



**Porous silicon and Si nanoparticles:
new photonic and electronic materials
*Technologies and physics properties***

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OUTLINE

1

Quantum confined effect

2

Technology of nano- and Porous Si

3

Optical properties

Surface

Luminescence

Electrical properties

4 Applications

Wave-guides, optical fibers, filters, mirrors

Chemical & bio-sensors

Photonic crystals

Microelectronics: SOI, Si epitaxy

Solar Cells

Hydrogen reservoirs

Explosive materials

LED,

Bioreactors, synthesis

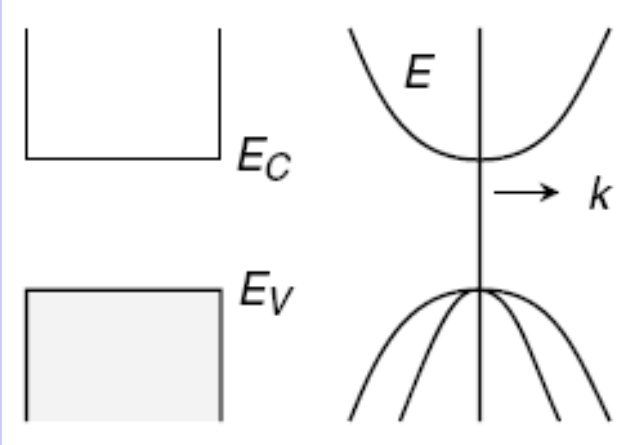
Medicine: Implants, Diagnostics electrophoresis, drug deliver

Evolution of modern semiconductor physics: *from bulk to nano*

- Band theory + doping
- Effective mass theory

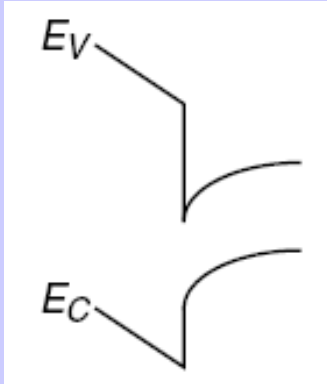
$$p = \hbar k$$

$$E = \frac{\hbar^2 k^2}{2m_0}$$

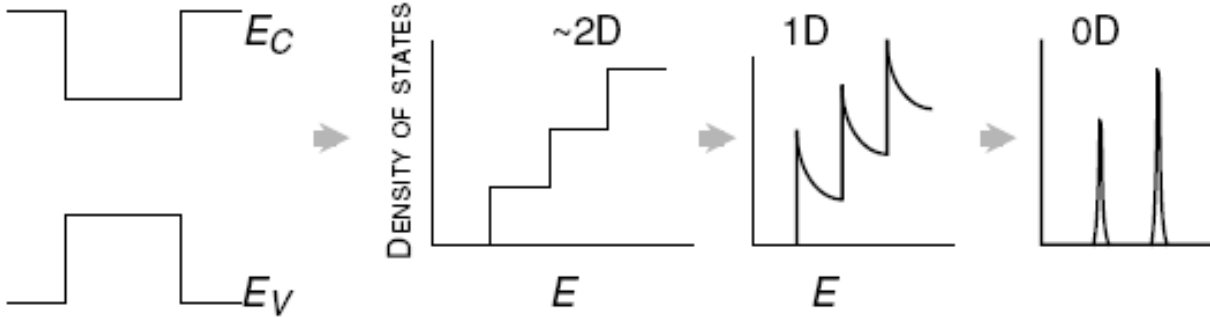


Semiconductor transistor

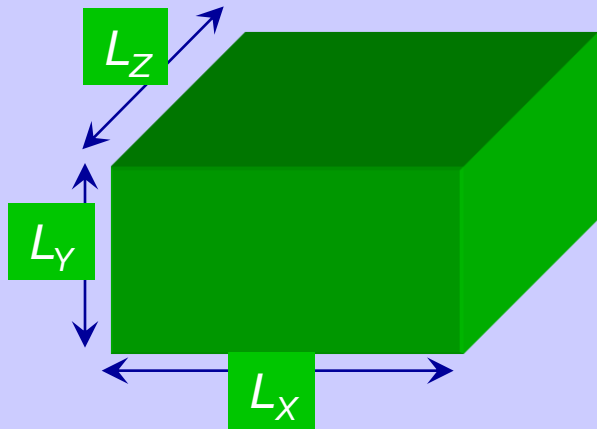
Semiconductor laser



HETEROSTRUCTURES
 Heteroepitaxy, strained epitaxy, self-assembly
 ➔ carrier confinement
 ➔ low-dimensional systems



Why nano ?



Move of electron in periodic field of lattice
Schrodinger equation

$$\left[\frac{-\hbar^2}{2m_0} \nabla^2 + U(\mathbf{r}) \right] \psi(\mathbf{r}) = E\psi(\mathbf{r})$$

$$\psi(\mathbf{r}) = u(\mathbf{r})e^{i\mathbf{k}\cdot\mathbf{r}}$$

**Quantum effects
for electron in Si:
 $\lambda \sim 3 \text{ nm}$**

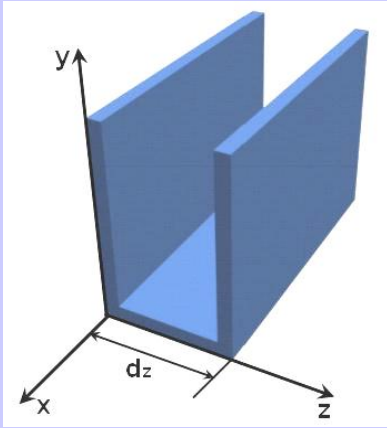
**Geizenberg
equation**

de Broglie wavelength (λ) – quantum phenomena

$$\lambda \approx L_i$$

$$\lambda = \frac{h}{p} = \frac{h}{m_e^* v} \quad m_e^* \sim 0.2m_0$$

Quantum confined effect



$$V(z) = \begin{cases} 0, & 0 \leq z \leq d_z \\ \infty, & \text{autrement} \end{cases}$$

Quantum well

Quantum wire

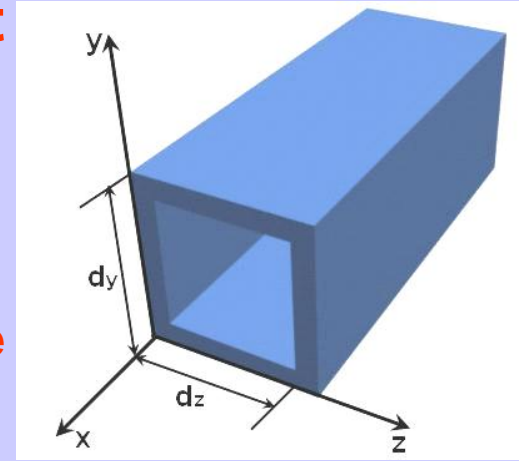


Figure 1. 1 Modèle d'un puits quantique infini : l'électron est confiné dans la direction z, sur une épaisseur de largeur d_z .

Figure 1. 1 Modèle de fil quantique infini : l'électron est confiné dans les directions z et y.

$$E = E_n^\infty + \frac{\hbar^2}{2m^*} (k_x^2 + k_y^2) \quad E_n^\infty = \frac{\hbar^2}{2m^*} \left(\frac{n\pi}{d_z} \right)^2, \quad n \in \mathbb{N}$$

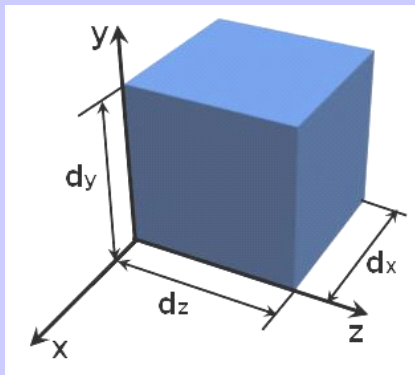


Figure 1. 1 Modèle de boîte rectangulaire : l'électron est confiné dans trois directions.

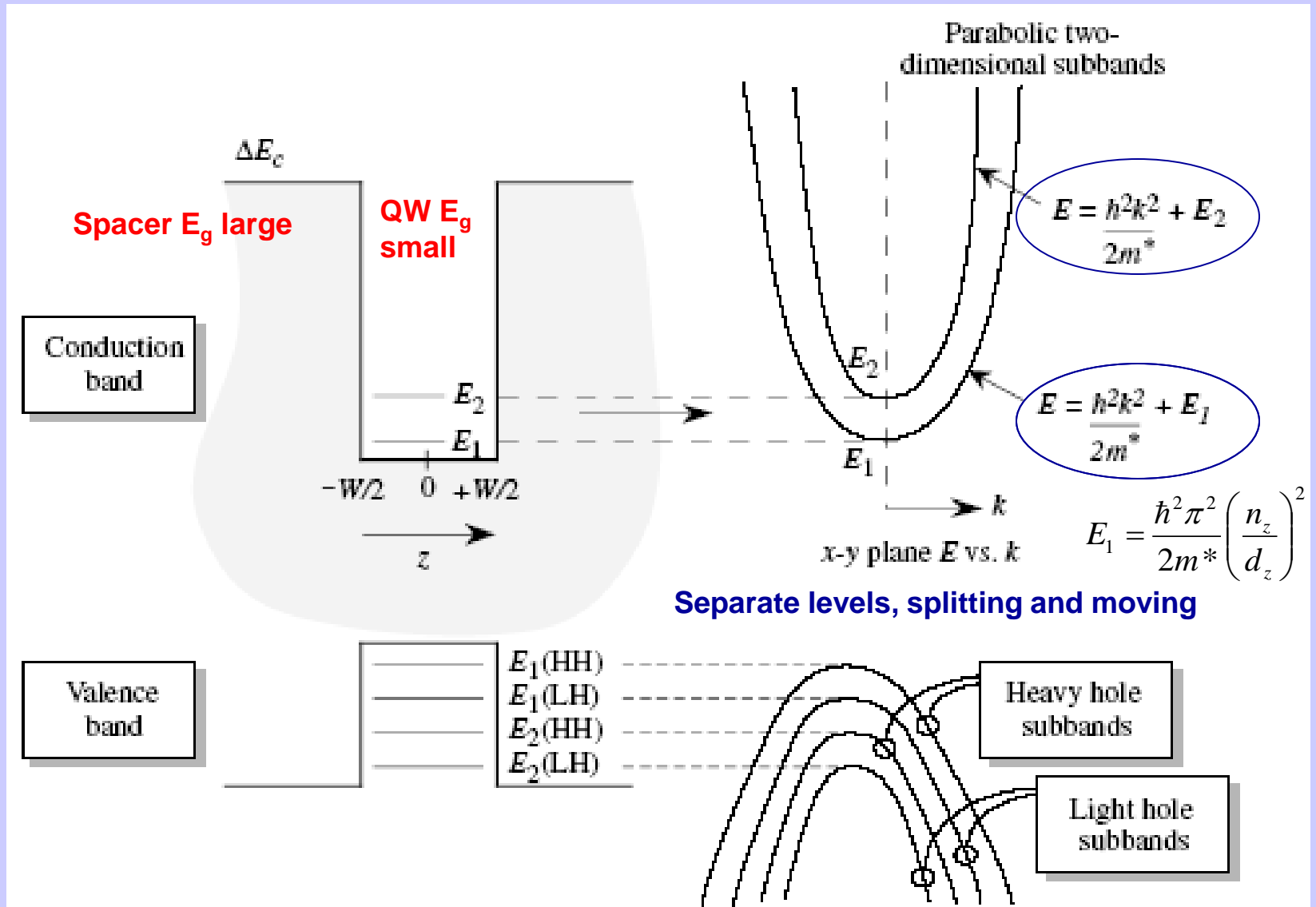
$$E = \frac{\hbar^2 \pi^2}{2m^*} \left[\left(\frac{n_y}{d_y} \right)^2 + \left(\frac{n_z}{d_z} \right)^2 \right] + \frac{\hbar^2 k_x^2}{2m^*}$$

$$E = \frac{\hbar^2 \pi^2}{2m^*} \left[\left(\frac{n_x}{d_x} \right)^2 + \left(\frac{n_y}{d_y} \right)^2 + \left(\frac{n_z}{d_z} \right)^2 \right]$$

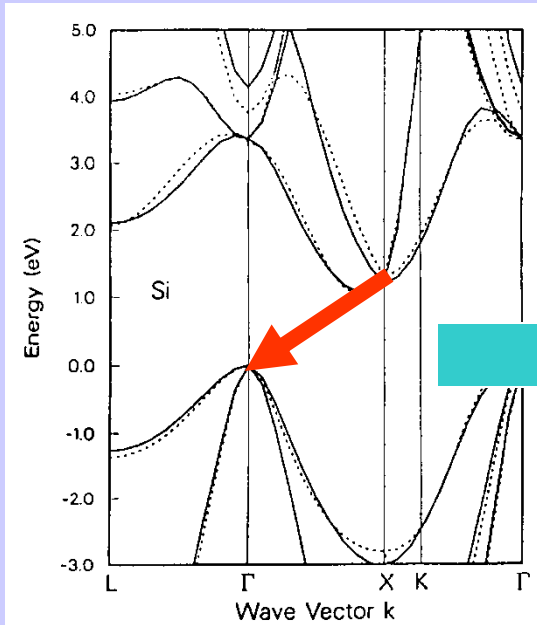
Quantum dot

Electronic spectra – series of levels like in atom !

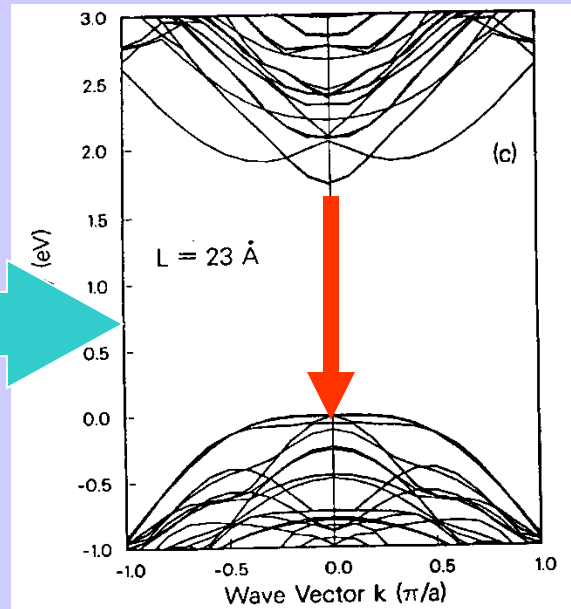
Quantum well



Band structure of nano-Si: two possibilities



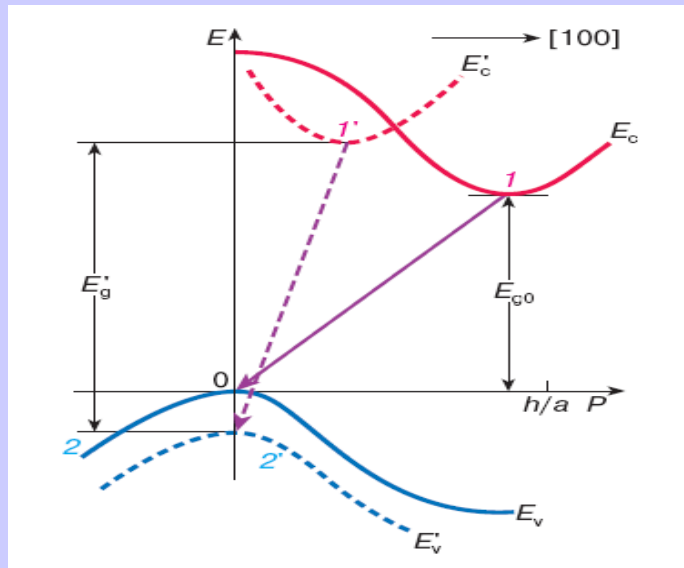
Band structure of bulk Si



Si quantum wires , L= 2.3 nm

Si Qwires:
Indirect- direct band gap transformation,
 E_g increases

Si Qdot:
Indirect band gap,
 E_g increases,
Electron-wall collision



$$E_c - E_v = h\nu$$

$$\Delta\hbar k \gg \frac{\hbar\omega}{c}$$

$$\Delta\hbar k = \frac{\hbar\omega}{c} + mv_{collision}$$

law of conservation of energy

law of conservation of impulse in indirect semiconductor (need phonon mv_{ph}) and QW (collision with well)

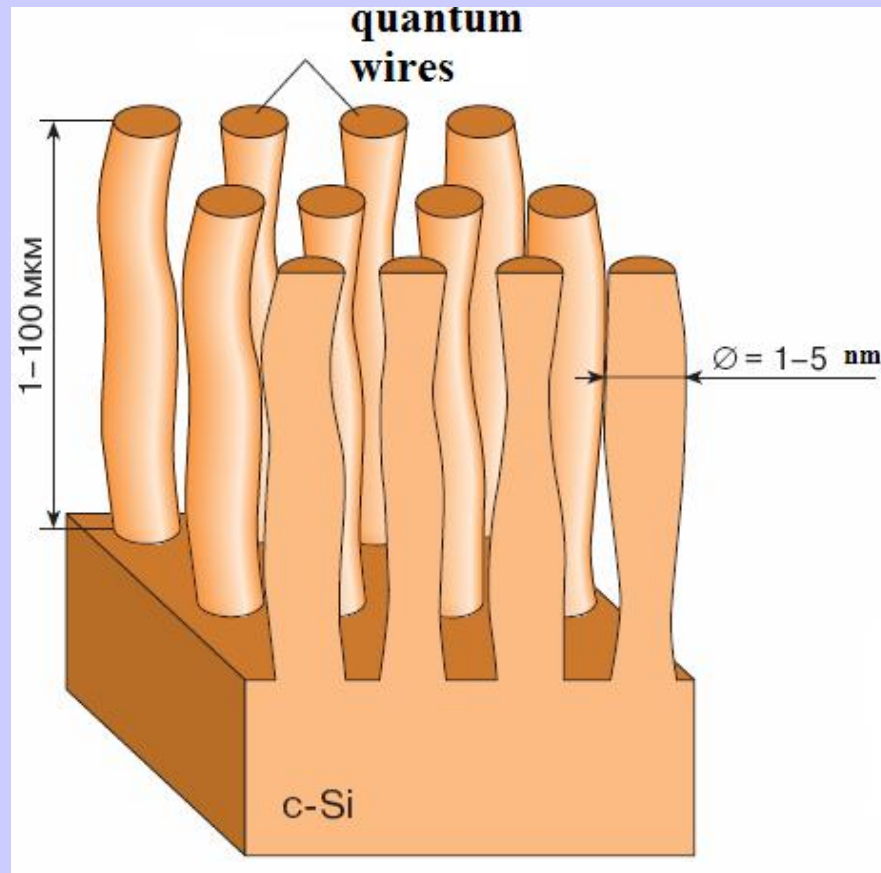
Nomenclature of pores

(International Union of Pure and Applied Chemistry, IUPAC) standard

Micropore, with pore diameters and pore distances ≤ 2 nm.

Mesopores, with geometries in the 2-50 nm region.

Macropores, with geometries in the >50 nm region.



Technology of nano- and Porous Si

Criteria for choice of pore formation methods

Preparation Methods:

High quality
Expensive

lasers, LED, FET,...



Targets

advantages and disadvantages



Low -cost
Nongomogeneous
Mass production

Sensors, hydrogen storage,
explosive materials,...



