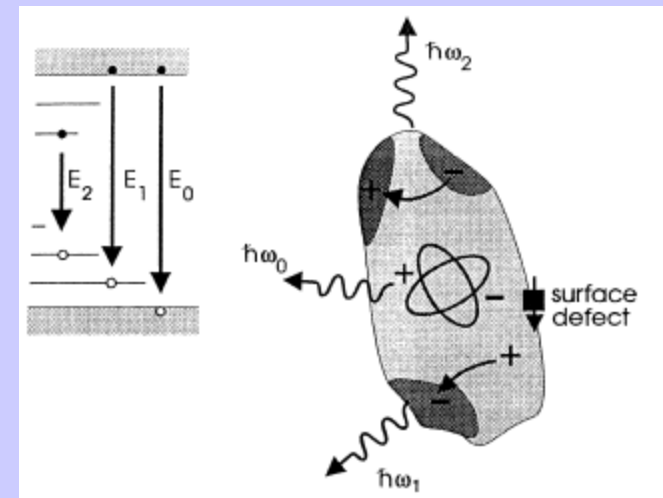


Photoluminescence models



KEY

- - silicon atoms
- - oxygen atoms
- - hydrogen atom

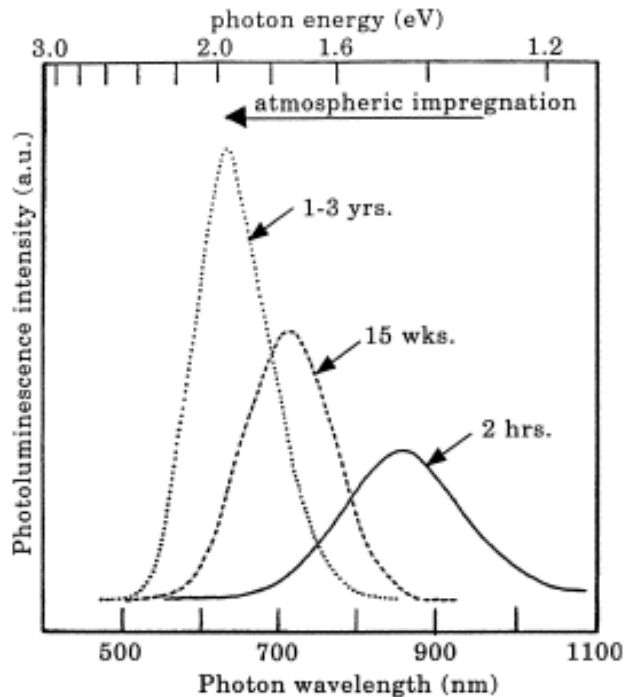


Hierarchy of transition in the SS model. The indices 0,1,2 indicate the number of SS involved

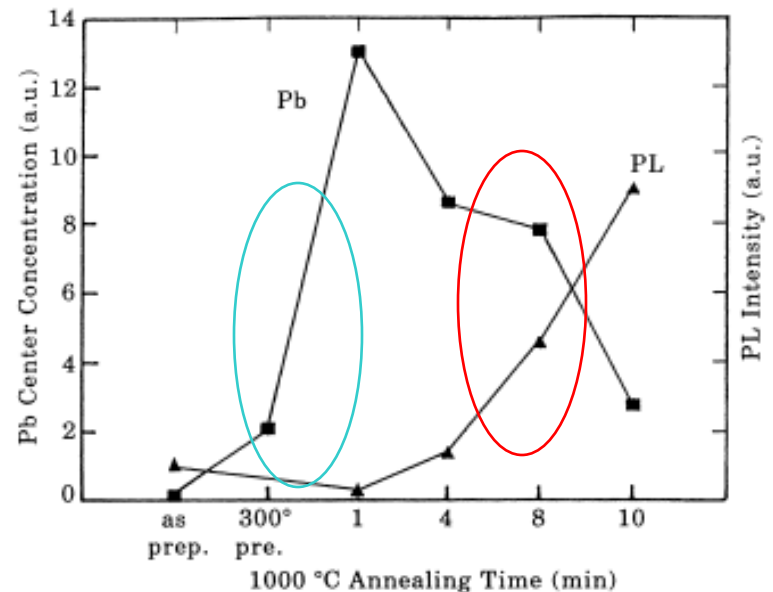
The six group of models proposed to explain PS PhL

- a) Crystalline QW. Localized on SS or free exciton recombination
- b) c-Si covered by layer of hydrogenated a-Si, where recombination occurs
- c) Si surface passivated by SiHx terminations. Radiative recombination occurs at the Si-H bonds
- d) Partially oxidized Si containing defects proposed as radiative centers
- e) Siloxene molecule $\text{Si}_6\text{O}_3\text{H}_6$ is proposed to exist on the large inner PS surface and act as luminescence center
- f) Si dot with SS that localize carriers and holes separately (upper part) or together (lower part, radiative recombination)