- Ion implantation
- Low-pressure CVD
- Annealing of induced precipitation from SiO₂ layers
- Laser ablation of Si target
- Laser pyrolysis of silanes



- Electrochemical anodization
- Stain etching

High Si nanotechnologies

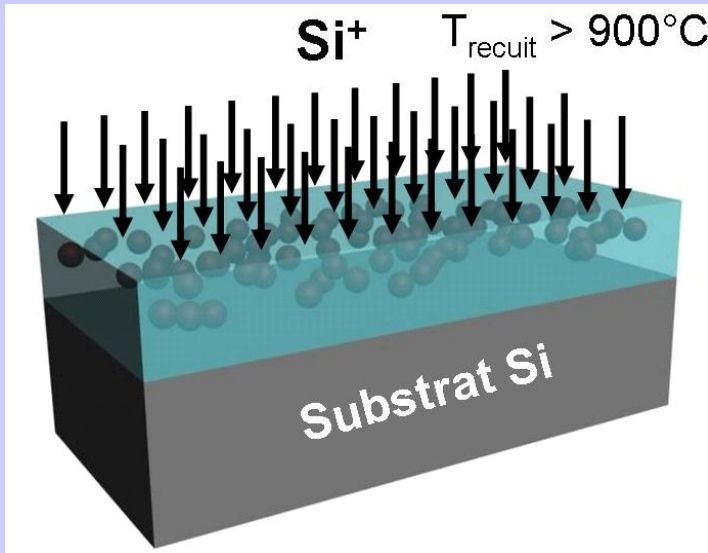


Schéma du processus de fabrication de nanostructures de Si par implantation ionique

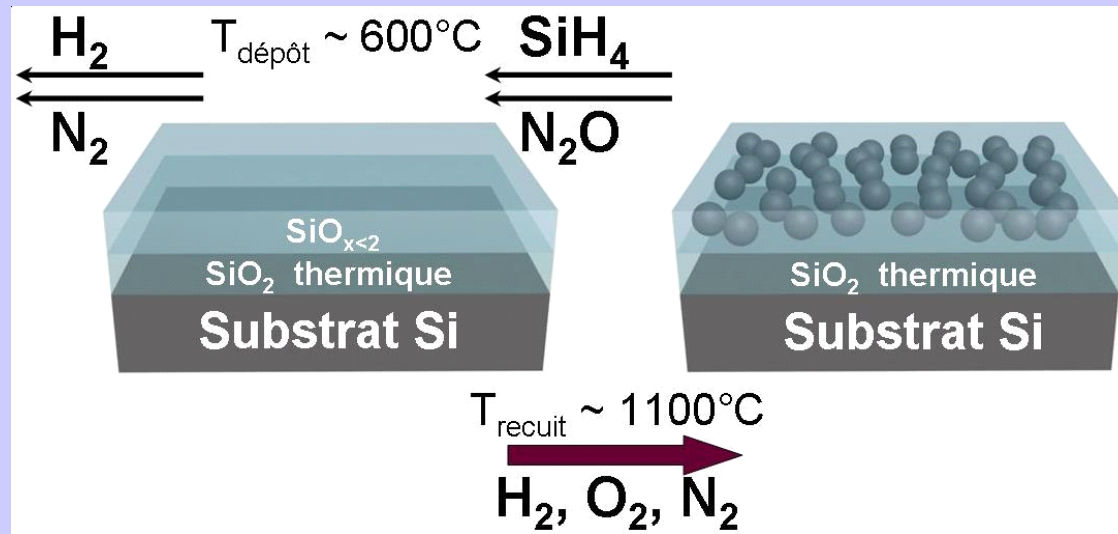
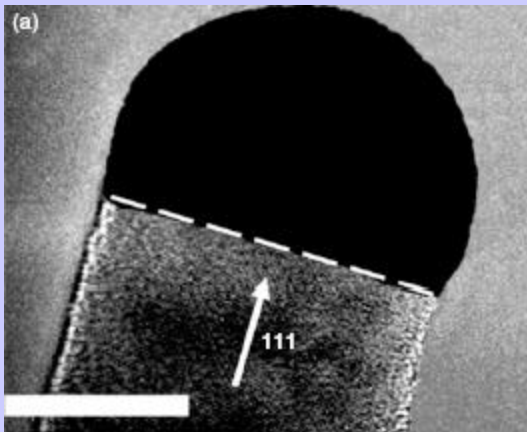
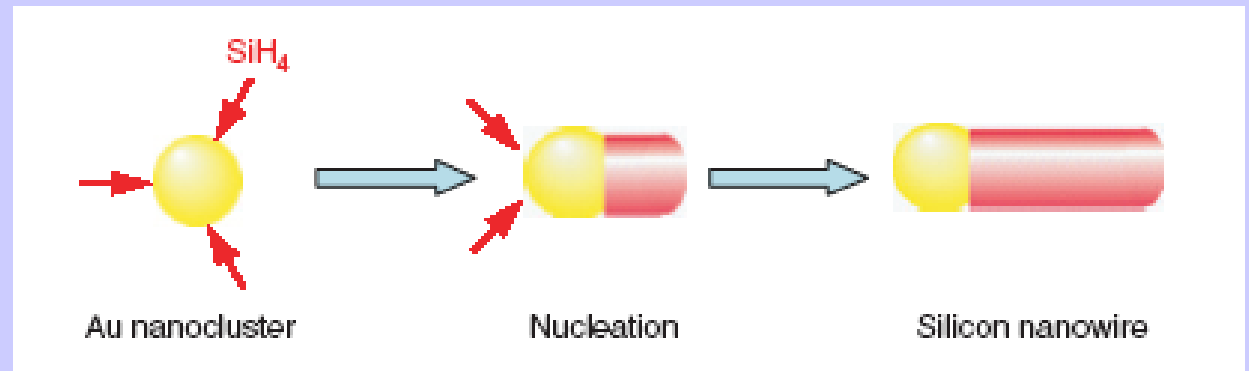


Schéma du processus de fabrication de nanostructures de Si par LPCVD : précipitation dans une couche d'oxyde.



scale bar 20 nm



A nanocluster catalyzed SiNW growth by CVD

High nano Si technologies

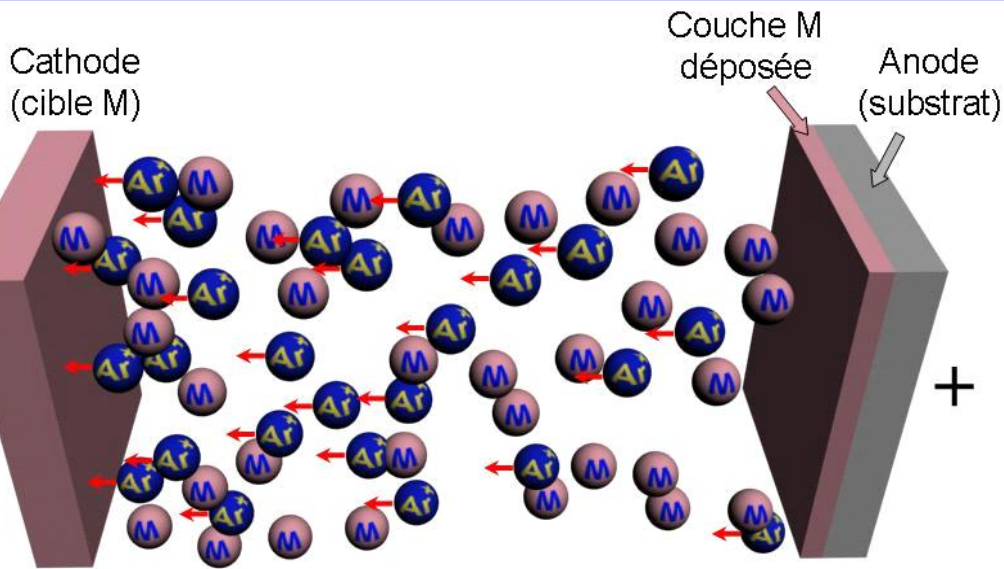


Schéma de principe de la pulvérisation cathodique.

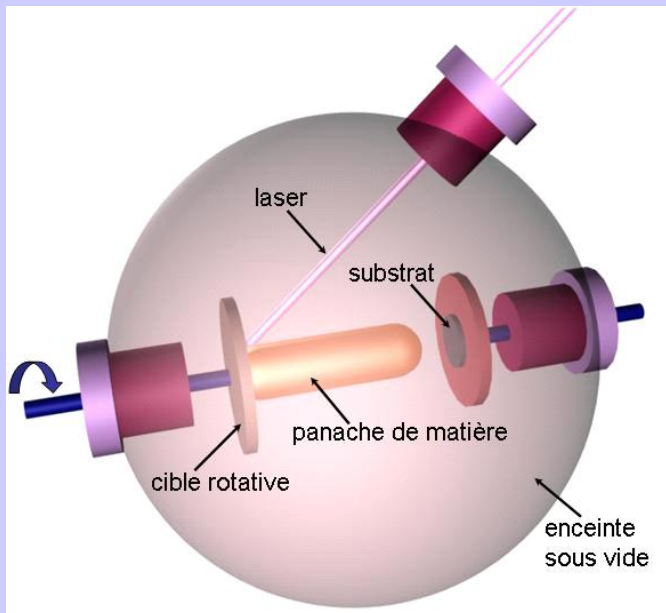


Schéma de principe de l'ablation laser.

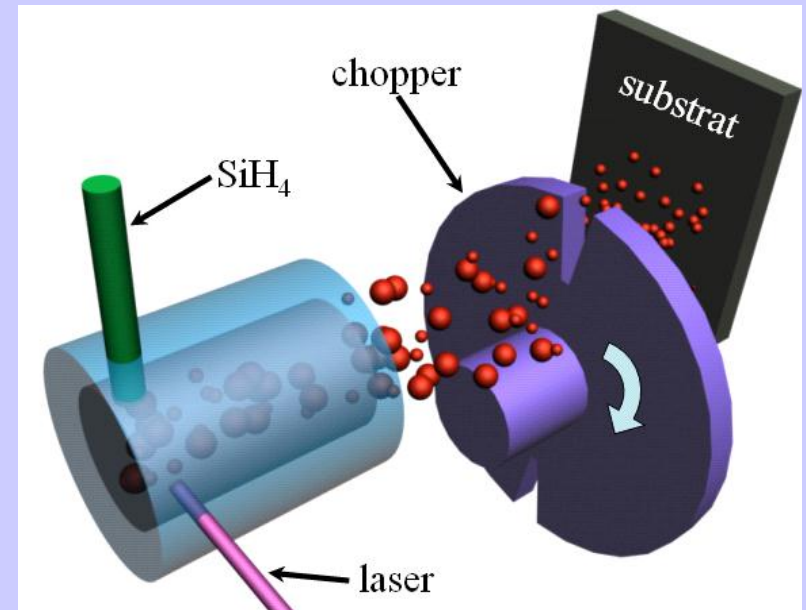


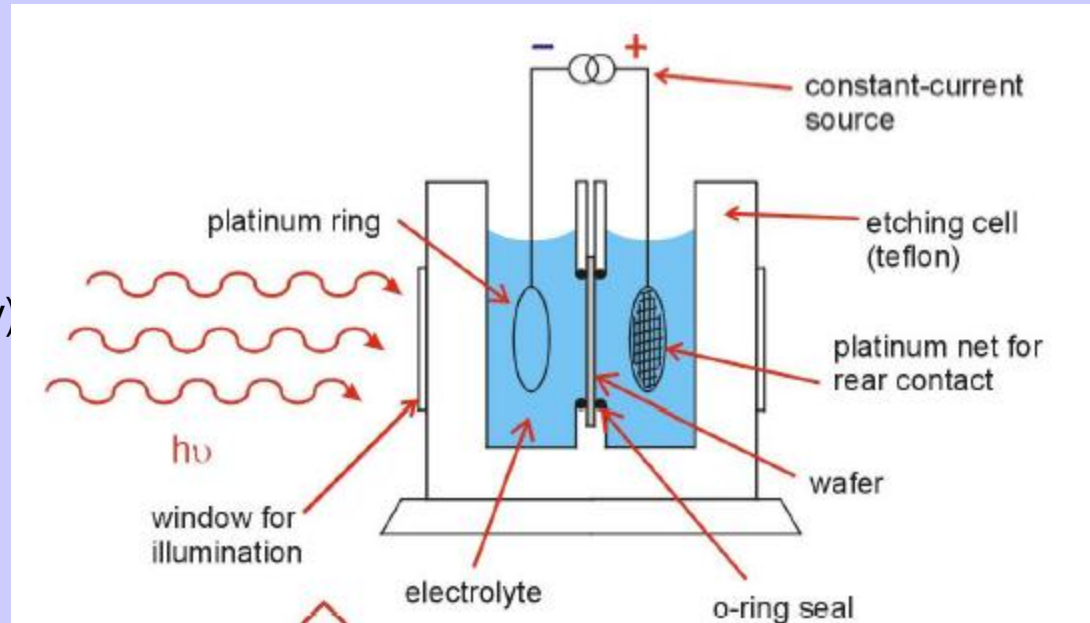
Schéma de principe du pyrolyse laser.

Electrochemical formation

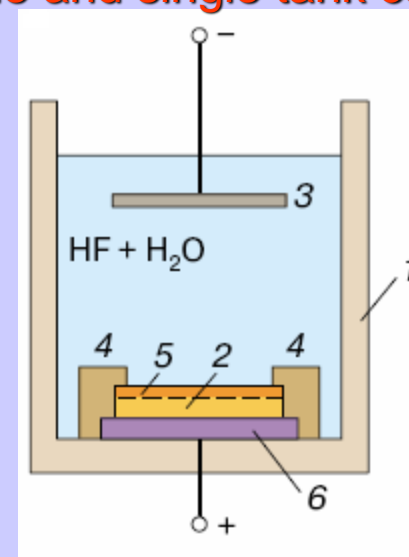
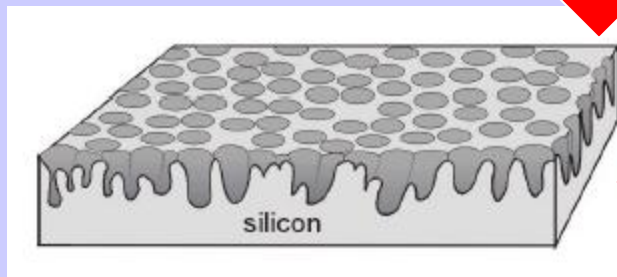
Key parameters:

Si surface- hydrophobic!

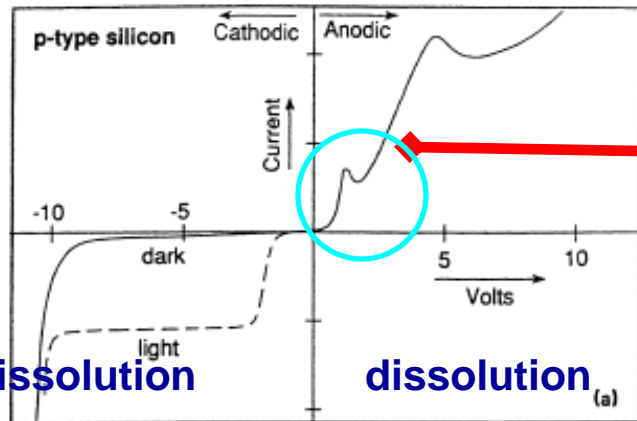
- Electrolyte type (C_2H_5OH for wettability, org. for homogeneity)
- HF concentration (<50%)
- Doping level (n, n+, p, p+)
- Illumination state
- Anodical current (constant I mode=control porosity)
- Cell: H_2 bubble remove!



Double and single tank cells

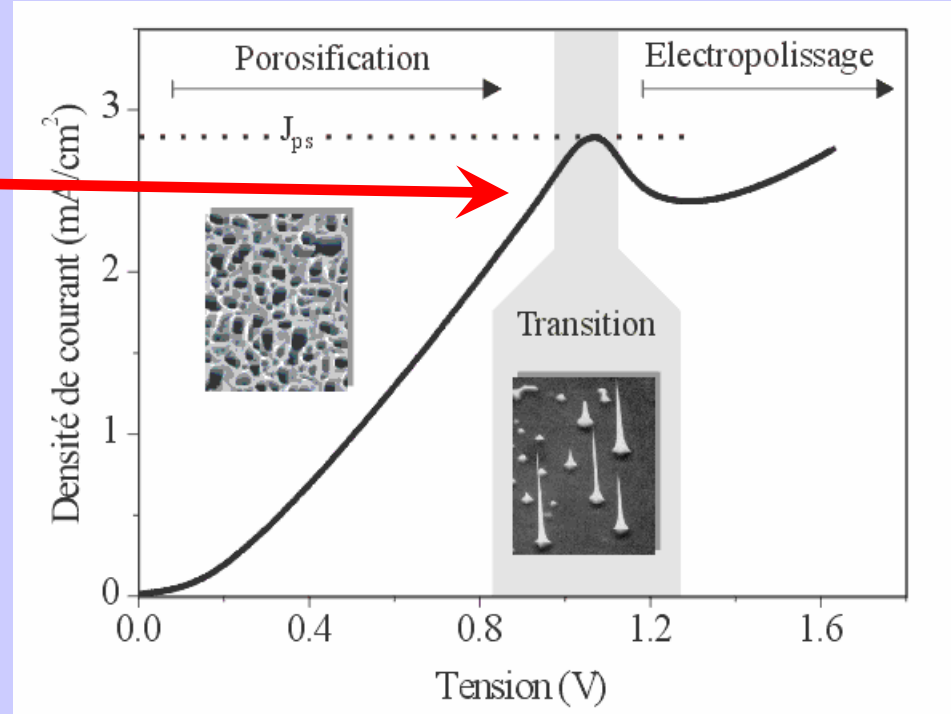
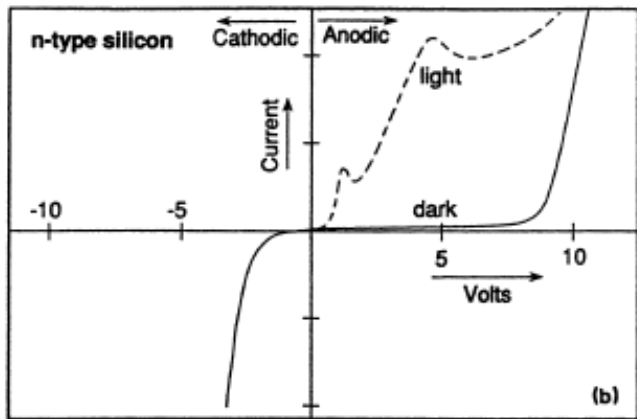


Electrochemical formation



No dissolution

dissolution



$$J = J_0 \left[e^{\frac{eV}{nkT}} - 1 \right]$$

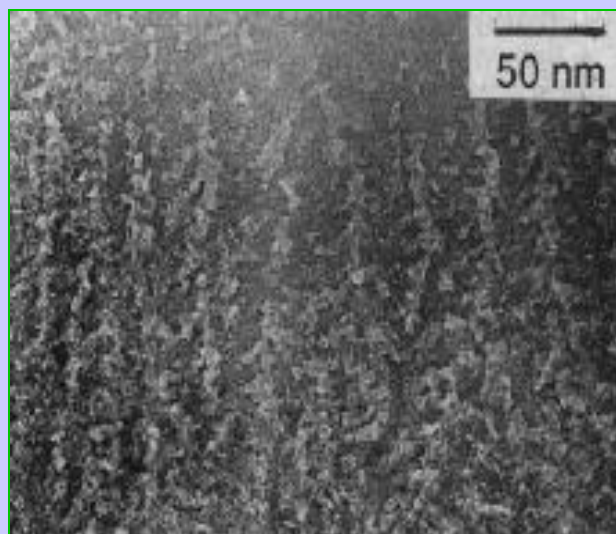
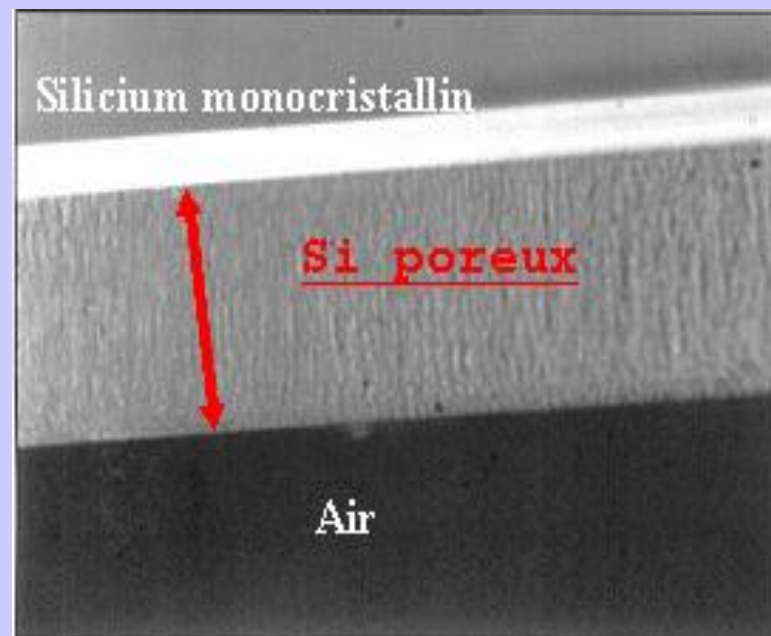
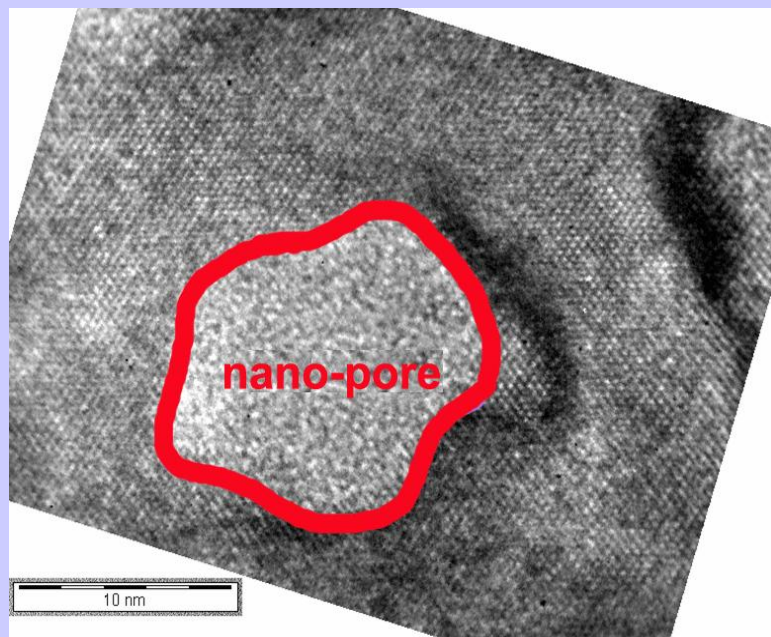
(Schottky diode behavior)

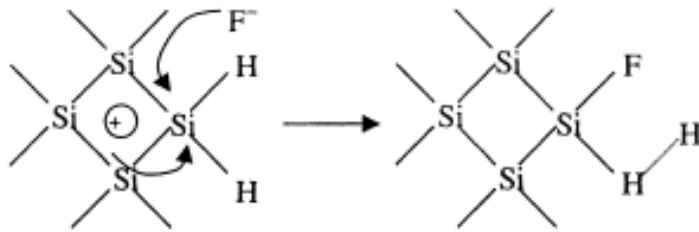
Change from electronic to ionic current
due to specific redox reaction on Si surface

Dissolution chemistry:

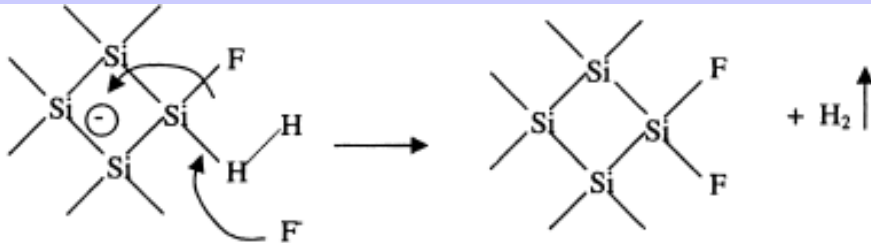


Pore formation domain

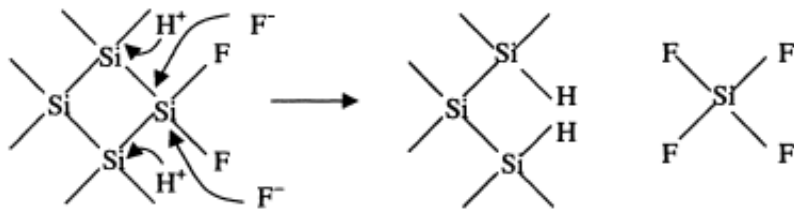




Hole injection and attack on a Si-H bond by a fluoride ion



Second attack by a fluoride ion with hydrogen evolution and electron injection into the substrate



HF attack to the Si-Si backbonds. The remaining Si surface atoms are bonded to the H atoms and a silicon tetrafluoride molecule is produced

Mechanism of Si dissolutions

To dissolve 1 Si atom:
 $2\text{H}^+ + \text{H}_2\text{O}$.

One H_2 molecule forms on the surface

Process of replacing:
 $\text{Si-H} \rightarrow \text{Si-OH} \rightarrow \text{Si-F}$ &
 settling-out of SiF_4

Silicon dissolution scheme, Lehmann and Gosele

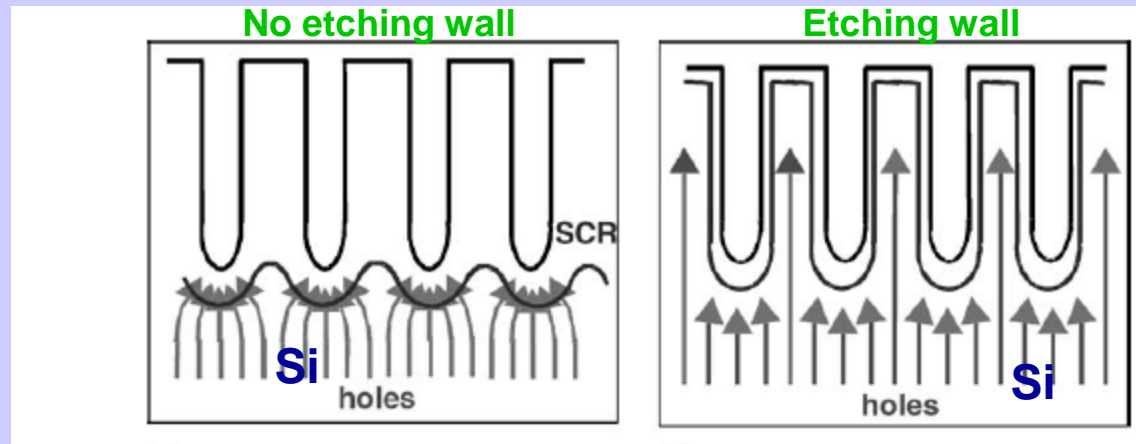
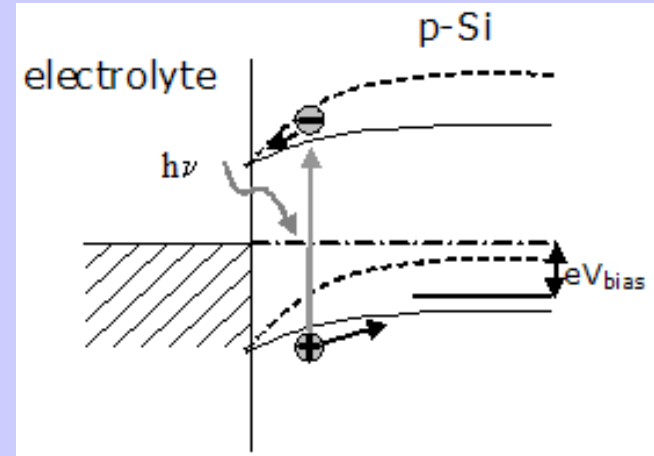


The silicon tetrafluoride reacts with two HF molecules to give H_2SiF_6 and then ionizes.

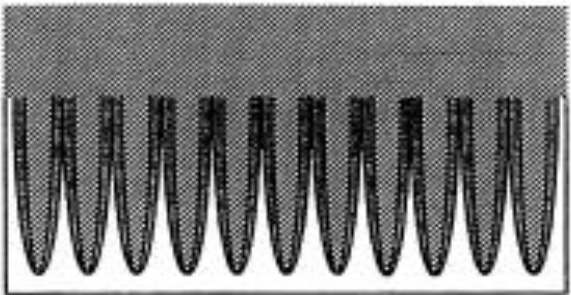
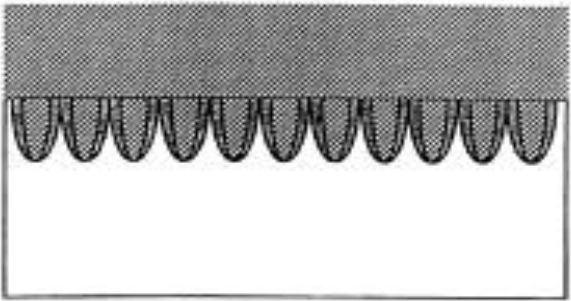
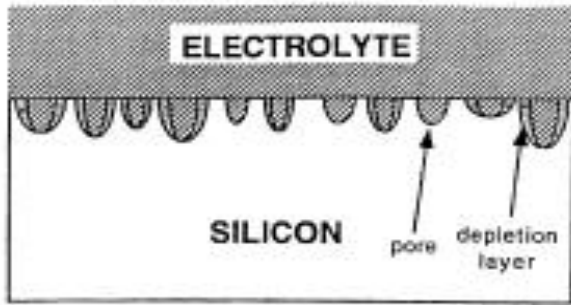
Why pore formation?

- There are initial roughness or pores
- A surface region depleted in mobile carriers at Si/electrolyte interface (Schottky contact).
- The thickness of depleted region depends on doping level.
- The size of pore is related both to the depletion layer and mechanism of charge transfer (breakdown, tunneling, overcome the barrier PS-Si...)

$$x_0 = \sqrt{\frac{2\epsilon_0 e \psi_s}{e^2 N_A}}$$

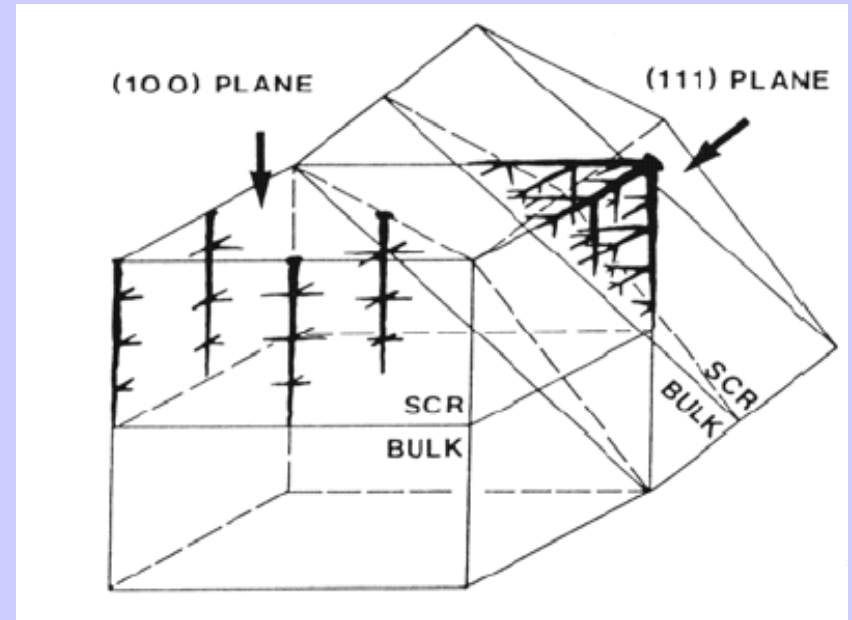
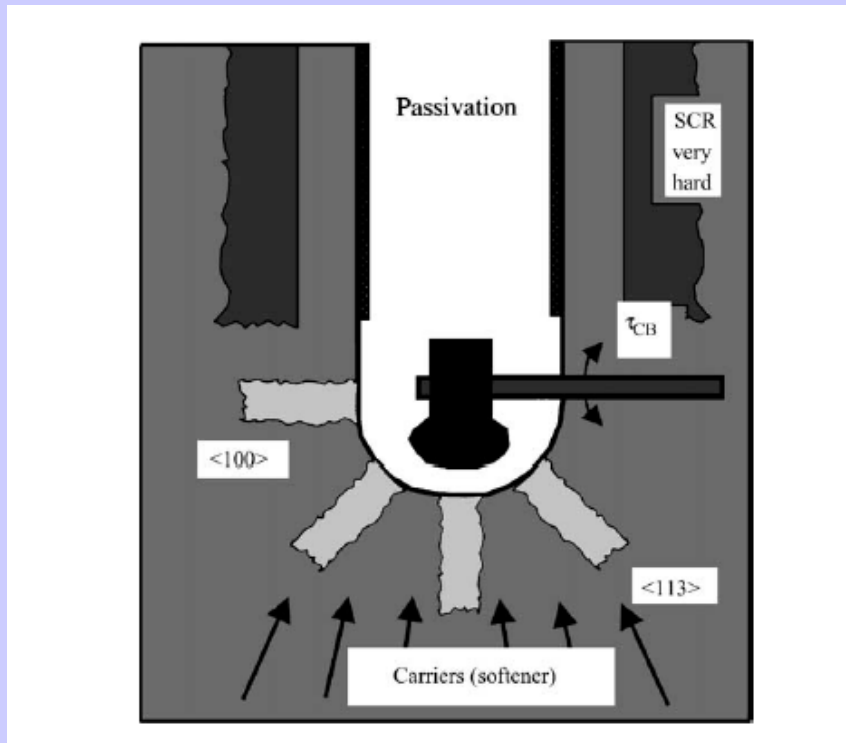


Large SCR and small SCR



Hammer model of pore formation

Si is always removed in patches corresponding to the domain size of system!