Photoluminescence aging and alternative model of PhL



Aging: blue shift of emission due to reduce of nanoparticle size



Dangling bond (Pb centers) concentration and PhL vs annealing time at 1000°C in O₂

Dangling bonds- most important paramagnetic defect centers: in Si/SiO₂ interface

•**Si≡Si₃ (Pb centers)**

in hydrogen depleted oxide layer

•**Si≡SiO₃ (E' center)**

Electrical transport in microporous Si

- a. Bandgap fluctuation due to variation of nanocrystalline size,
- b. density of states in forbidden band, E_t - level of current leaking, $f(E)$ –distribution function
- c. transport mode: hopping on surface states(I), thermogeneration, thermoionic or tunneling across state tails
- d. Poole-Frenkel mechanism

Surface states:

Density $>10^{12}-10^{14} \text{ cm}^{-2}\text{eV}^{-1}$

Free carriers:

Density $<10^{10}-10^{13} \text{ cm}^{-3}$

Mott law for jump (hopping):

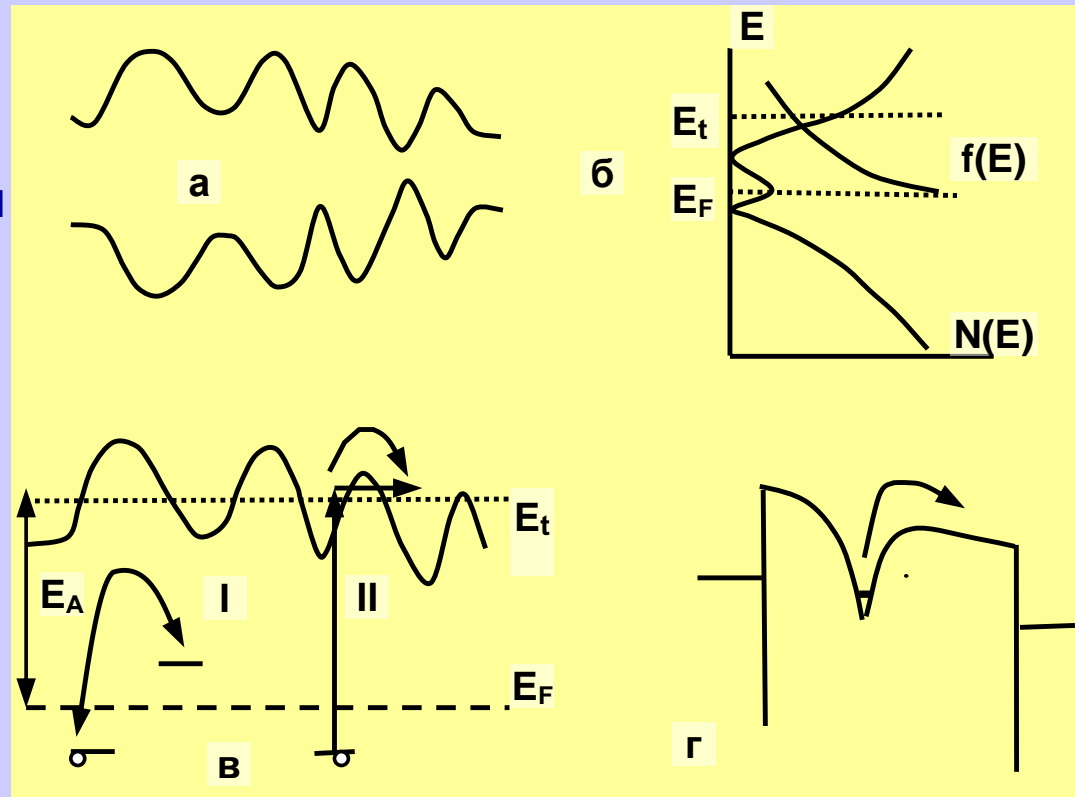
$$\sigma(T) = \sigma_0 \exp(T / T_0)^m, m = 4$$

Poole-Frenkel ionisation:

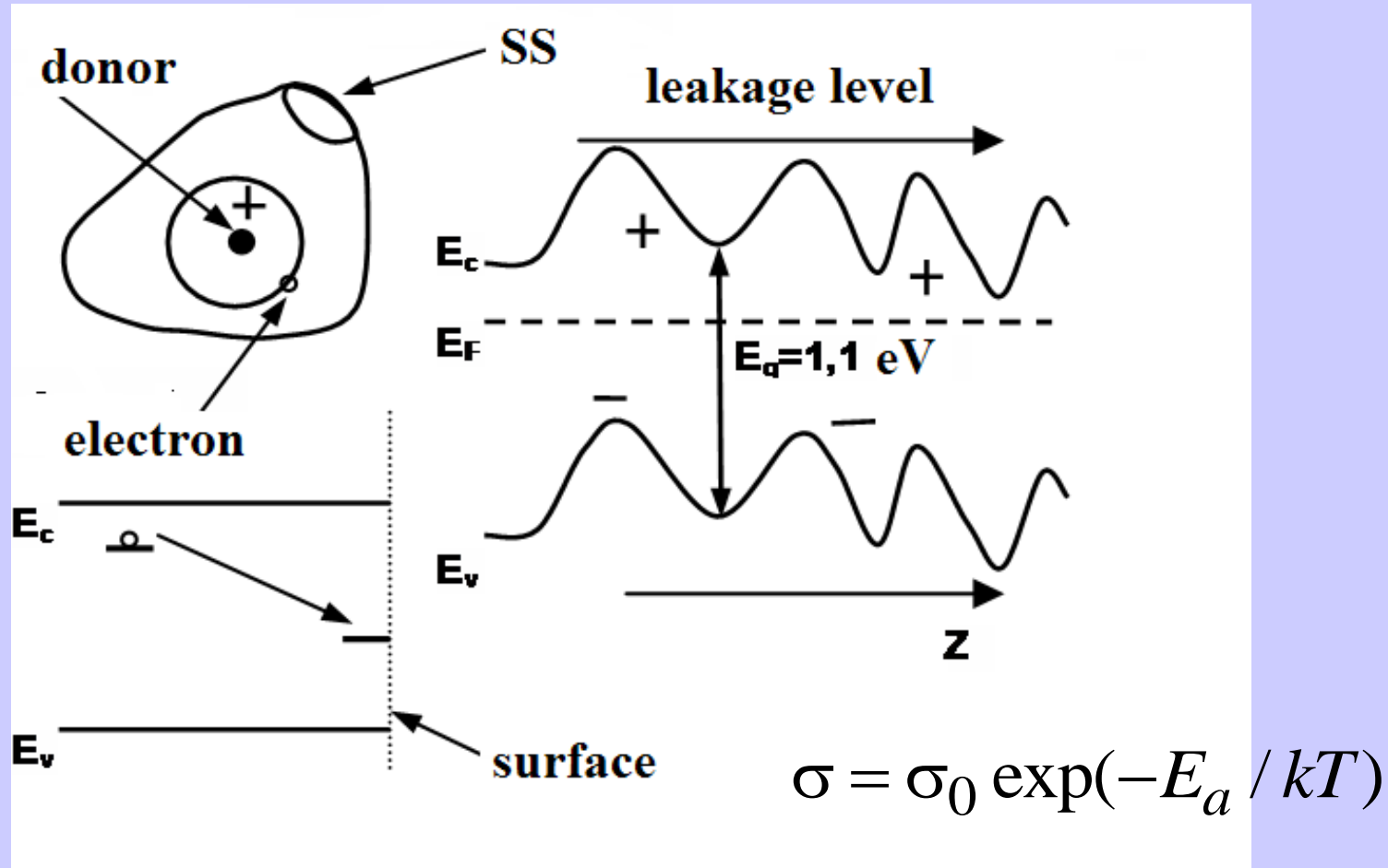
$$\sigma(V, T) = \sigma_0 \exp\left(\frac{E_a}{kT}\right) \exp\left(\beta \sqrt{\frac{V}{V_0(T)}}\right)$$

Space charge limited current:

$$I = \gamma(T) \frac{V^n}{d^m}, \quad n \sim 2$$



Electrical transport in macroporous Si



Initial Si is heavy doped, but meso-PS is high resistive!

a) Cross-section of Si microwire that shows the process of free electron capture on surface state of acceptor type, b) energetic sketch of process, b) band modulation due to electric field between D^+ and negatively charged SS. Z- direction along Si microwire