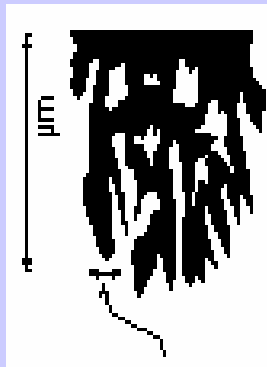


Pore formation region

Nano -porous Si P-type

- « nano - sponge » morphology

- nanocrystallites sizes: **1 - 5 nm**

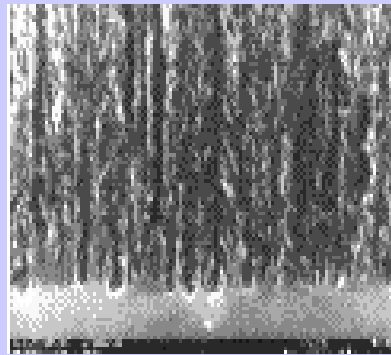


<5 nm

Meso -porous Si P+ -type

- « nano - column » morphology

- column width: **5 - 20 nm**



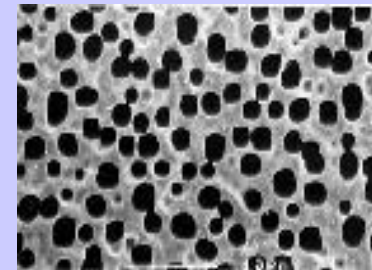
5 nm

Macro -porous Si N-type + light

- « nano - wells » morphology

- inter - well space: **0.1 - 1 μm**

Top view

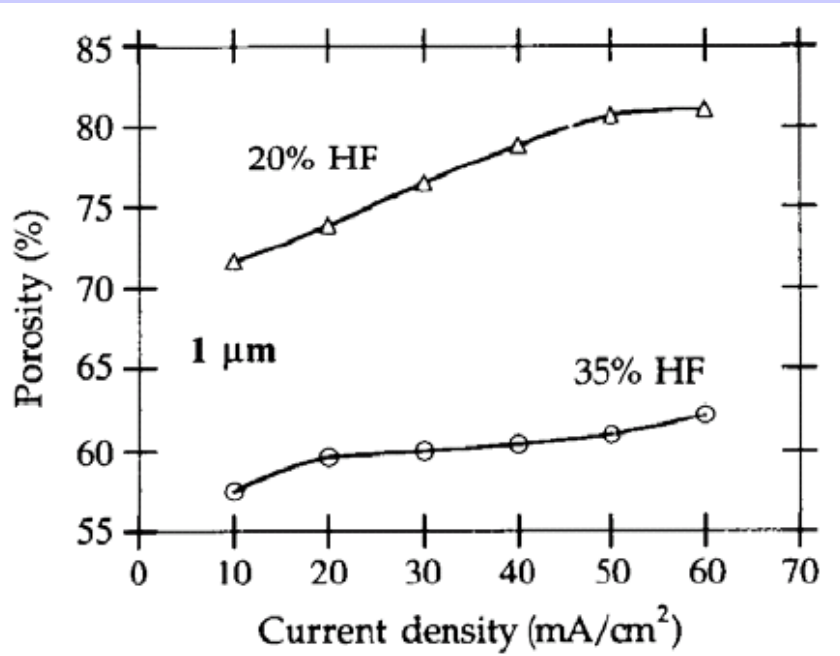


Cross -section

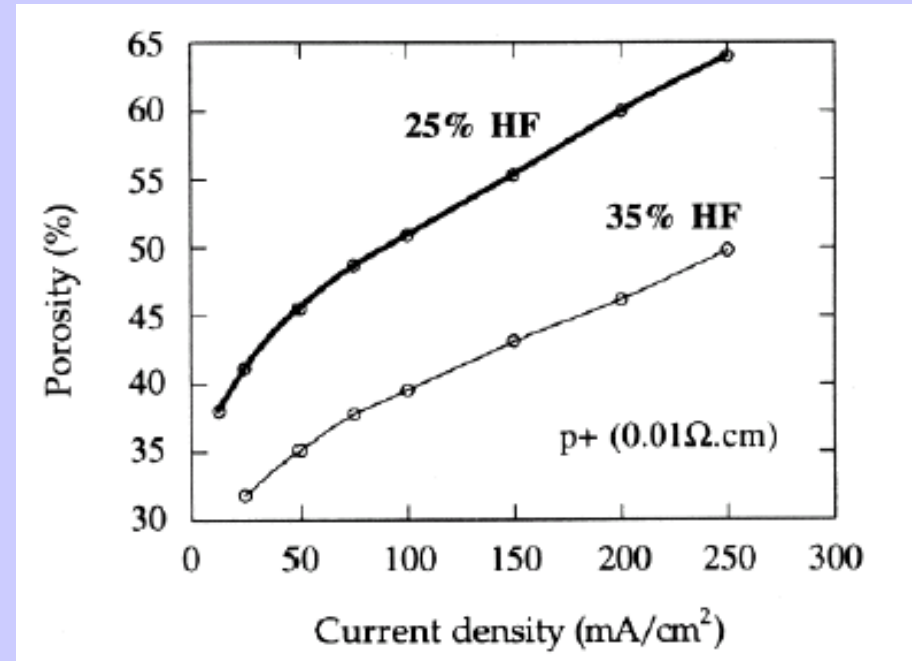


Porosity

Nano-porous Si P-type



Meso-porous Si P+-type

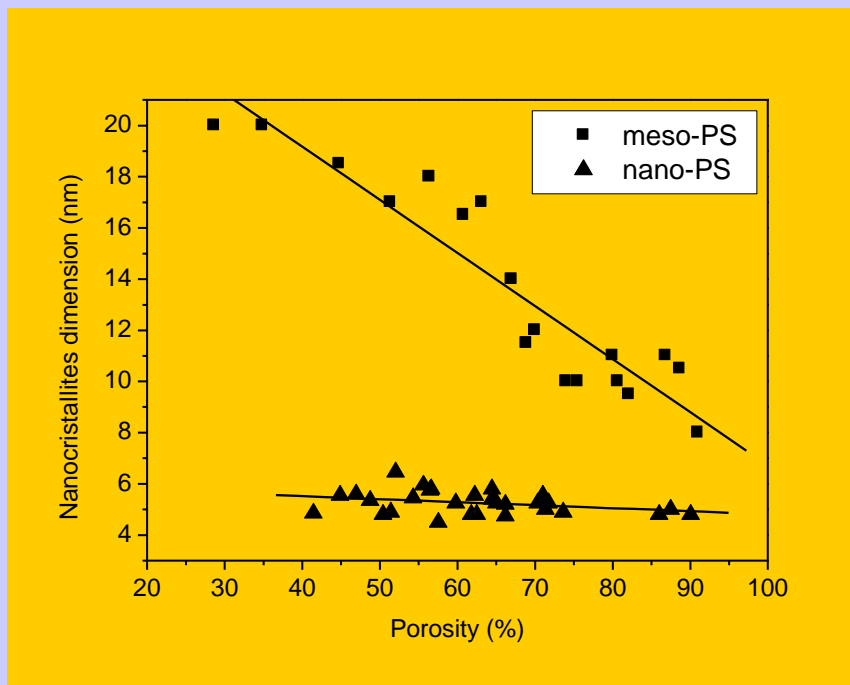


Porosity

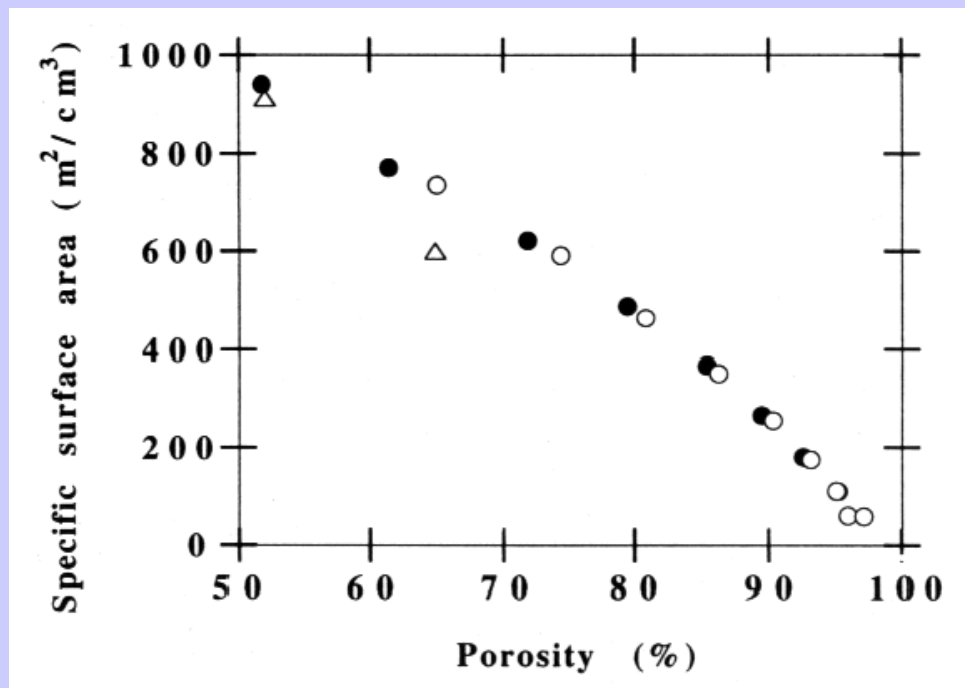
$$P = \frac{V_{pore}}{V_{pore} + V_{Si}} = \frac{m_1 - m_2}{m_1 - m_3}$$

m_1 - weight before anodization, m_2 - after, m_3 - after rapid dissolution of PS in KOH

Porosity, particles dimension, specific surface



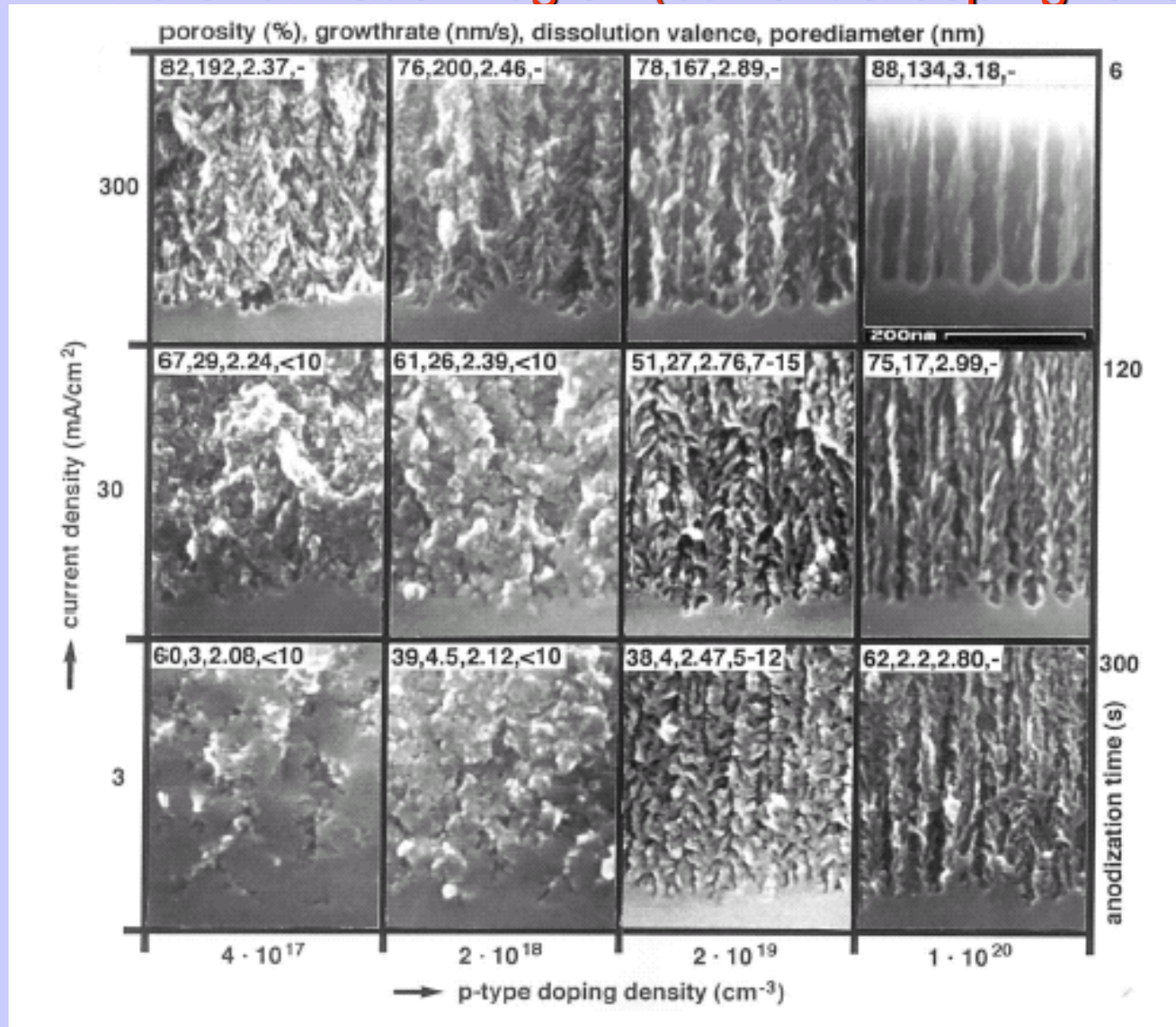
Particle dimension vs Porosity



Specific surface

Nano-PS (sponge type)
meso-PS (column type)

Pore formation region (current & doping level)



Macropores

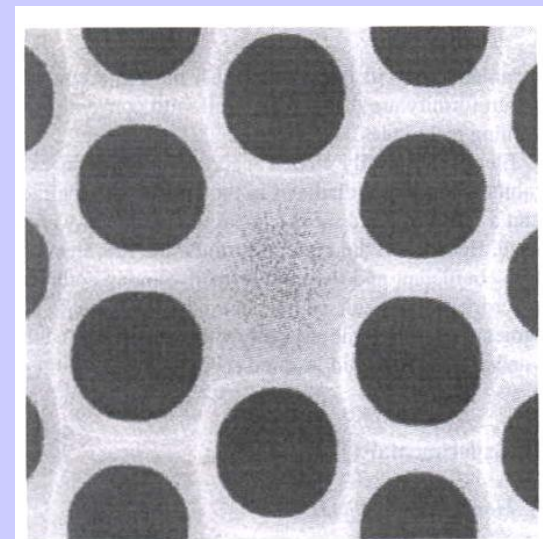
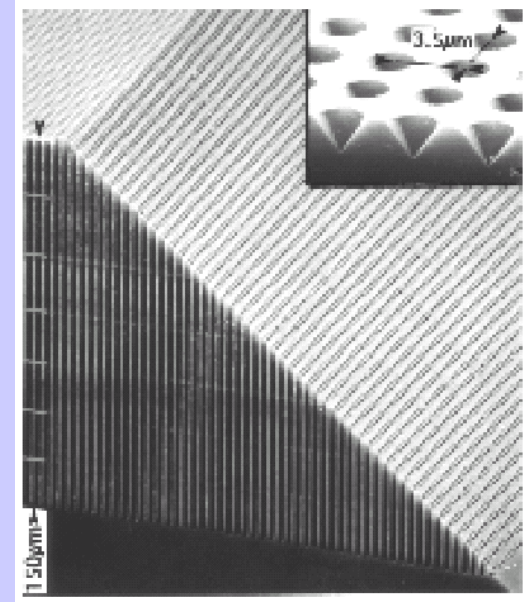
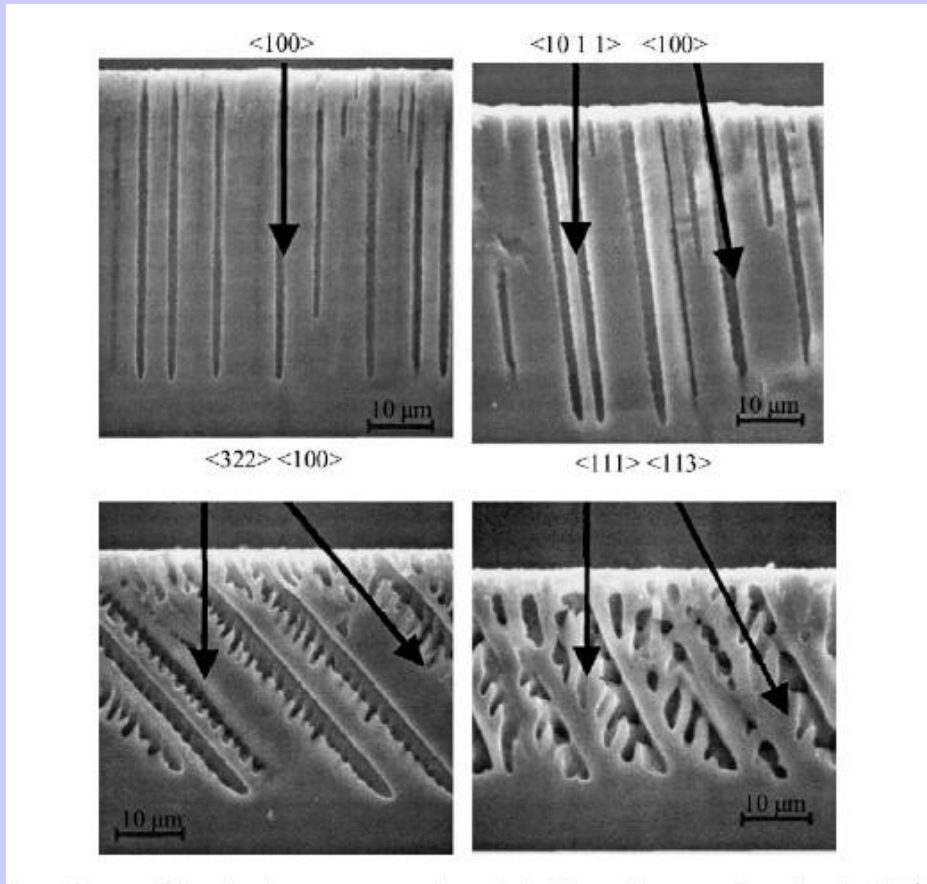
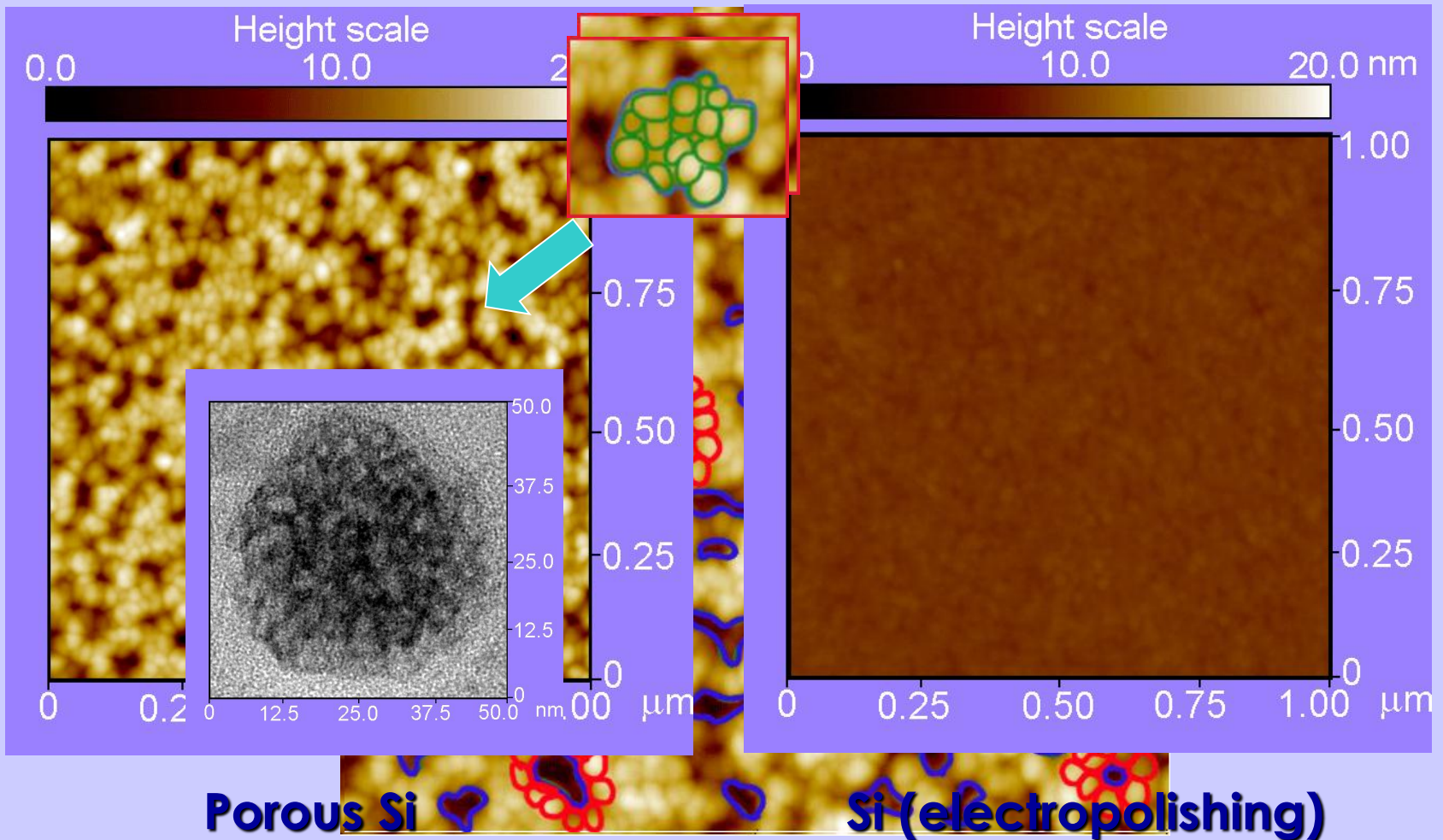
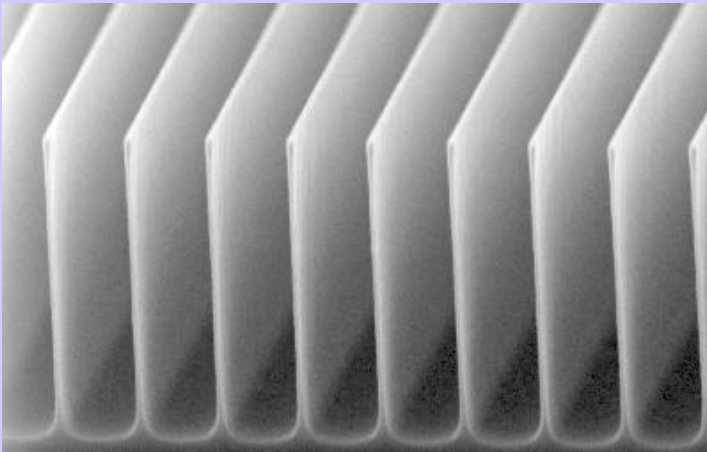


Figure 1. SEM image of the region around a missing etch pit after electrochemical pore growth and subsequent pore widening by oxidation/etching steps. The distance between the pores is 1.5 μm, pore diameters are 1.15 μm.

Nano-porous nanostructures

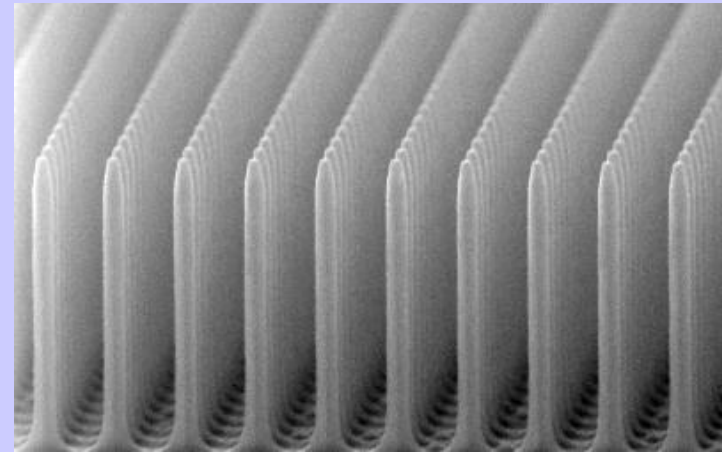


Transient anodization regime



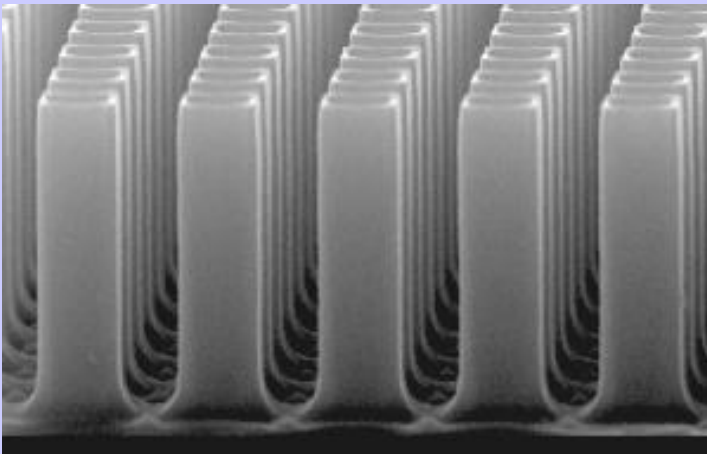
Réseau de Murs

Période $1.6 \mu\text{m}$; Largeur 110 nm ; hauteur $7 \mu\text{m}$



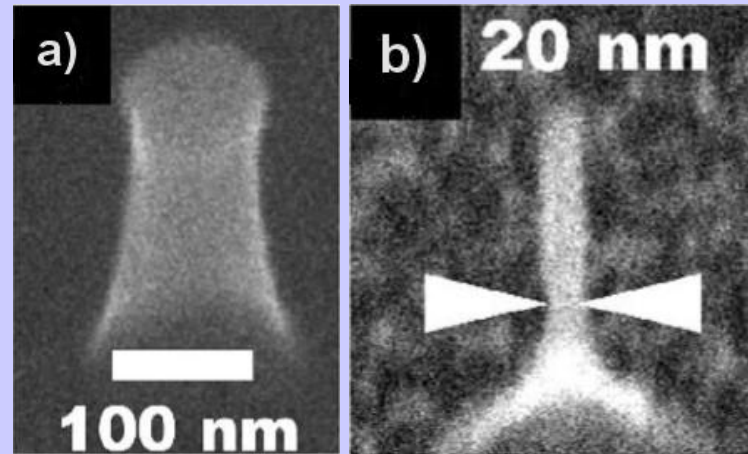
Réseau de Piliers

Période $1.6 \mu\text{m}$; Largeur 450 nm ; hauteur $7 \mu\text{m}$



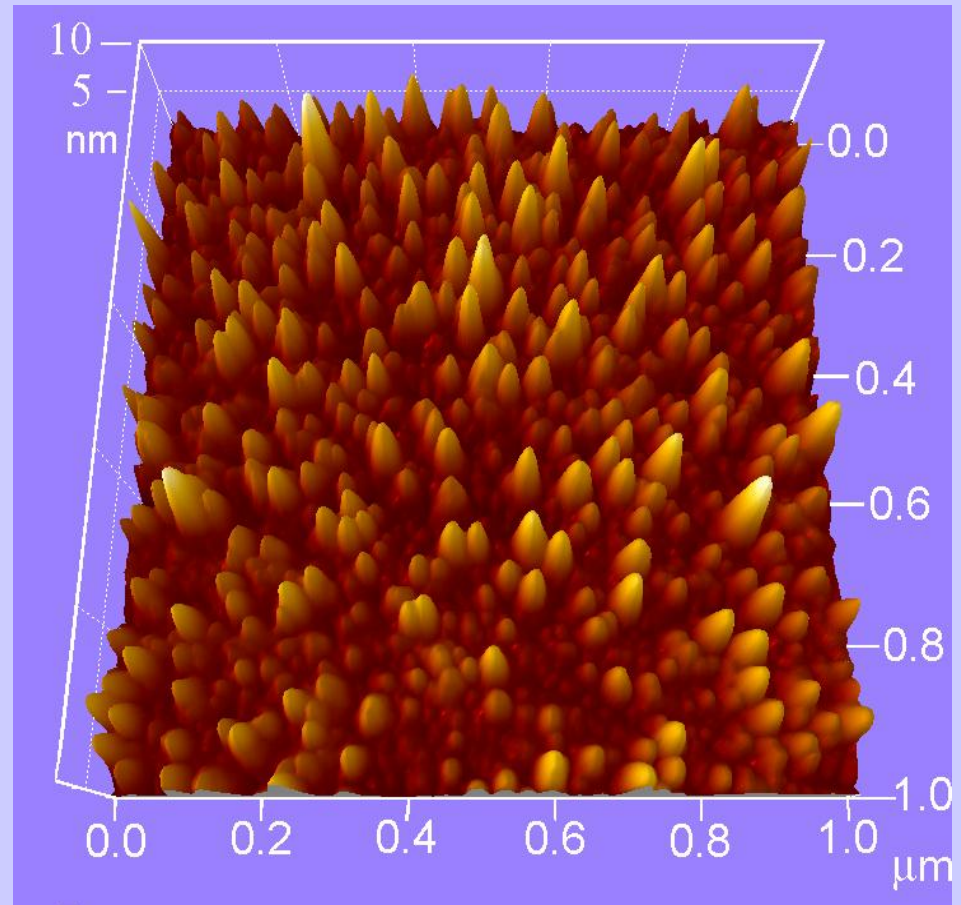
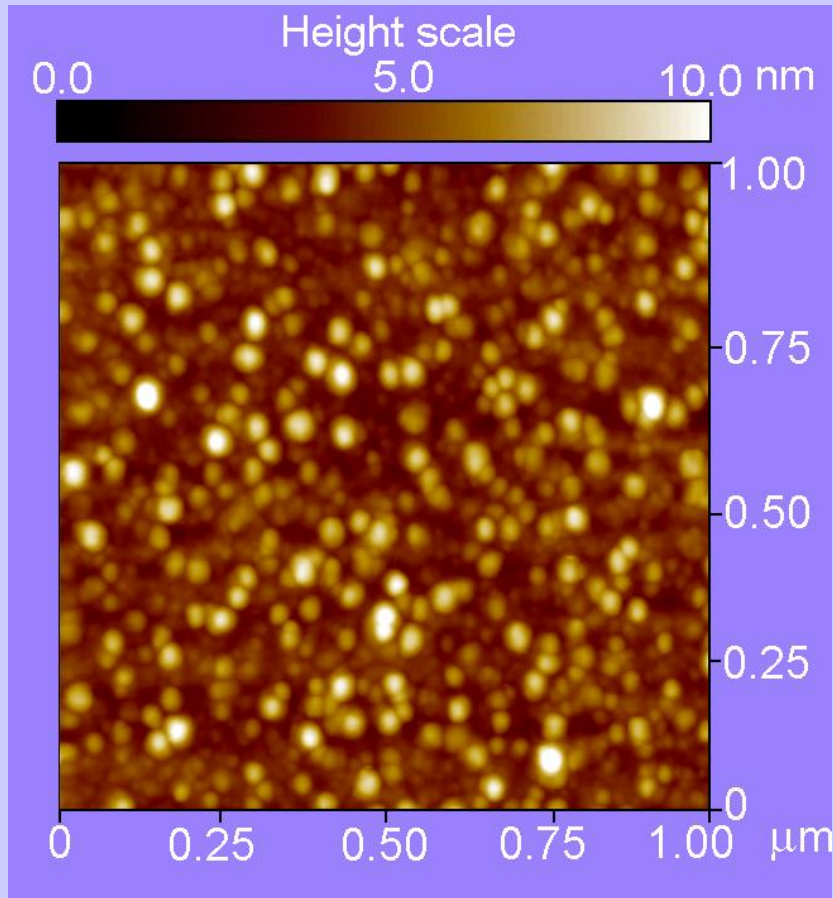
Réseau de Tubes

Période $3.2 \mu\text{m}$; Murs 220 nm ; hauteur $7 \mu\text{m}$

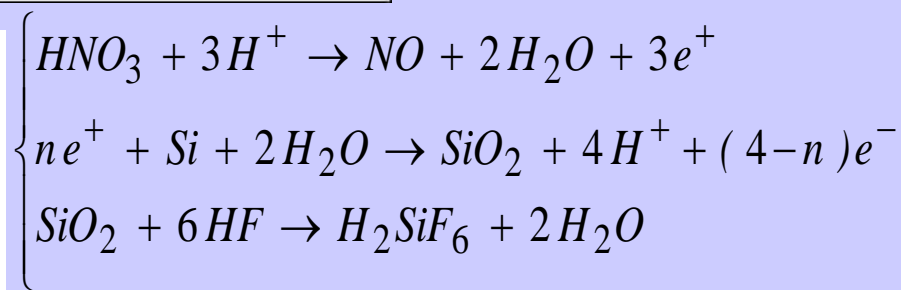
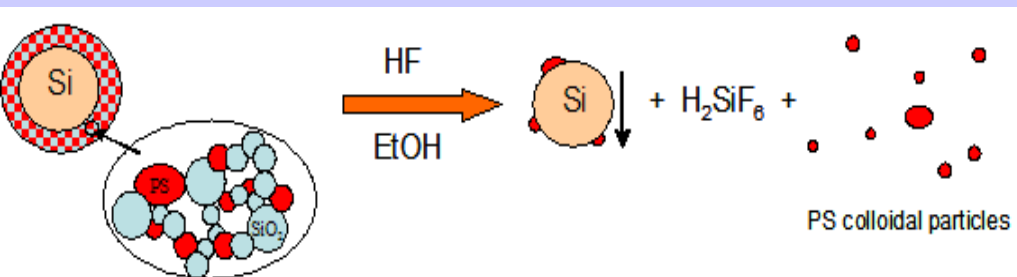
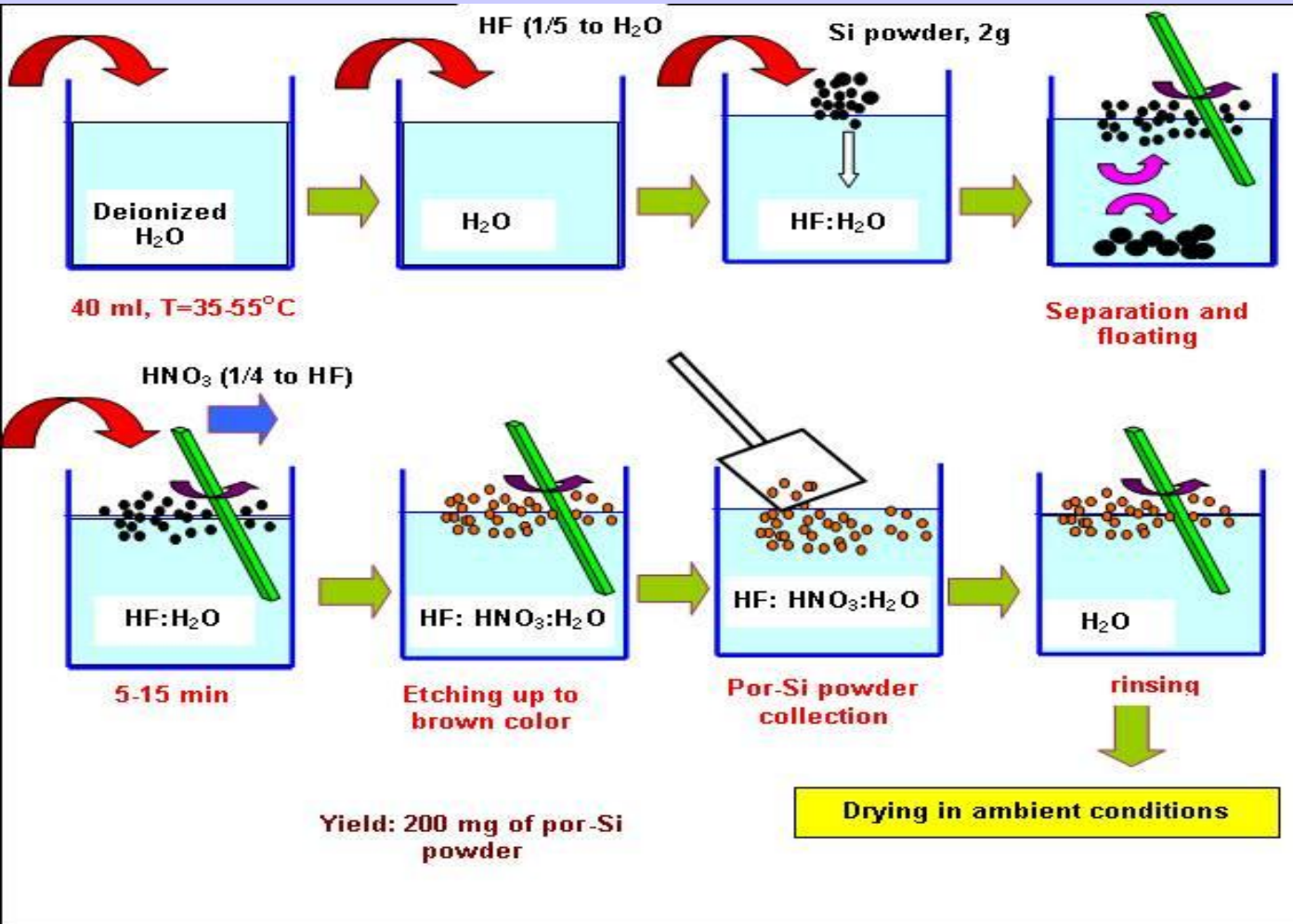


a) Pilier obtenu par gravure plasma puis b) aminci par gravure électrochimique

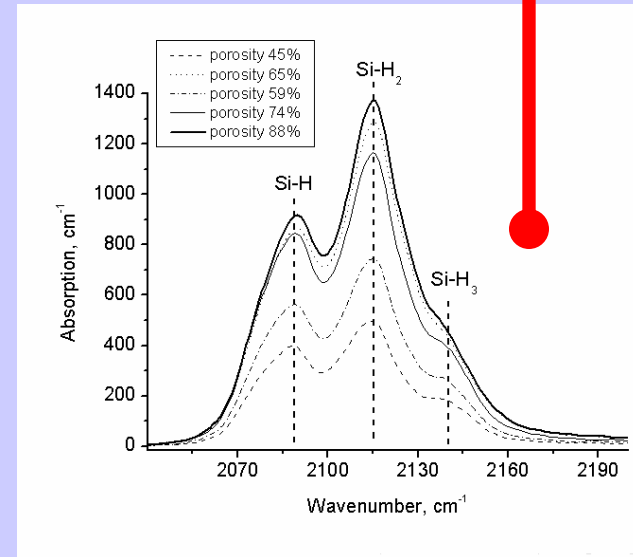
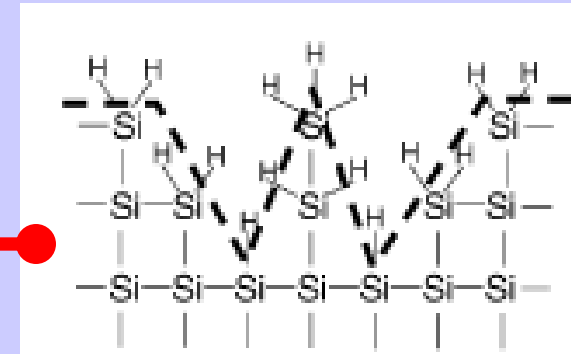
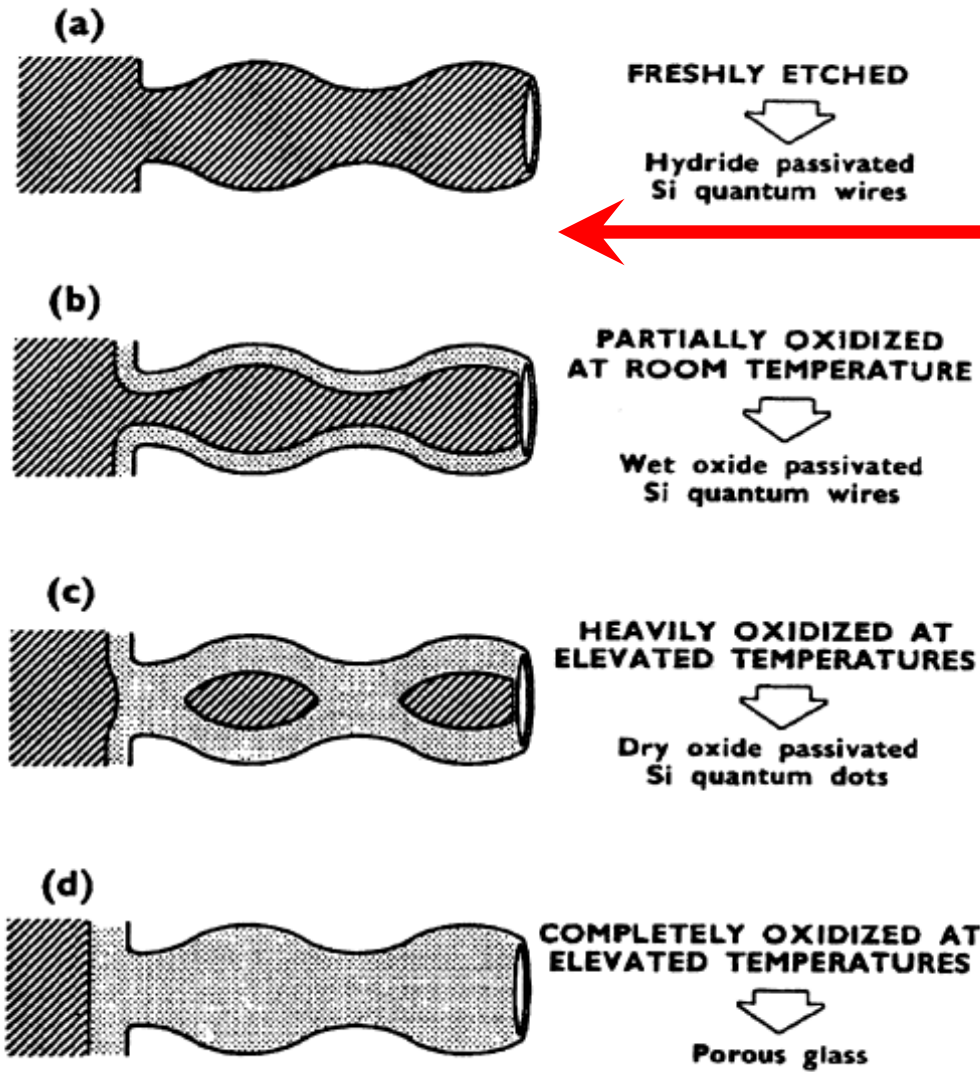
Time-resolved transient anodization regime: nanoparticle formation



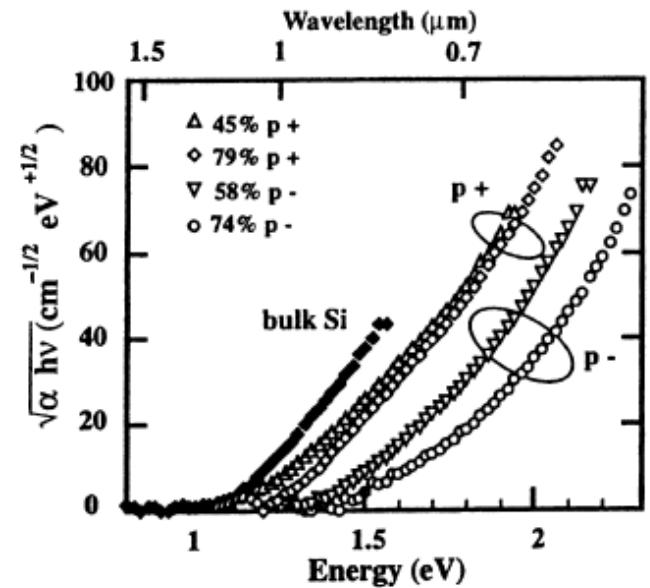
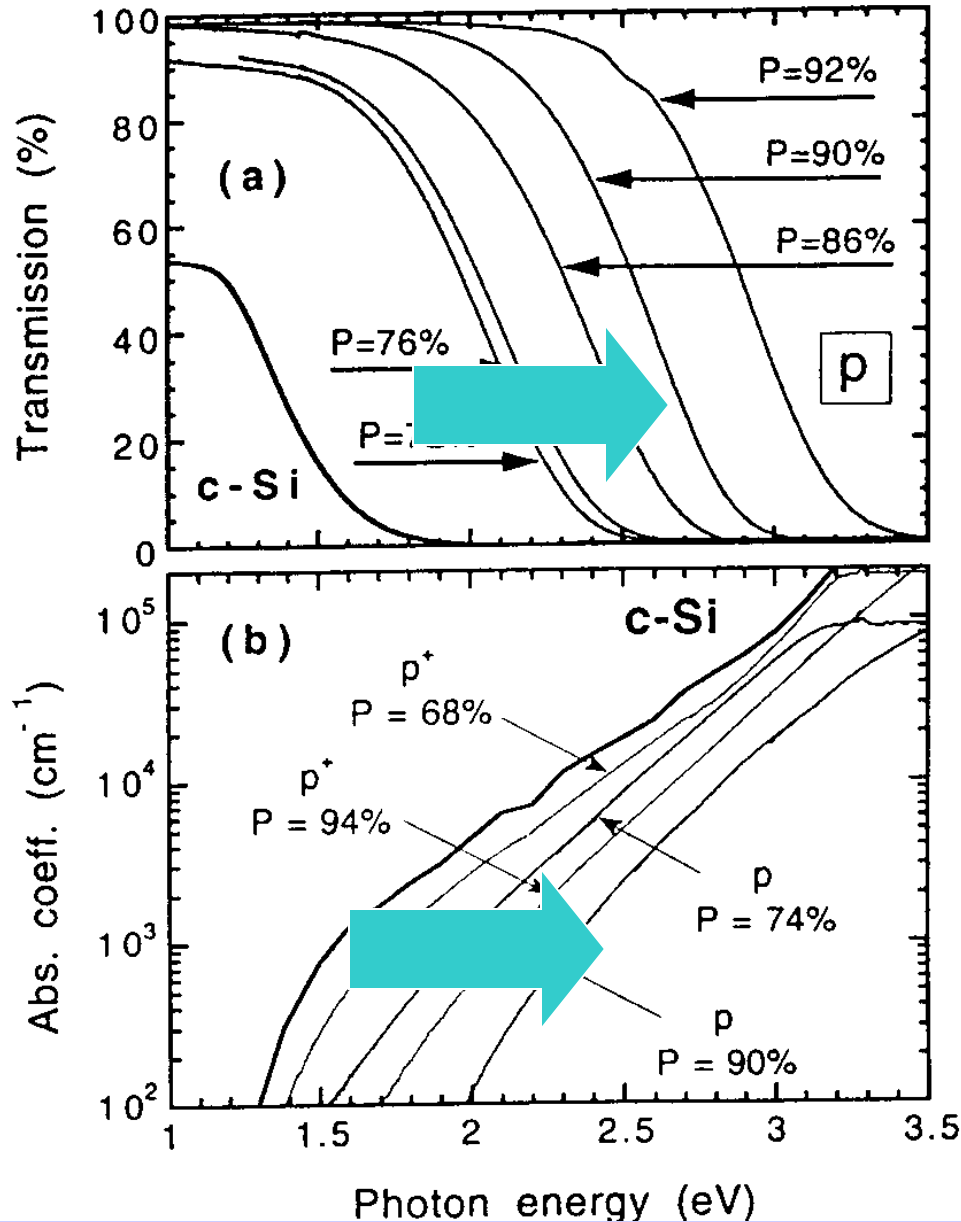
Stain etching of Si powder: method