New perspectives: Other stable Si nanoparticles

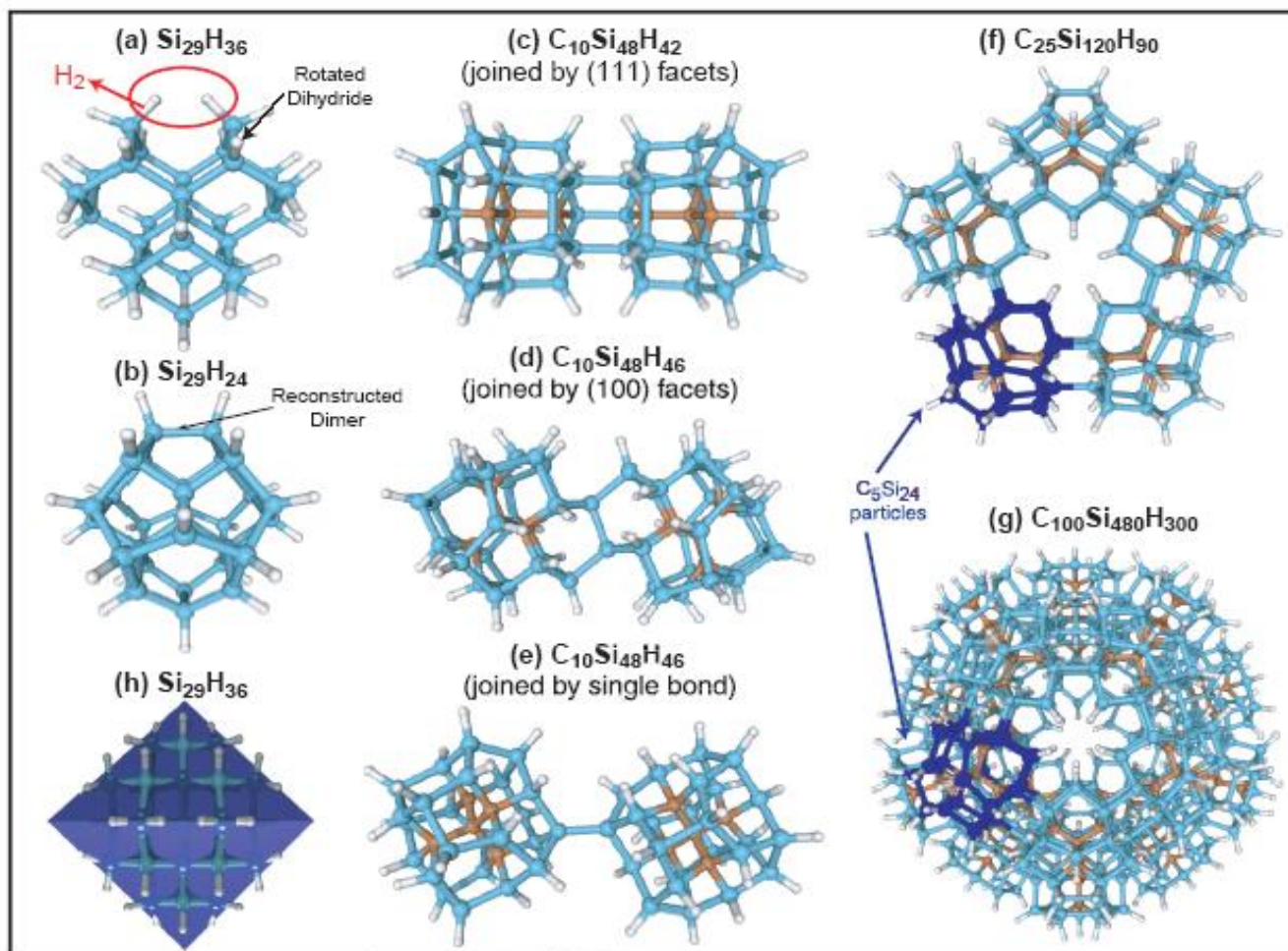


FIG. 1: Calculated atomic structures of single, double, 5-fold and 20 nanoparticles structures. Si, C and H atoms are colored blue, brown and white. In (f) and (g) atoms in a single C_5Si_{24} particle are highlighted in dark blue.

Properties of Micropores or nanocrystalline Si. Summary

Features:

- Surface area – **200- 1000** m²/cm³
- $E_g = 1.1- 3.0$ eV
- Resistivity $\rho = 10^8-10^{12}$ Ω .cm
- Carrier mobility $10^{-3} - 10^0$ cm²/V.s
- Quantum efficiency of PL- more than 10 %
- Quantum efficiency of EL - 1 %
- Chemical composition (Cullis A.G., Canham L.T, J.Appl.Phys, 82(1997) 909).

Condition of porous Si	Chemical composition
1. In situ in HF during and after formation	SiF_xH_y
2. Freshly etched in inert ambient	SiH_x
3. Chemically or anodically oxidized 4. Rapid thermally oxidized at high temperatures	SiO_xH_y
5. Aged in ambient air for months to years	$\text{SiO}_x\text{H}_y\text{C}_z$