Idealized schematic steps in the oxidation process of highly PS



Optical properties of nano-porous Si

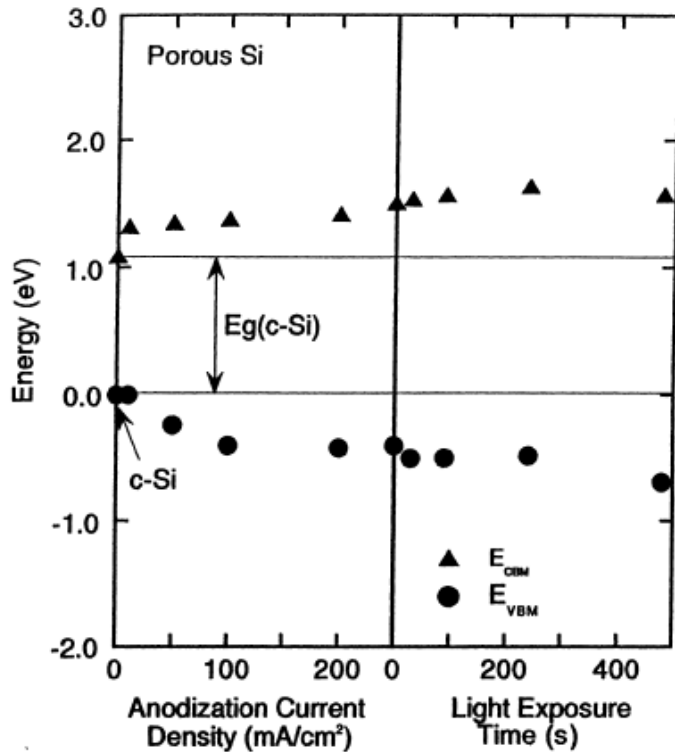


Square root of the absorption coefficient times photon energy vs photon energy

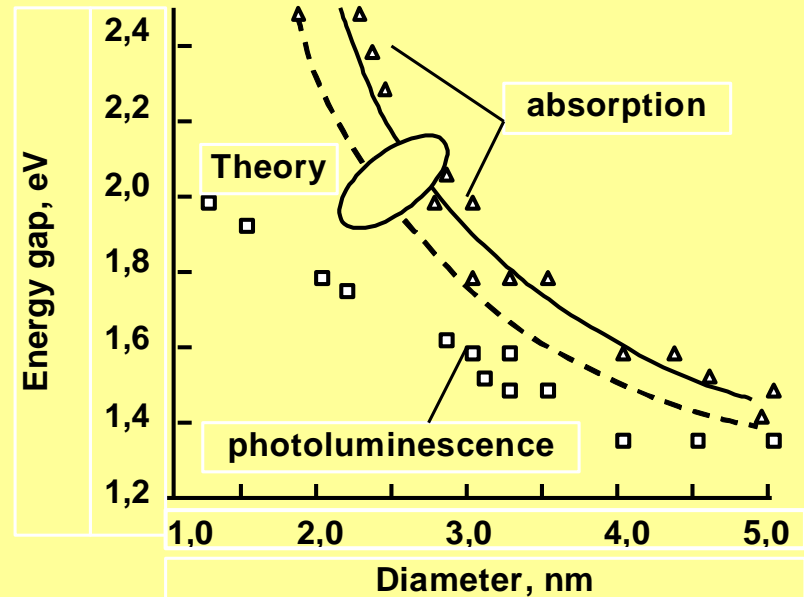
$$\alpha = (h\nu - E_g \pm E_{ph})^2$$

/P.M.Fauchet, In: "Properties of porous silicon", ed.L.Canham, Emis, N18, 1997

Energy band of nano-porous Si

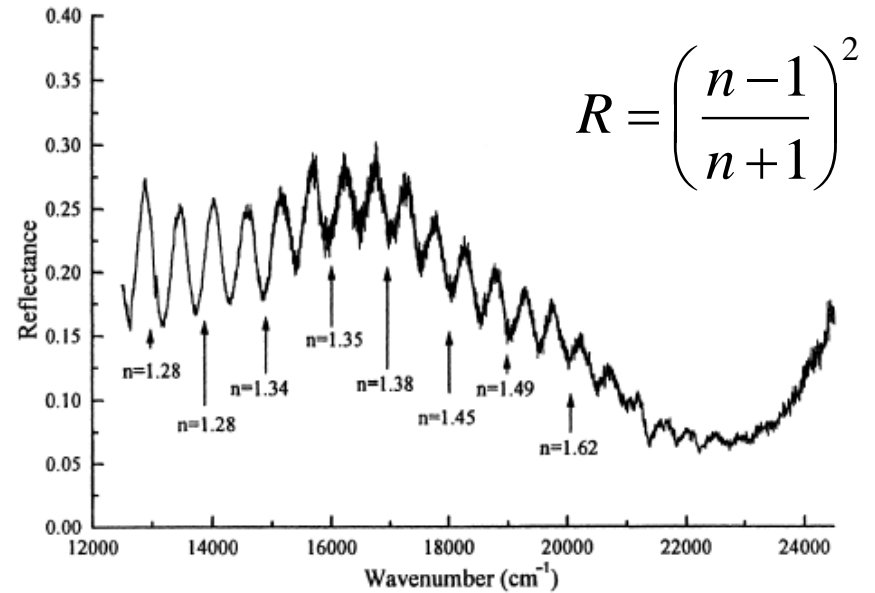
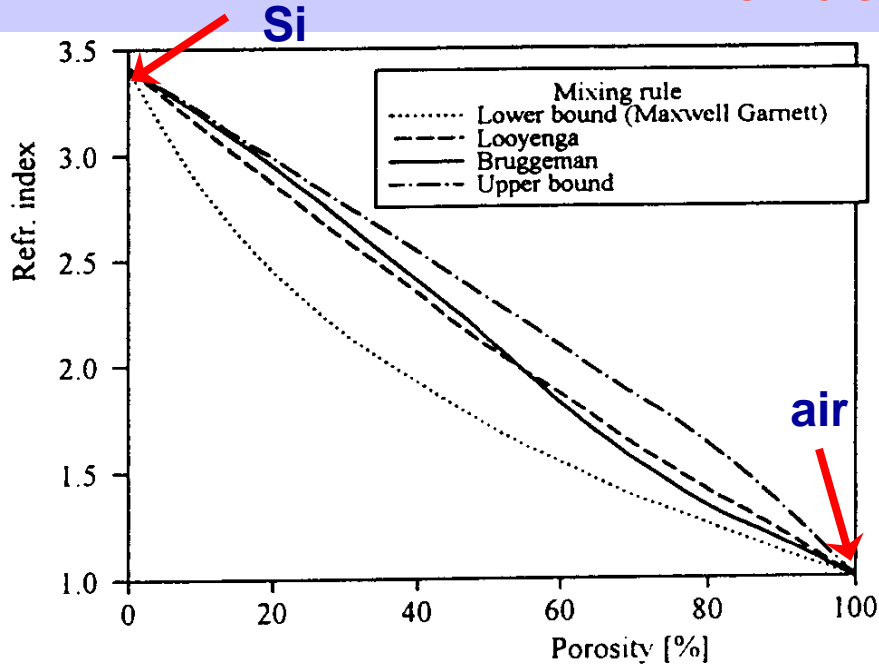


Energy position of c-band minimum and v-band maximum vs anodization current



Energy band gap vs diameters of Si particles

Refractive index



Bruggeman effective medium approximation

$$P \left(\frac{1 - \hat{\varepsilon}}{1 + 2\hat{\varepsilon}} \right) + (1 - P) \left(\frac{\hat{\varepsilon}_{Si} - \hat{\varepsilon}}{\hat{\varepsilon}_{Si} + 2\hat{\varepsilon}} \right) = 0$$

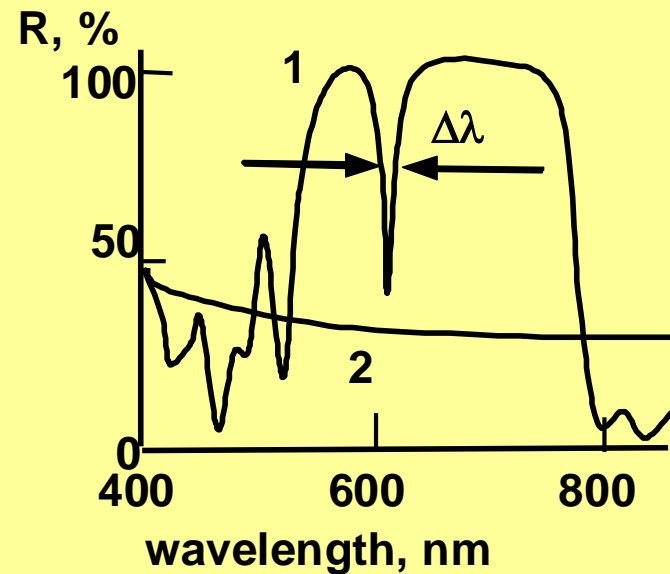
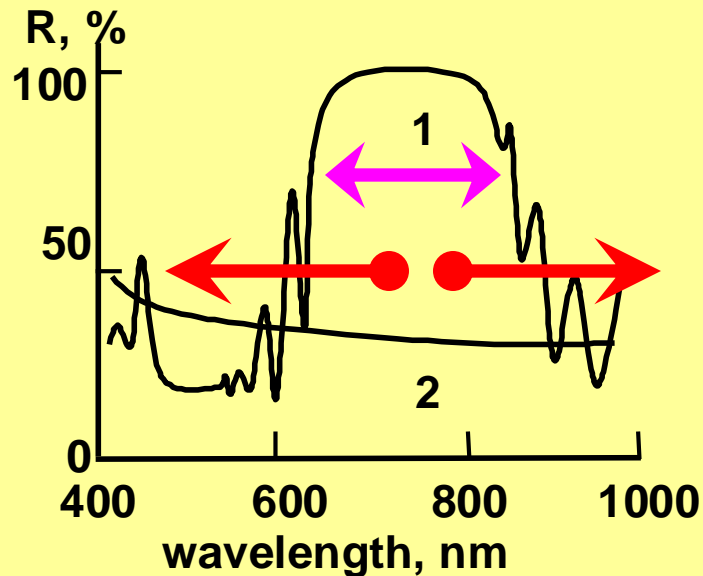
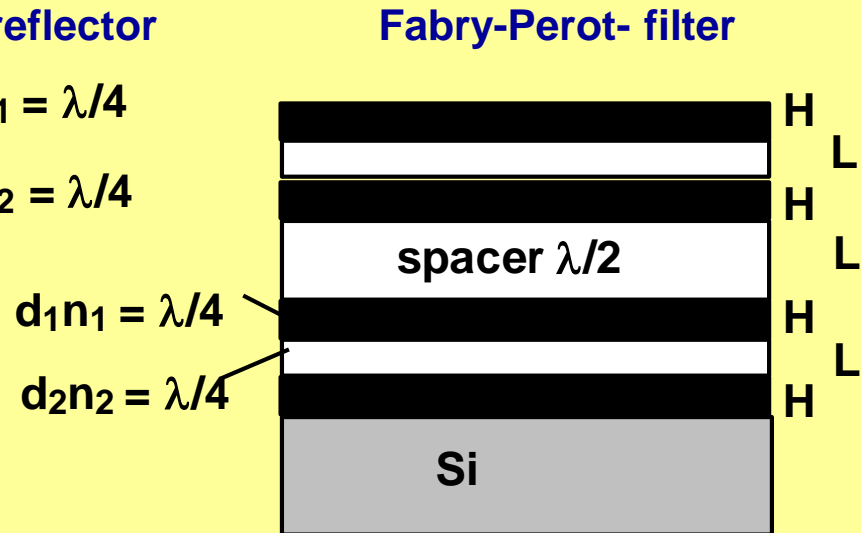
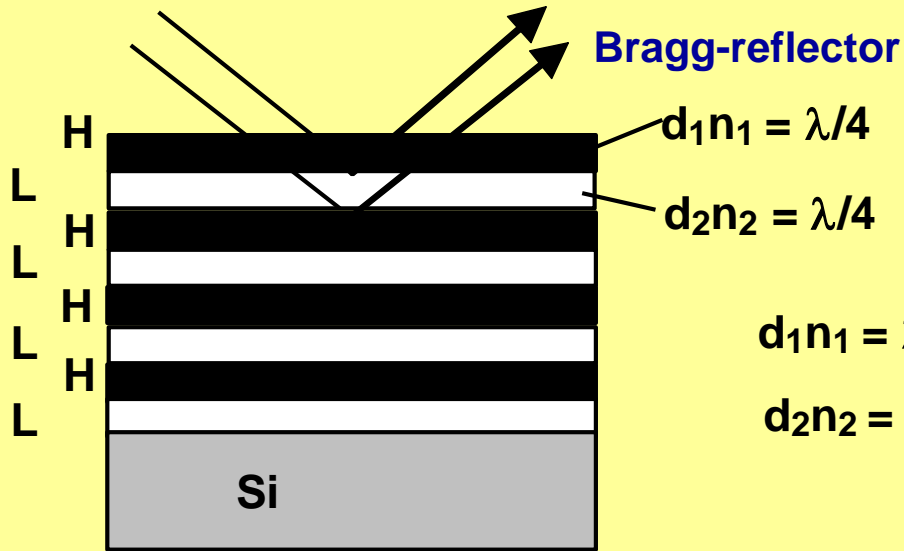
$$\hat{n} = \sqrt{\hat{\varepsilon}} \quad \hat{\varepsilon} = \varepsilon_1 + i\varepsilon_2$$

$$P = \frac{V_{pore}}{V_{pore} + V_{Si}}$$

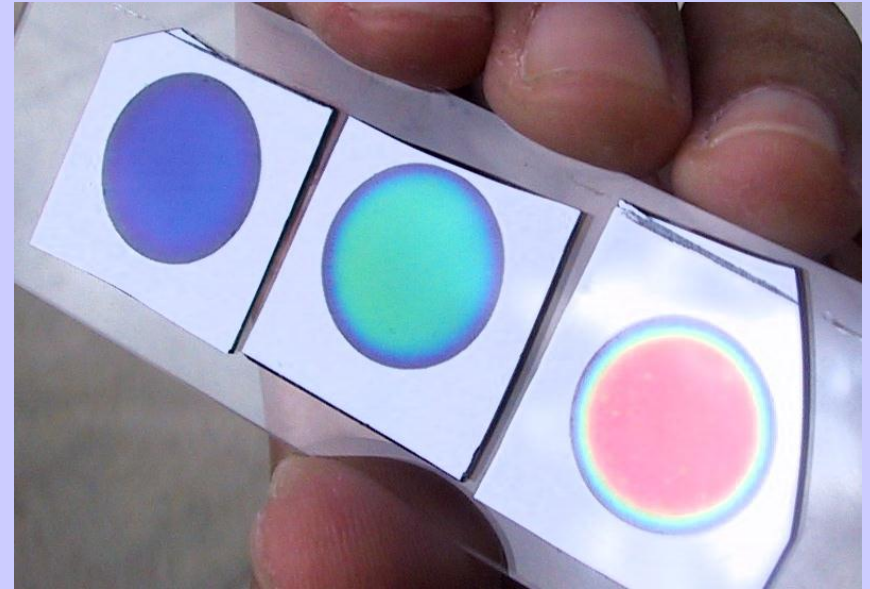
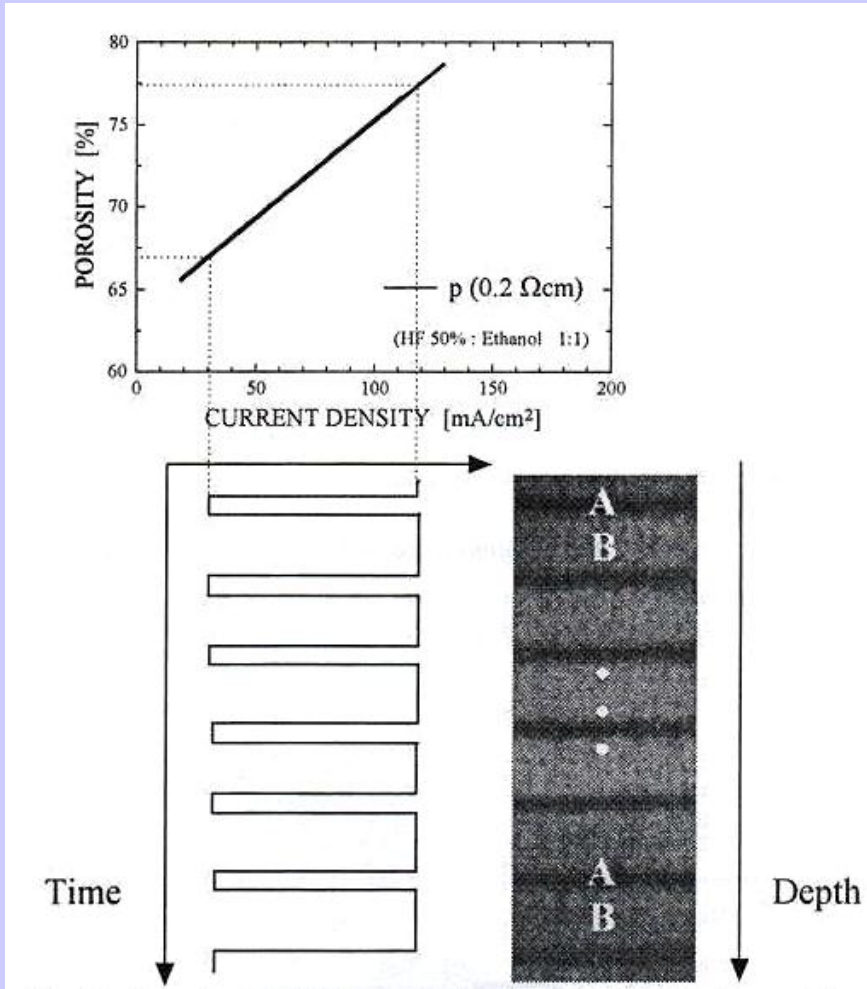
$$\varepsilon = (1 - P)\varepsilon_{Si} + P\varepsilon_{air}$$

$$n = \frac{1}{2d} \left(\frac{1}{\lambda_k} - \frac{1}{\lambda_{k+1}} \right)^{-1}$$

Optical multi-structures



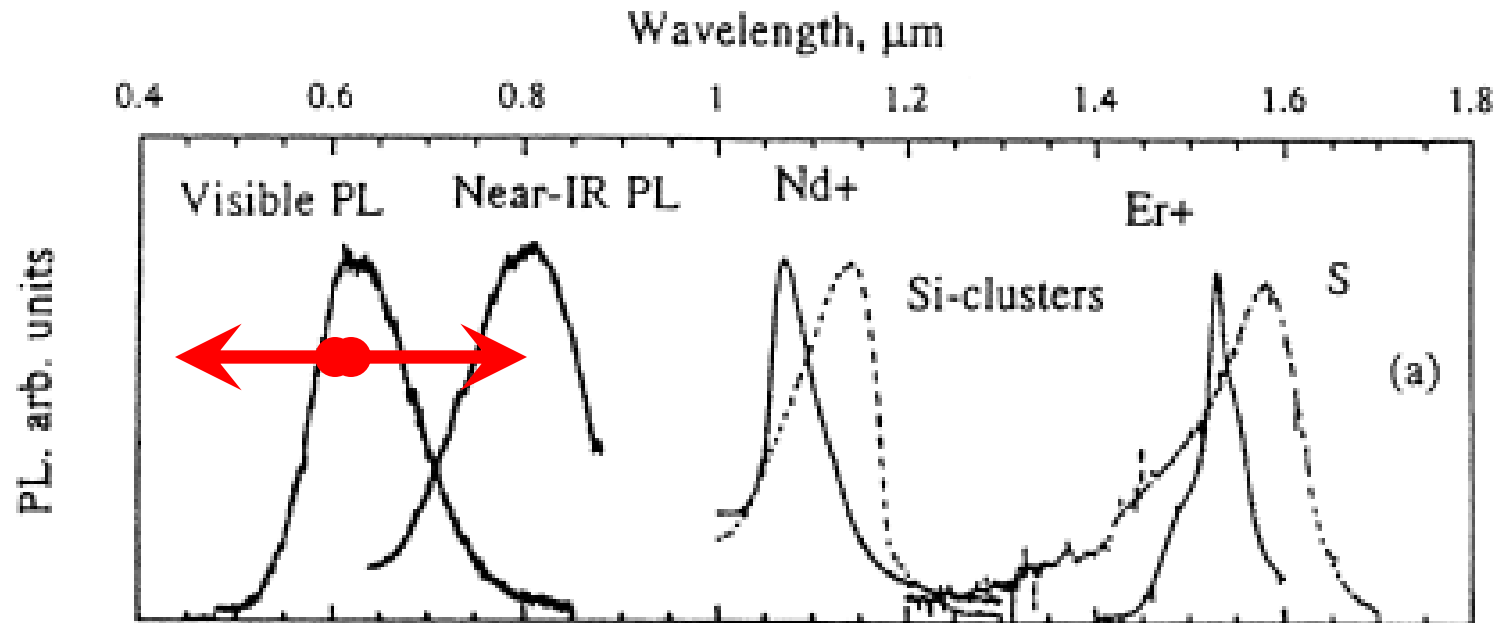
Bragg's reflectors



$$m\lambda_{Bragg} = 2(d_1n_1 + d_2n_2)$$

$$\lambda_{Bragg} \uparrow \Rightarrow d_{12} \uparrow n_{12} \uparrow$$

Photoluminescence of nano-porous Silicon at UV illumination at T_{room}

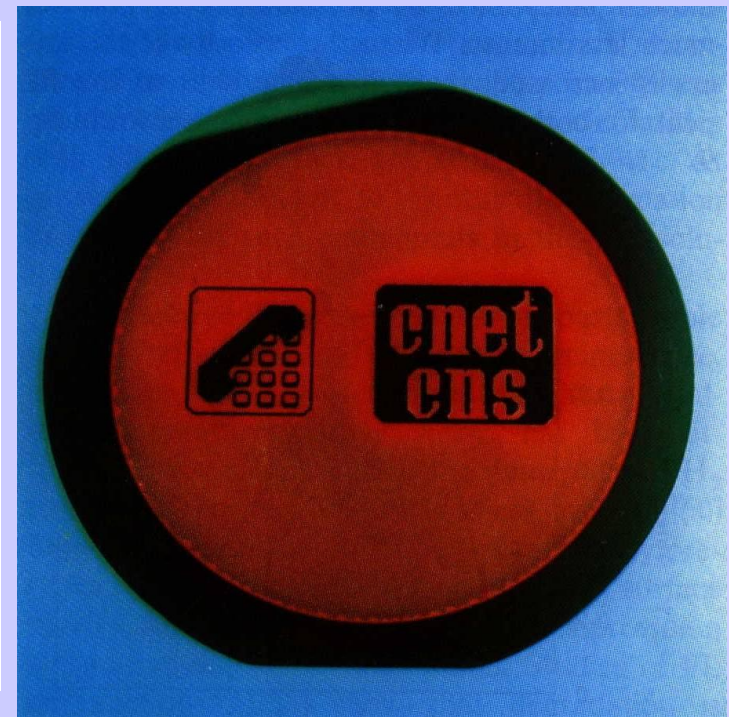
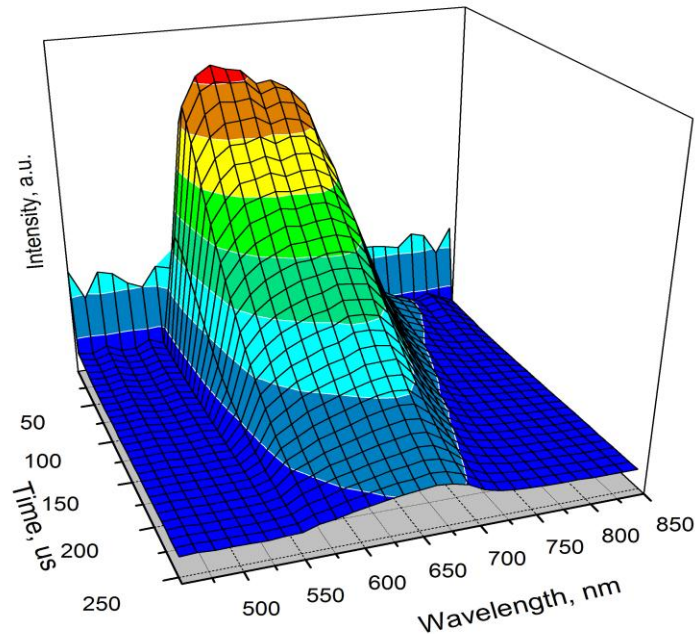


Spectral range	Peak wavelength	Label
UV	~350 nm	UV band
Blue-green	~470 nm	F band
Blue-red	400-800 nm	S band
Near IR	1100-1500 nm	IR band

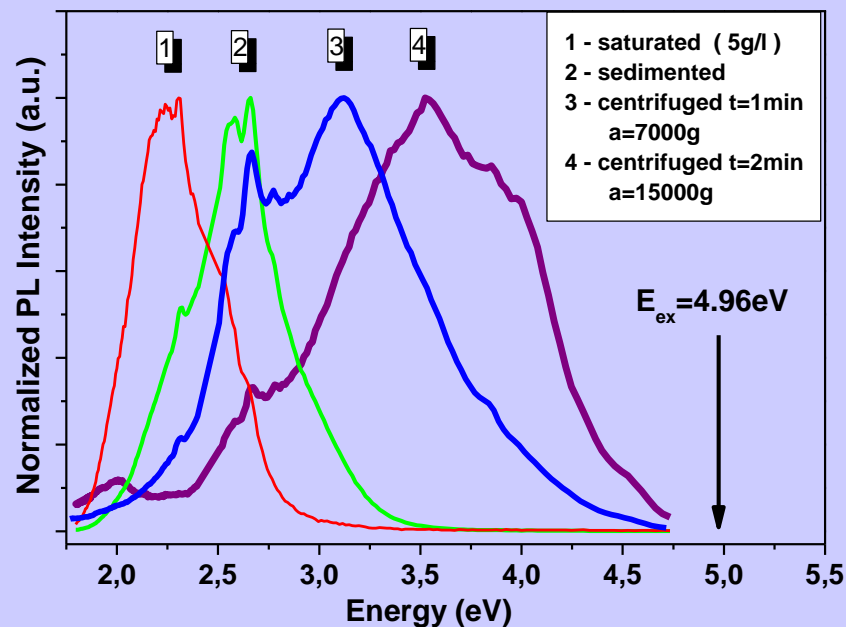
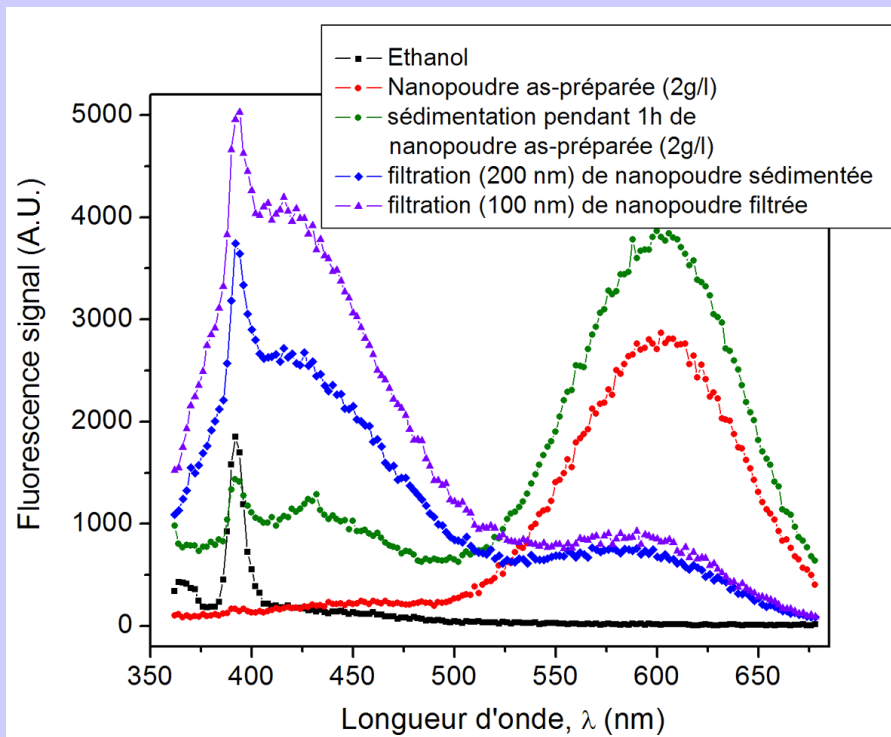
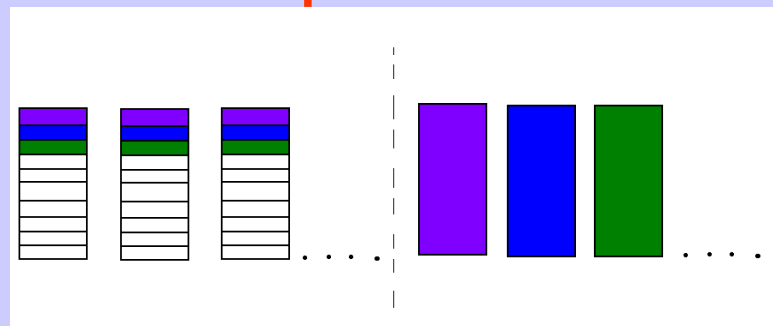
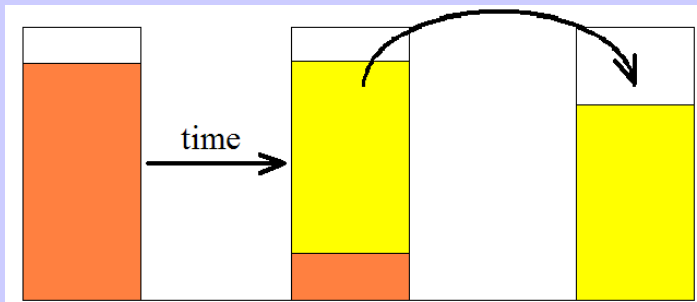
Photoluminescence of nano- porous Silicon

Some spectral characteristics of the S-band (adapted from Ref. [459])

Property	Typical values	Comments
Peak wavelength	1100–400 nm	At 300 K
PL efficiency	$\geq 5\%$	At 300 K and for external quantum efficiency
FWHM	0.3 eV	At 300 K (8 meV in porous silicon microcavities)
PL decay times	$\simeq 10 \mu\text{s}$	Strongly dependent on wavelengths, temperature and aging condition
Polarizability ratio	$P \leq 0.2$	
Fine structure under resonant excitation	Phonon replica at 56 and 19 meV	Heavily aged PS, energies typical of Si phonons



Photoluminescence of sediment Si nanoparticles



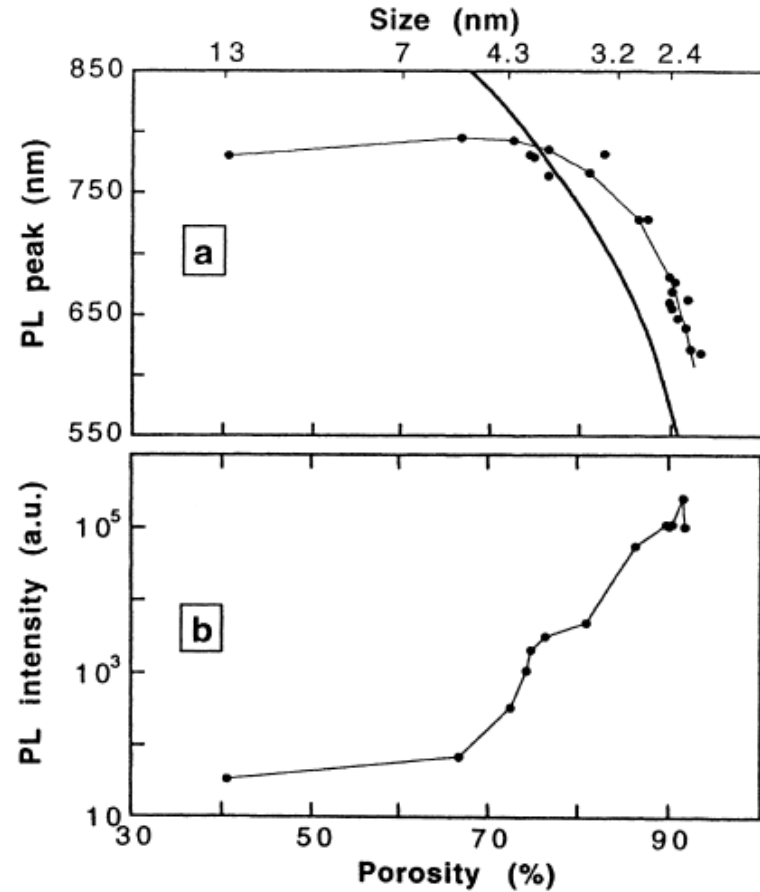
Sedimentation of ethyl solutions of Si nanoparticles + centrifugation

Photoluminescence of nano-porous Silicon



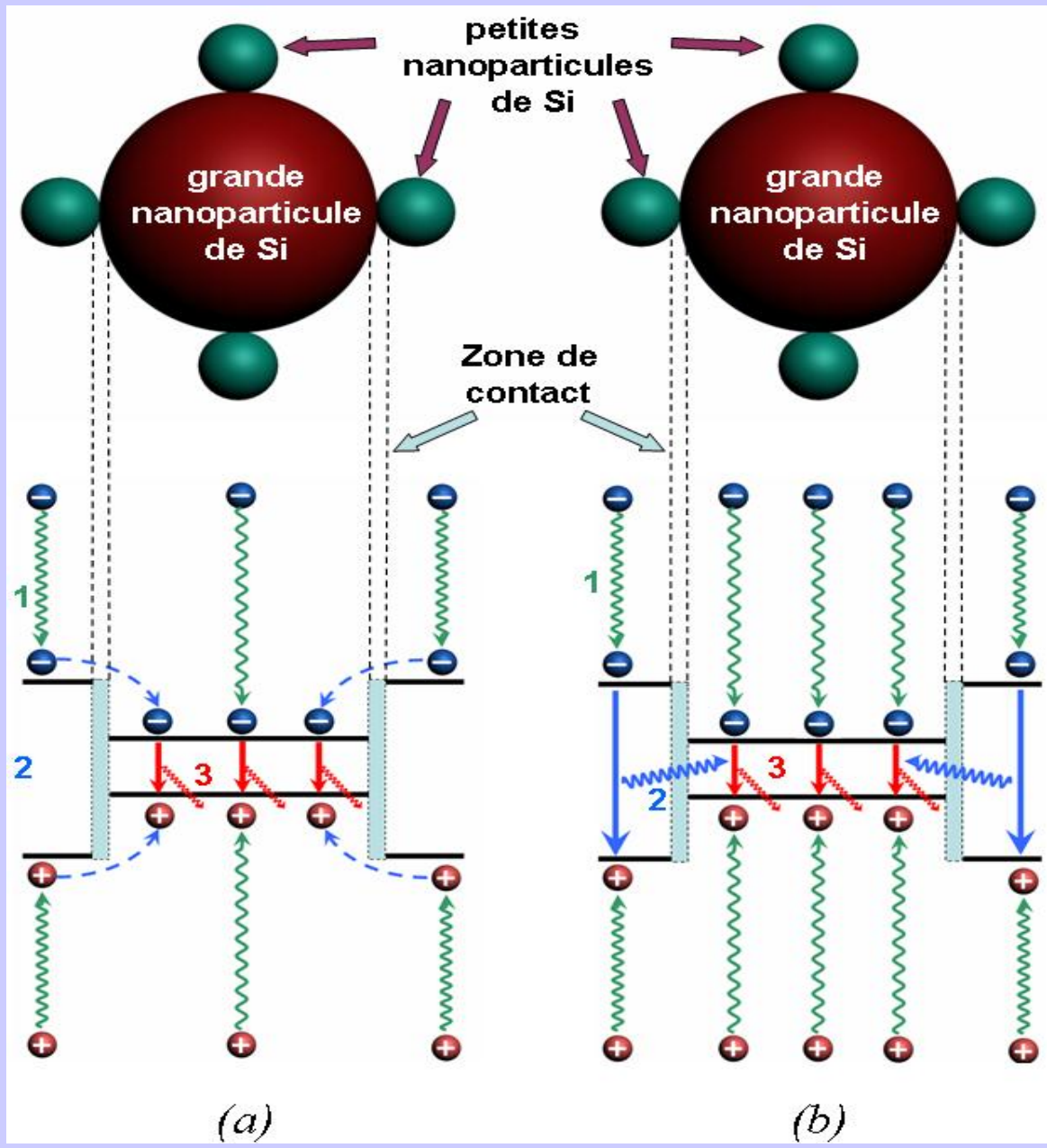
Emission of colloids of 4 members of the magic family 2.9, 2.15, 1.7 and 1.0 nm in diameter, after they have been separated, excitation 365 nm

V.Kumar, Nanosilicon, Elsevier, 2007

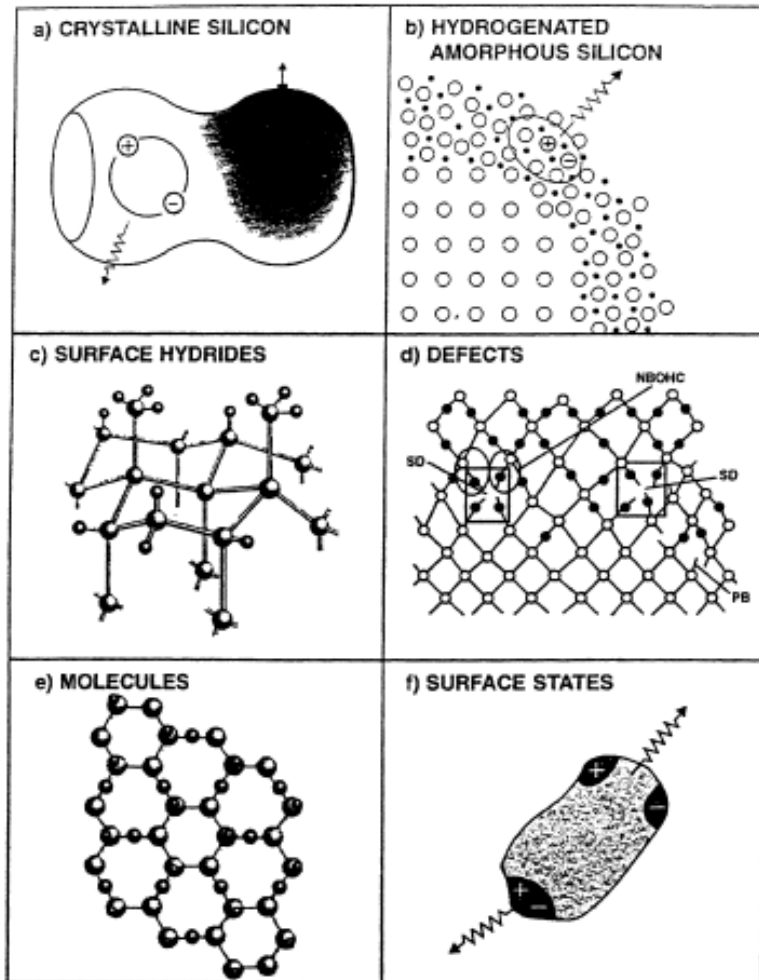


Emission peak and intensity vs size and porosity

Why UV Photoluminescence is not observed in solid PS?

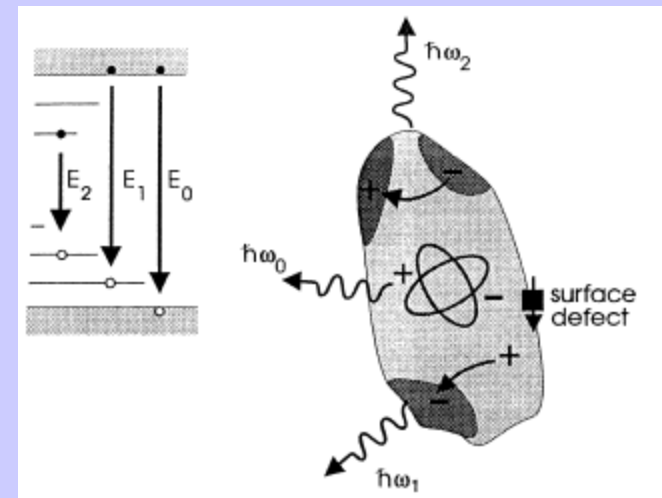


Photoluminescence models



KEY

- - silicon atoms
- - oxygen atoms
- - hydrogen atom

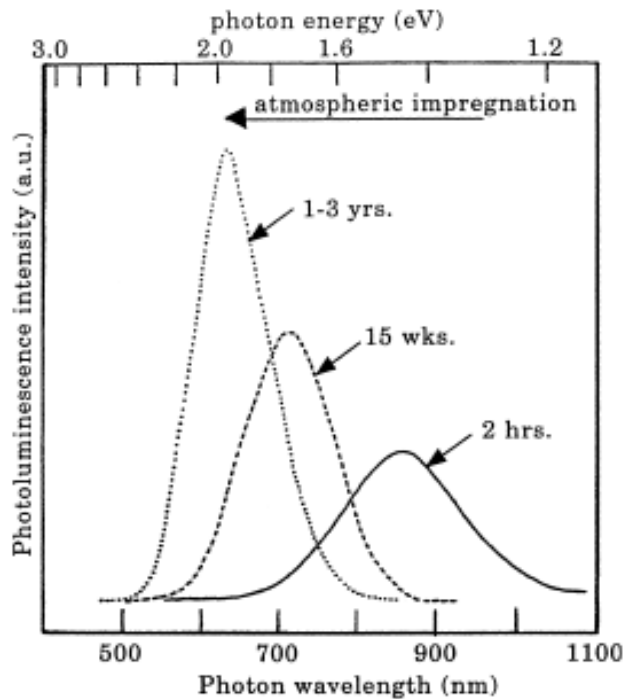


Hierarchy of transition in the SS model. The indices 0,1,2 indicate the number of SS involved

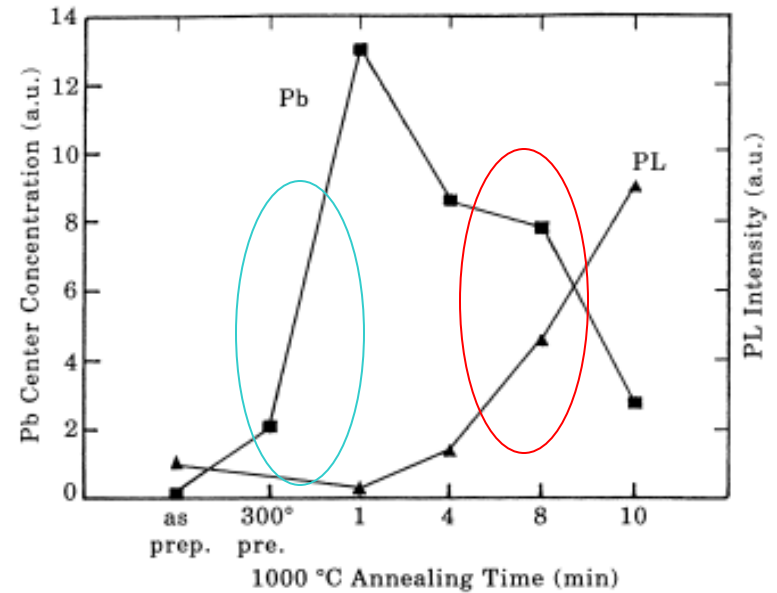
The six group of models proposed to explain PS PhL

- a) Crystalline QW. Localized on SS or free exciton recombination
- b) c-Si covered by layer of hydrogenated a-Si, where recombination occurs
- c) Si surface passivated by SiHx terminations. Radiative recombination occurs at the Si-H bonds
- d) Partially oxidized Si containing defects proposed as radiative centers
- e) Siloxene molecule $\text{Si}_6\text{O}_3\text{H}_6$ is proposed to exist on the large inner PS surface and act as luminescence center
- f) Si dot with SS that localize carriers and holes separately (upper part) or together (lower part, radiative recombination)

Photoluminescence aging and alternative model of PhL



Aging: blue shift of emission due to reduce of nanoparticle size



Dangling bond (Pb centers) concentration and PhL vs annealing time at 1000°C in O₂

Dangling bonds- most important paramagnetic defect centers: in Si/SiO₂ interface

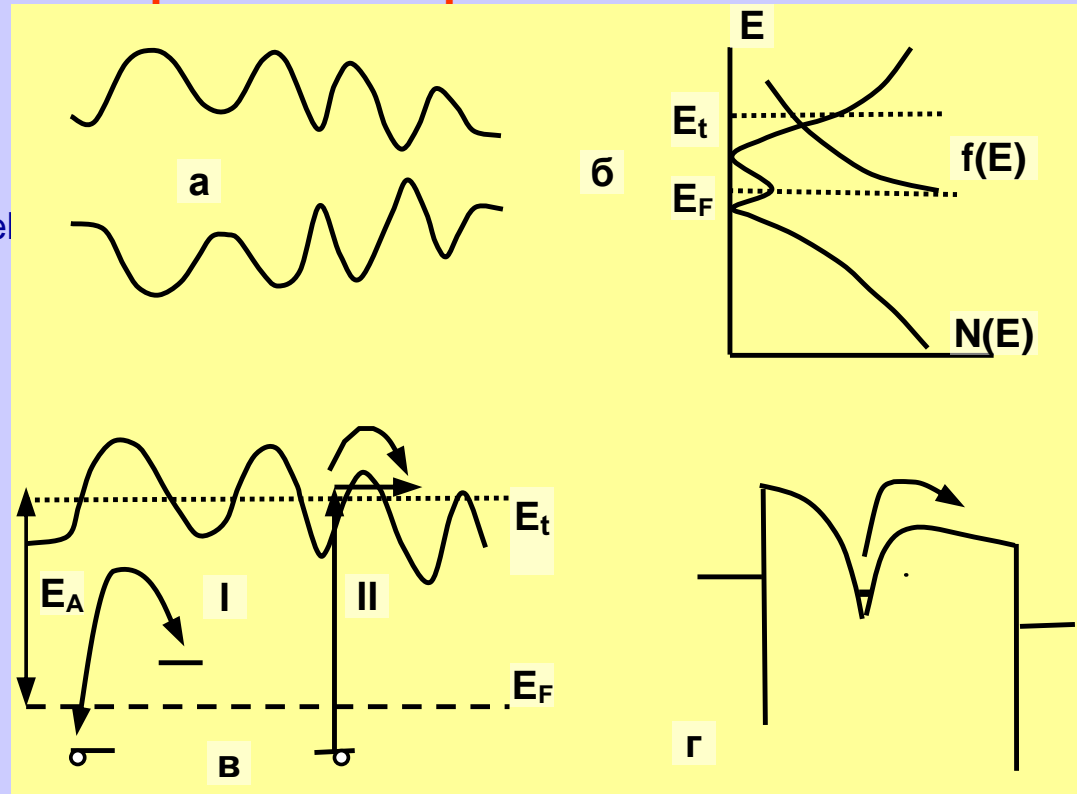
•**Si≡Si₃ (Pb centers)**

in hydrogen depleted oxide layer

•**Si≡SiO₃ (E' center)**

Electrical transport in microporous Si

- a. Bandgap fluctuation due to variation of nanocrystalline size,
- b. density of states in forbidden band, E_t - level of current leaking, $f(E)$ –distribution function
- c. transport mode: hopping on surface states(I), thermogeneration, thermoionic or tunneling across state tails
- d. Poole-Frenkel mechanism



Surface states:

Density $>10^{12}-10^{14} \text{ cm}^{-2}\text{eV}^{-1}$

Free carriers:

Density $<10^{10}-10^{13} \text{ cm}^{-3}$

Mott law for jump (hopping):

$$\sigma(T) = \sigma_0 \exp(T / T_0)^m, m = 4$$

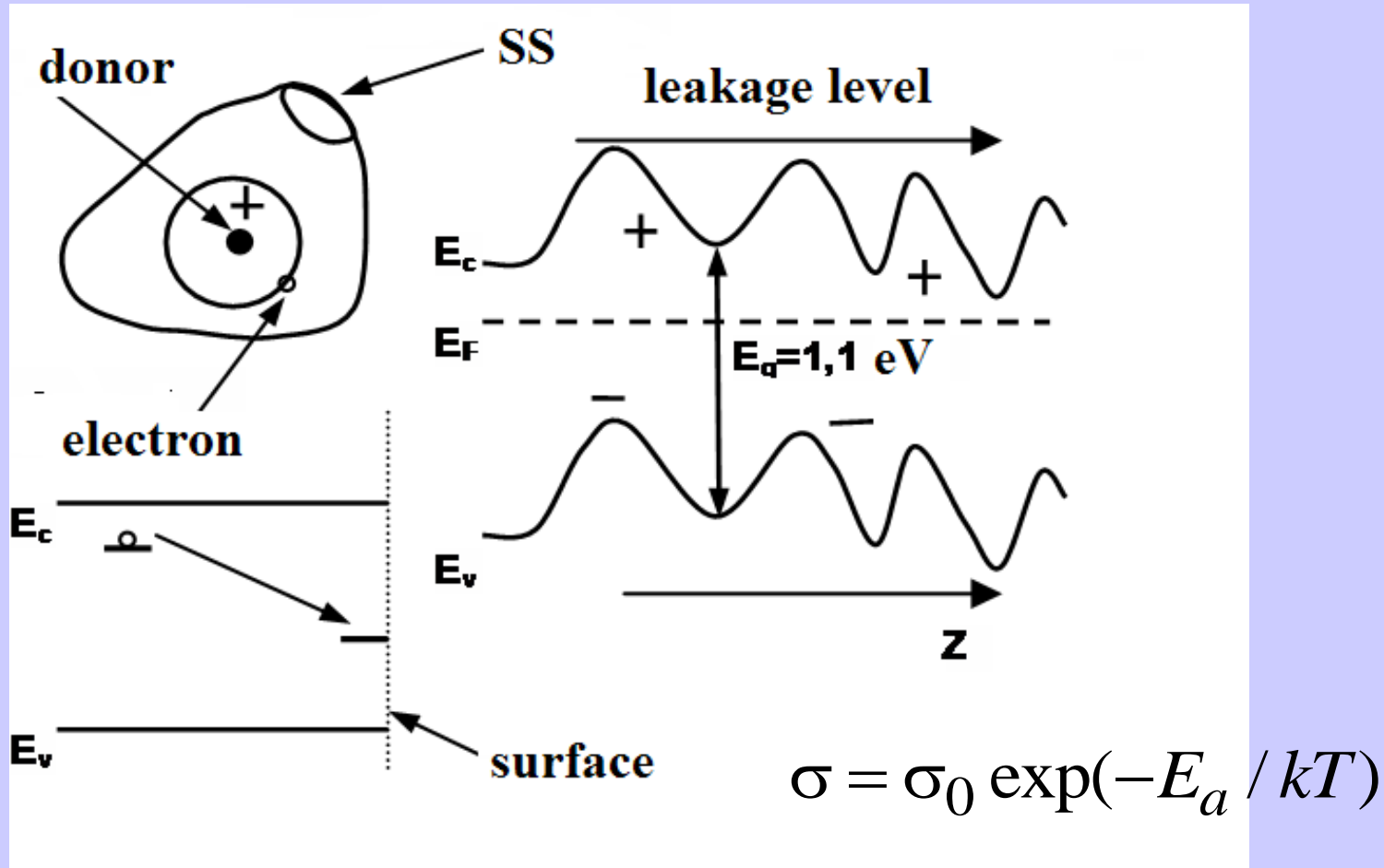
Poole-Frenkel ionisation:

$$\sigma(V, T) = \sigma_0 \exp\left(\frac{E_a}{kT}\right) \exp\left(\beta \sqrt{\frac{V}{V_0(T)}}\right)$$

Space charge limited current:

$$I = \gamma(T) \frac{V^n}{d^m}, \quad n \sim 2$$

Electrical transport in macroporous Si



Initial Si is heavy doped, but meso-PS is high resistive!

a) Cross-section of Si microwire that shows the process of free electron capture on surface state of acceptor type, b) energetic sketch of process, b) band modulation due to electric field between D⁺ and negatively charged SS. Z- direction along Si microwire

New perspectives: Other stable Si nanoparticles

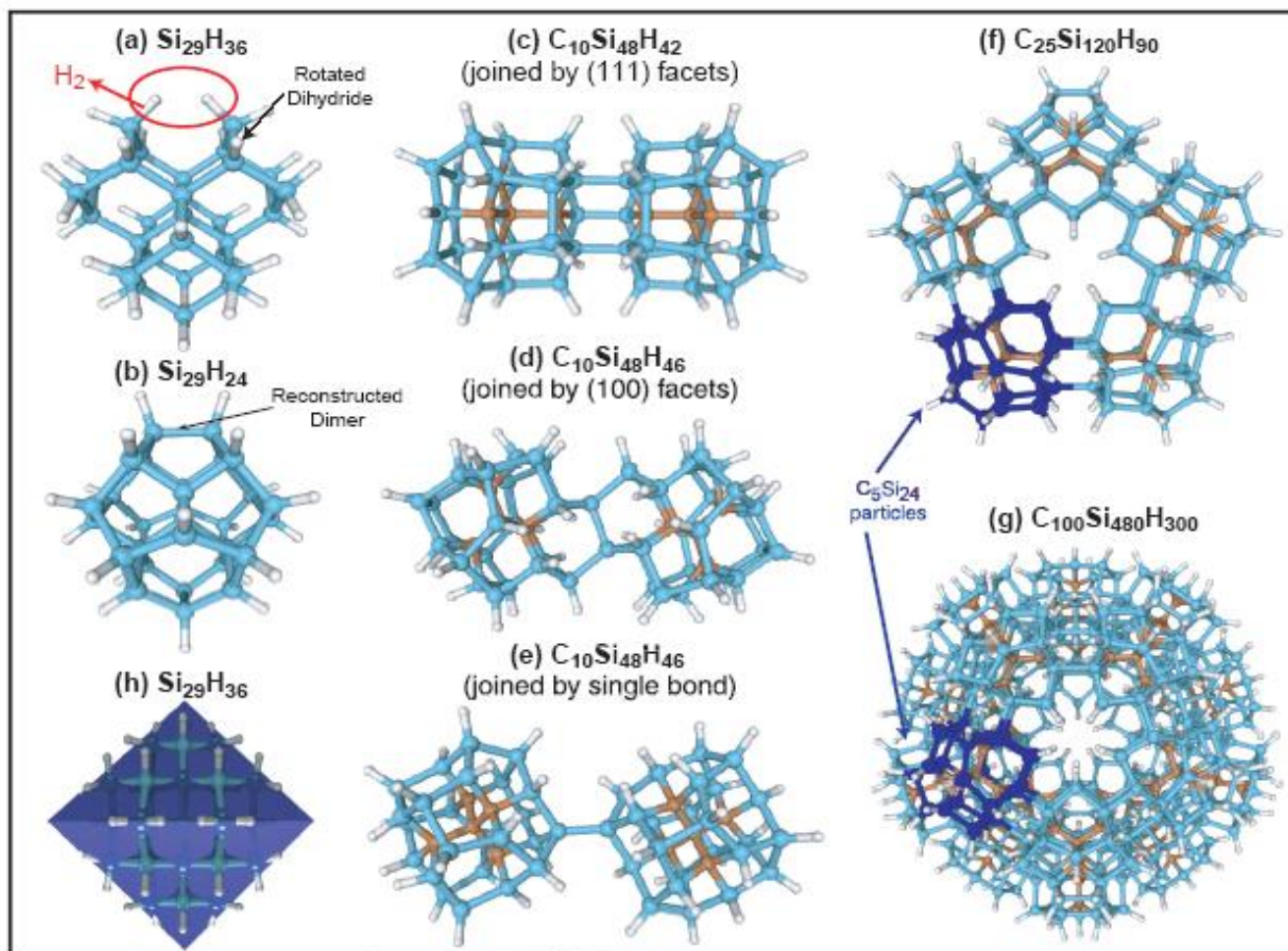


FIG. 1: Calculated atomic structures of single, double, 5-fold and 20 nanoparticles structures. Si, C and H atoms are colored blue, brown and white. In (f) and (g) atoms in a single C_5Si_{24} particle are highlighted in dark blue.

Properties of Micropores or nanocrystalline Si. Summary

Features:

- Surface area – 200- 500 m²/cm³
- E_g = 1.1- 3.0 eV
- Resistivity $\rho = 10^8$ - 10^{12} Ω .cm
- Carrier mobility $10^{-3} - 10^0$ cm²/V.s
- Quantum efficiency of PL- more than 10 %
- Quantum efficiency of EL - 1 %
- Chemical composition (Cullis A.G., Canham L.T, J.Appl.Phys, 82(1997) 909).

Condition of porous Si	Chemical composition
1. In situ in HF during and after formation	SiF _x H _y
2. Freshly etched in inert ambient	SiH _x
3. Chemically or anodically oxidized	SiO _x H _y
4. Rapid thermally oxidized at high temperatures	
5. Aged in ambient air for months to years	SiO _x H _y C _z